



R-mode instability and related phenomena

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Outline

- Ways R-modes could be interesting
- What we did
- Conclusions

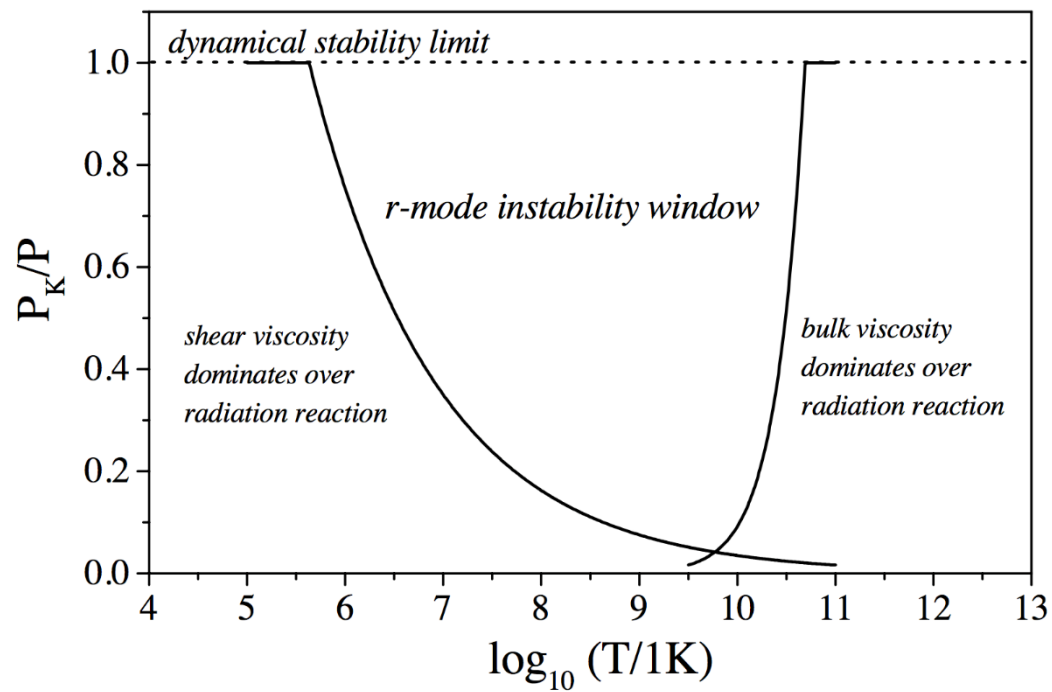
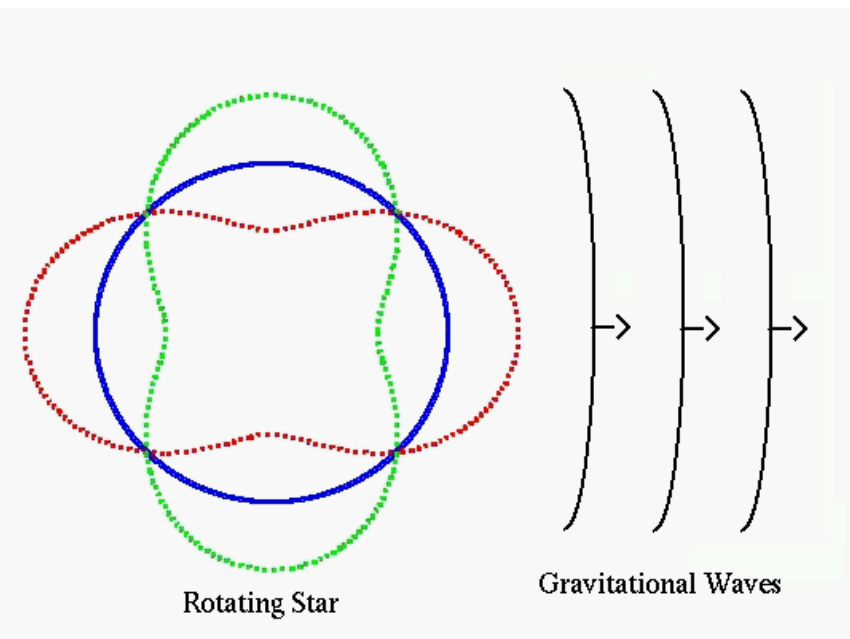
Way R-modes could be interesting

- R-modes can produce **Gravitational waves**
- direct way to **probe the interior of compact stars**

R-mode instability

- GR tends to drive all rotating stars unstable!

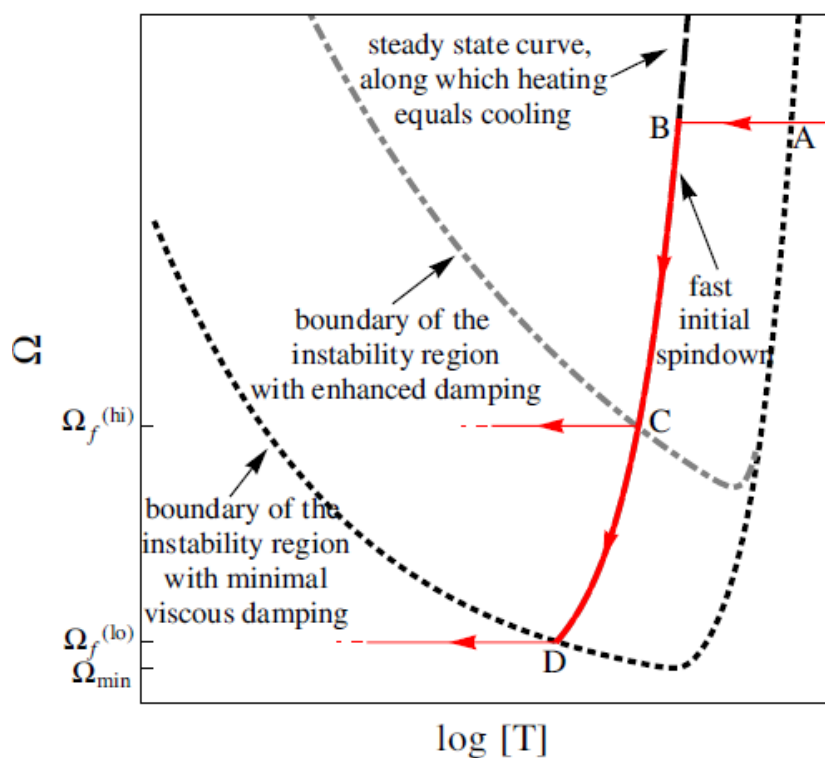
- Internal dissipation in the star can suppress the instability



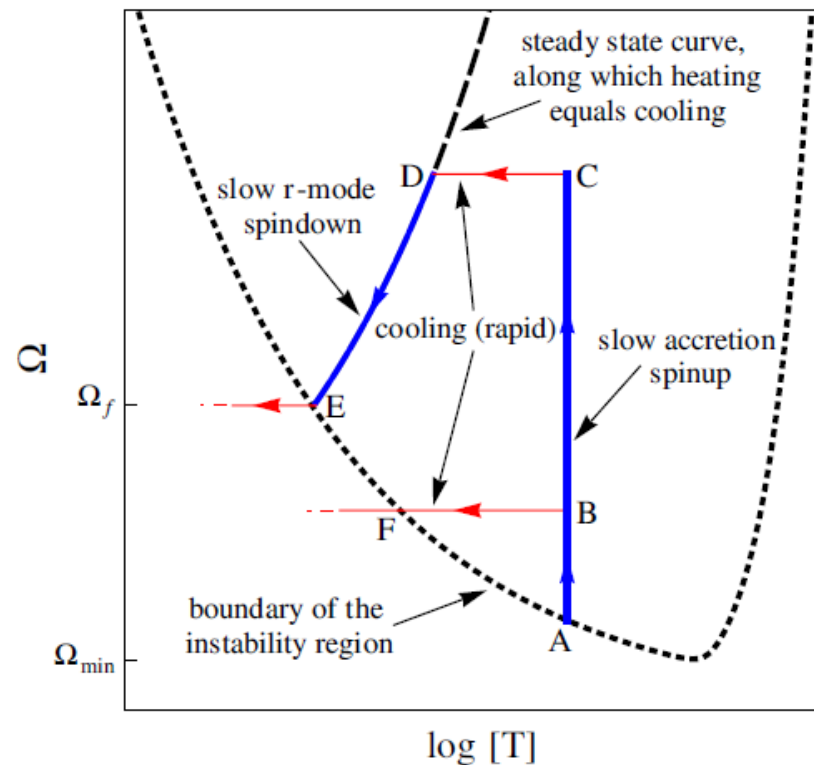
N. Andersson & K.D.Kokkotas, IJMPD, 2001
K.D.Kokkotas & K. Schweizer, EPJA, 2016

R-mode gravitational wave scenarios

$$h_0 = \sqrt{\frac{2^{15} \pi G}{365} \tilde{J} M R^3 \frac{\chi^2 \Omega^3 \alpha}{D}}$$



newly formed compact stars
young sources



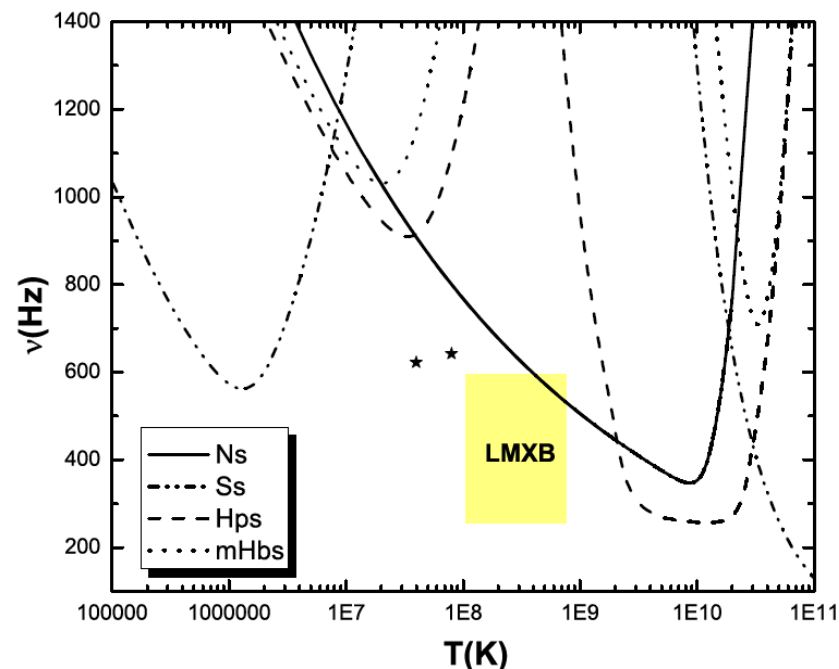
sources in LMXBs
millisecond pulsars

R-mode instability window

- competition between the destabilizing effect of GR and the damping effect of viscosity

- $dE/dt > 0$, r-mode increase, GW emission
- $dE/dt < 0$, r-mode decrease, no instability
- critical condition $\frac{dE}{dt} = 0$

$$\frac{1}{\tau_{gw}} + \frac{1}{\tau_v} = 0$$



Pan et al., 2006
K.D.Kokkotas & K. Schweizer, EPJA, 2016

R-mode instability and GW emission

$$\frac{1}{\tau_{GW}} + \frac{1}{\tau_V} = 0$$

- $\frac{1}{\tau_{\xi}} = \frac{4\pi}{690} \left(\frac{\Omega^2}{\pi G \bar{\rho}} \right)^2 R^{2l-2} \left[\int_0^R \rho r^{2l+2} dr \right]^{-1} \int_0^R \xi \left(\frac{r}{R} \right)^2 \left[1 + 0.86 \left(\frac{r}{R} \right)^2 \right] r^2 dr$
- $\frac{1}{\tau_{\eta}} = (l-1)(2l+1) \left[\int_0^R \rho r^{2l+2} dr \right]^{-1} \int_0^R \eta r^{2l} dr$
- $\frac{1}{\tau_{GW}} = \frac{32\pi G \Omega^{2l+2}}{c^{2l+3}} \frac{(l-1)^{2l}}{[(2l+1)!!]^2} \left(\frac{l+2}{l+1} \right)^{2l+1} \int_0^R \rho r^{2l+2} dr$

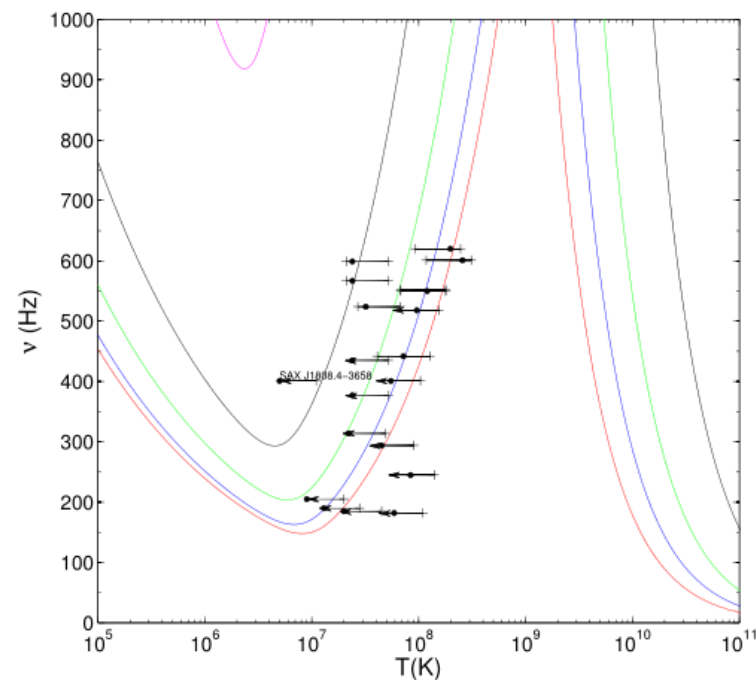
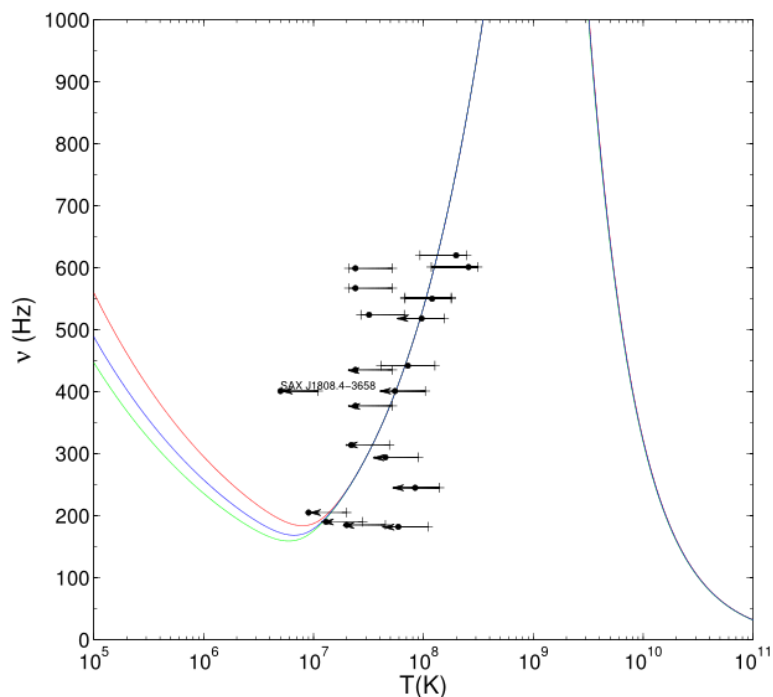
$$C_V \frac{dT}{dt} = -L_\nu - L_\gamma + H,$$

$$\frac{d\Omega}{dt} = -\frac{\Omega}{\tau_m} - \frac{2Q\alpha^2\Omega}{\tau_v},$$

$$\frac{d\alpha}{dt} = \alpha \left(\frac{1}{\tau_g} - \frac{1 - \alpha^2 Q}{\tau_v} + \frac{1}{2\tau_m} \right)$$

- ✓ EOS
- ✓ Dissipation mechanisms
- ✓ R mode saturation amplitude α_{sat}
- ✓ Thermal evolution/Spin evolution

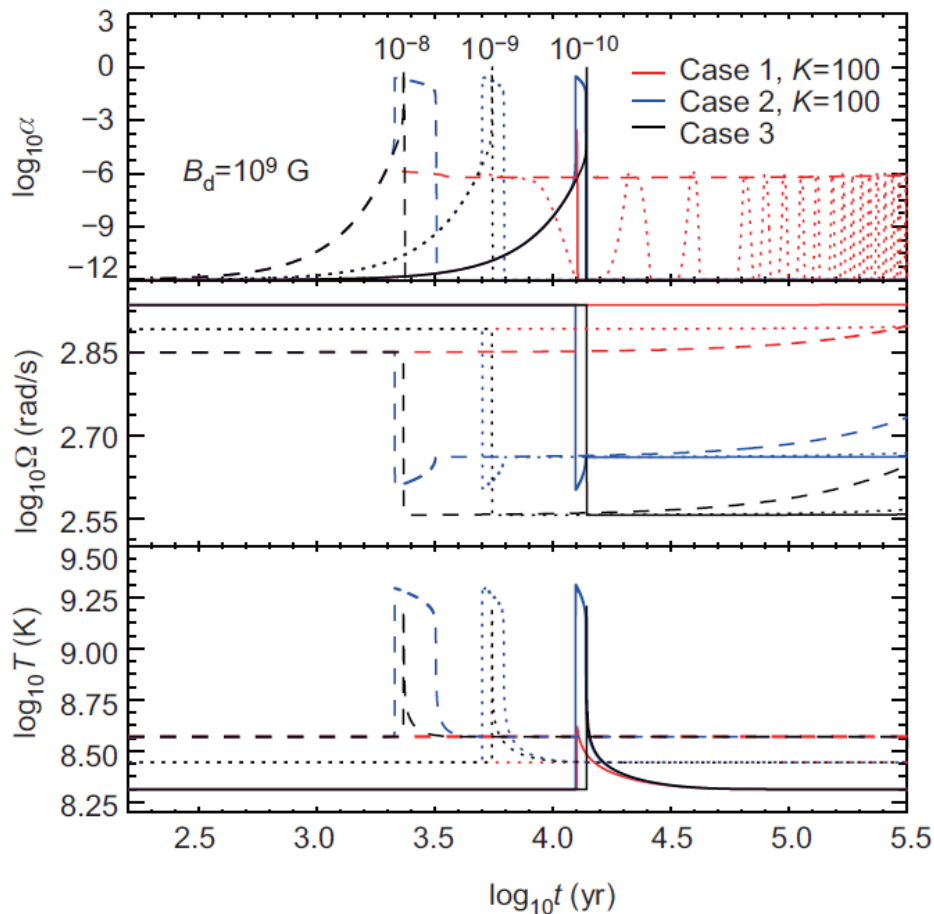
R-mode instability windows and EOS



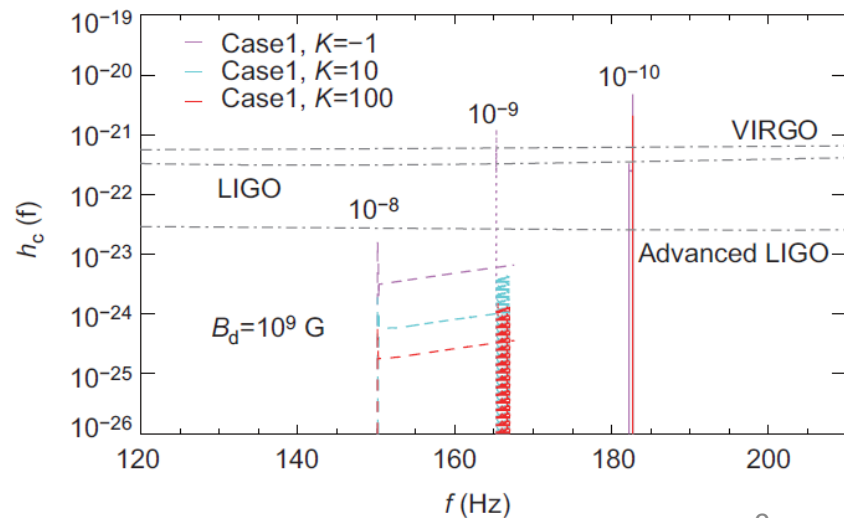
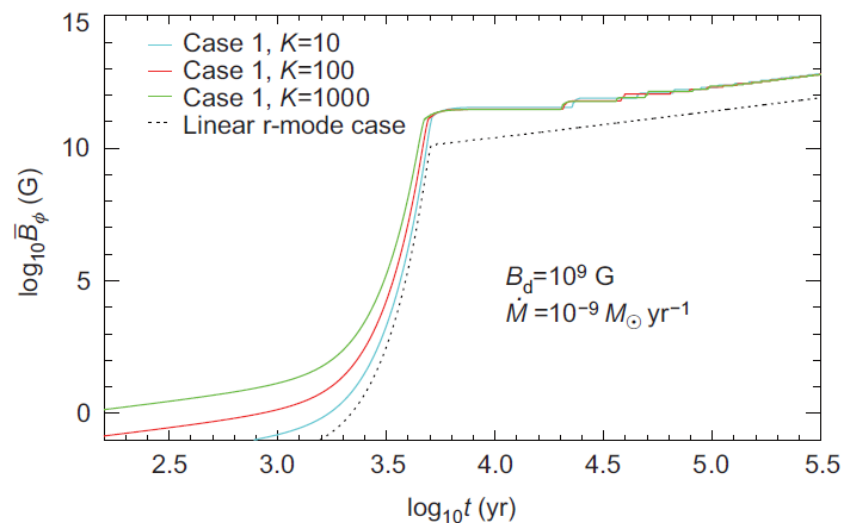
Wang et al. 2018, in preparation

- Constraints on interquark interaction parameters with GW170817 and two-solar-mass pulsar observations (Zhou et al. 2018, PRD)

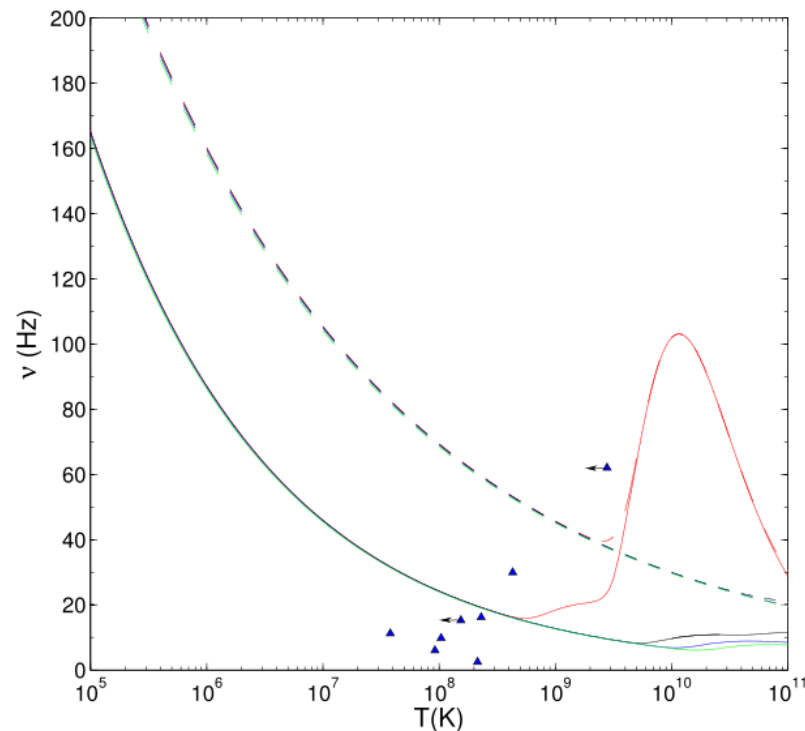
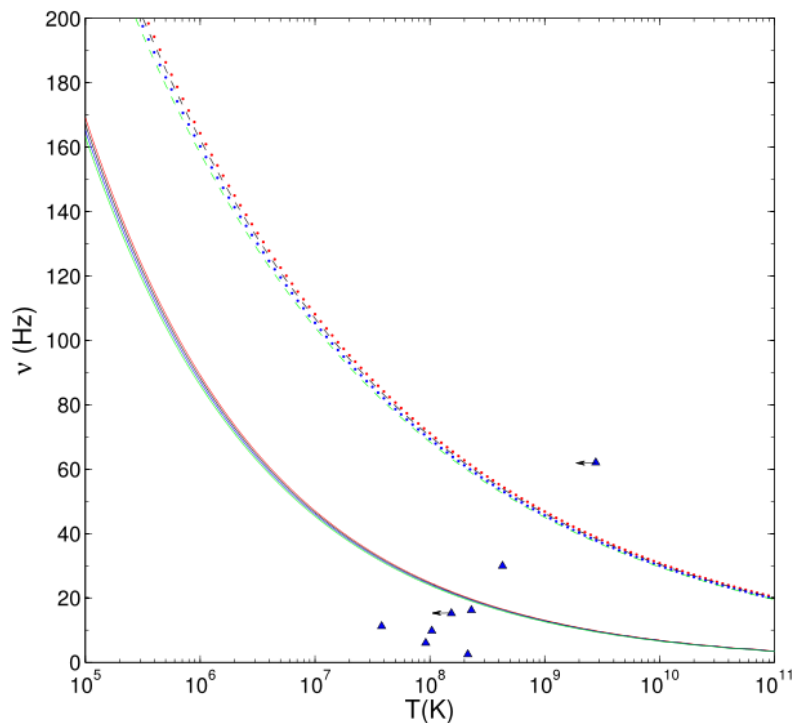
R-mode instability and Dissipation mechanisms-magnetic damping



Cao et al., 2015, *Sci China-Phys Mech Astron*



R-mode instability and Dissipation mechanisms

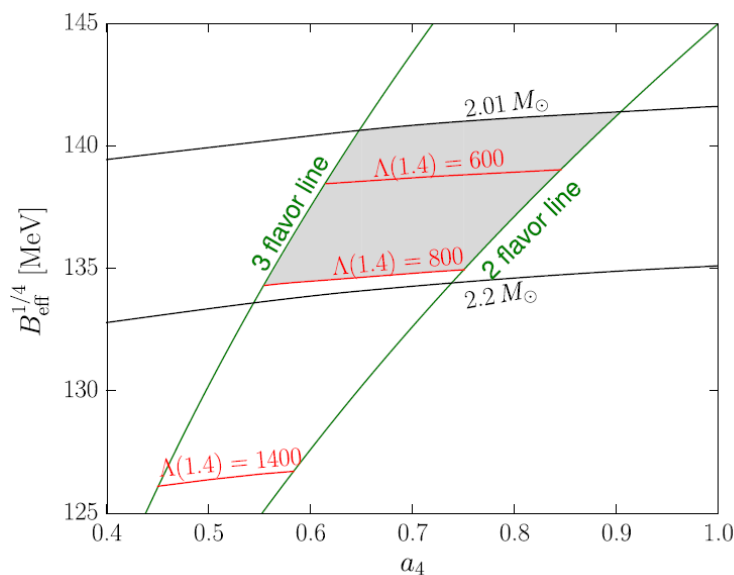


Surface rubbing and shear viscosity due to electron-electron scattering

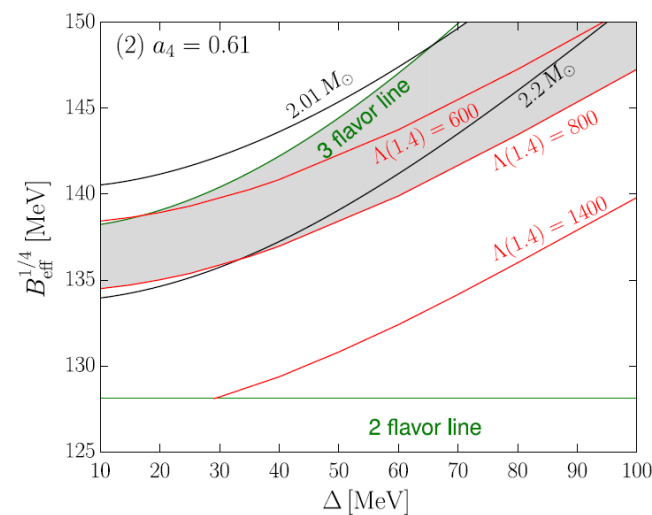
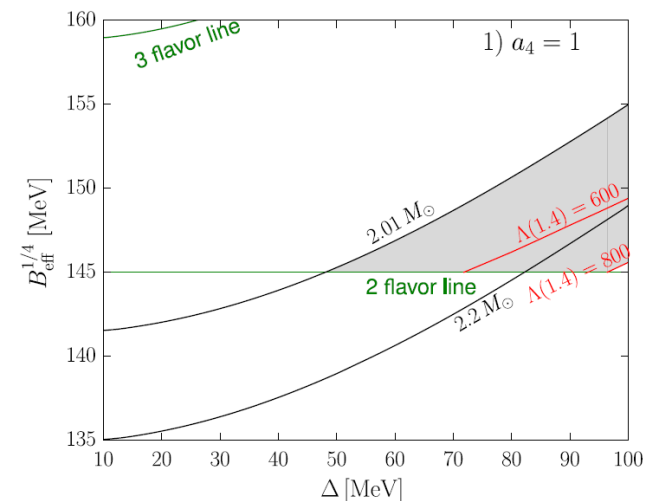
Wang et al. 2018, in preparation

Parameters of r-mode instability

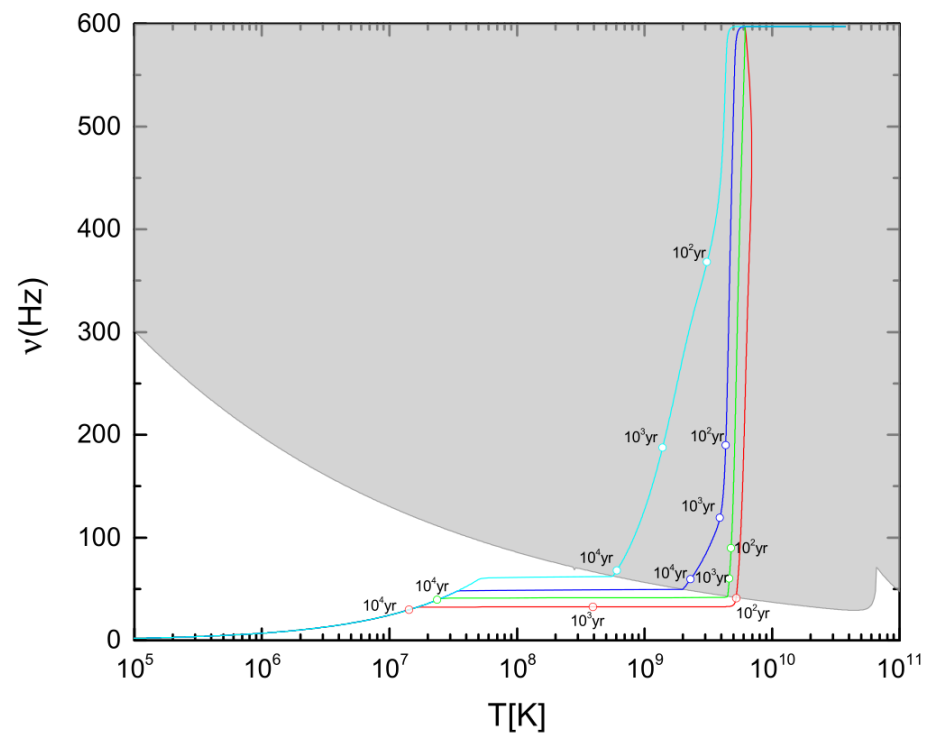
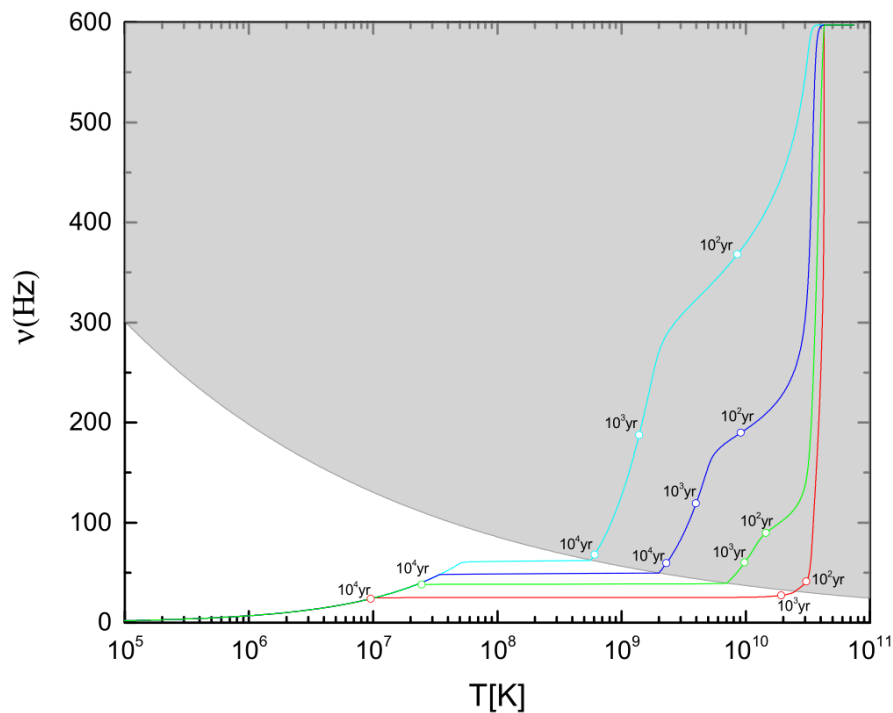
- **Problem:** model parameters α_{sat} , Δ
- ✓ **Observation:** constraint the parameters



PSR J2215+5135 $M_1 = 2.27^{+0.17}_{-0.15} M_\odot$



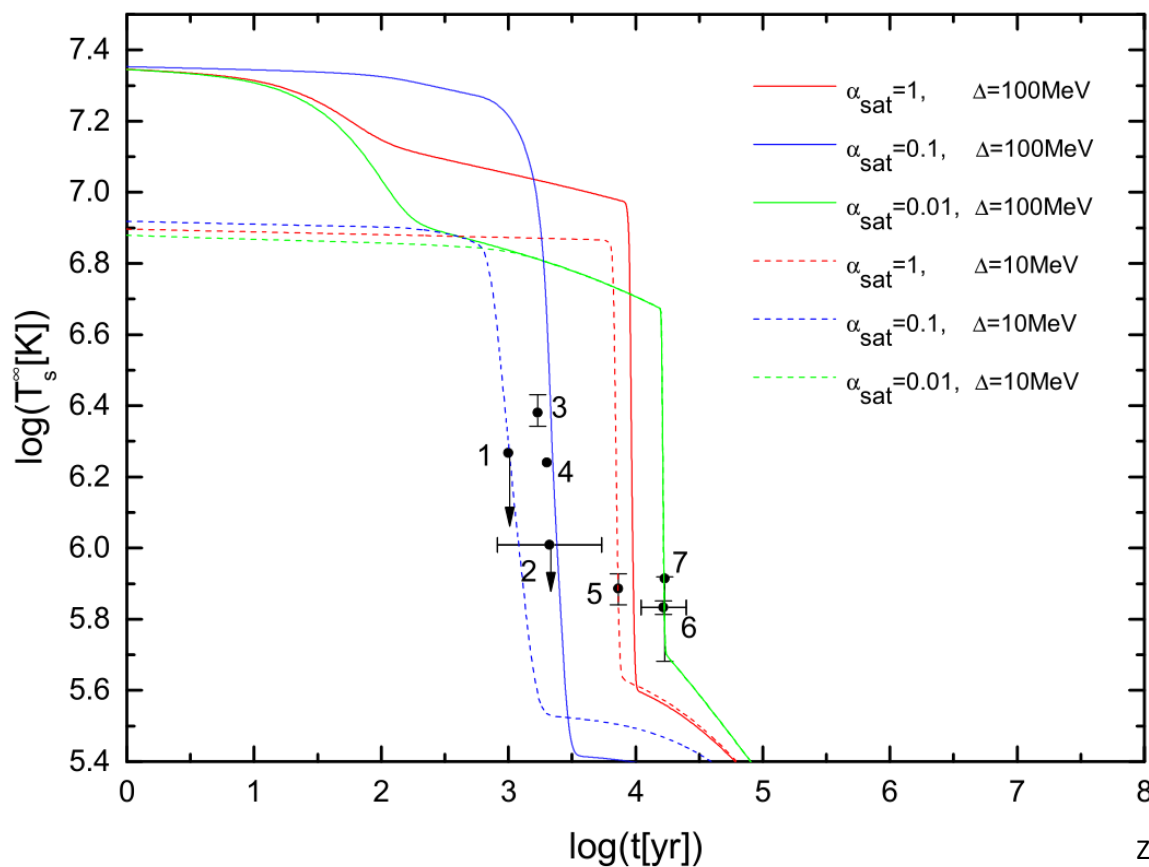
R mode saturation amplitude α_{sat}



$\alpha_{sat} > 0.01$

Zhou et al. 2018, in preparation

R-mode instability and thermal evolution of young pulsars



Zhou et al. 2018, in preparation

Conclusion

- Using multiple observational data to constrain the model parameters in a reasonable regime
- A more realistic structure of compact stars
- $N \sim 7$
- gravitational wave emission

