

Neutron star phase transition Probed via interfacial modes

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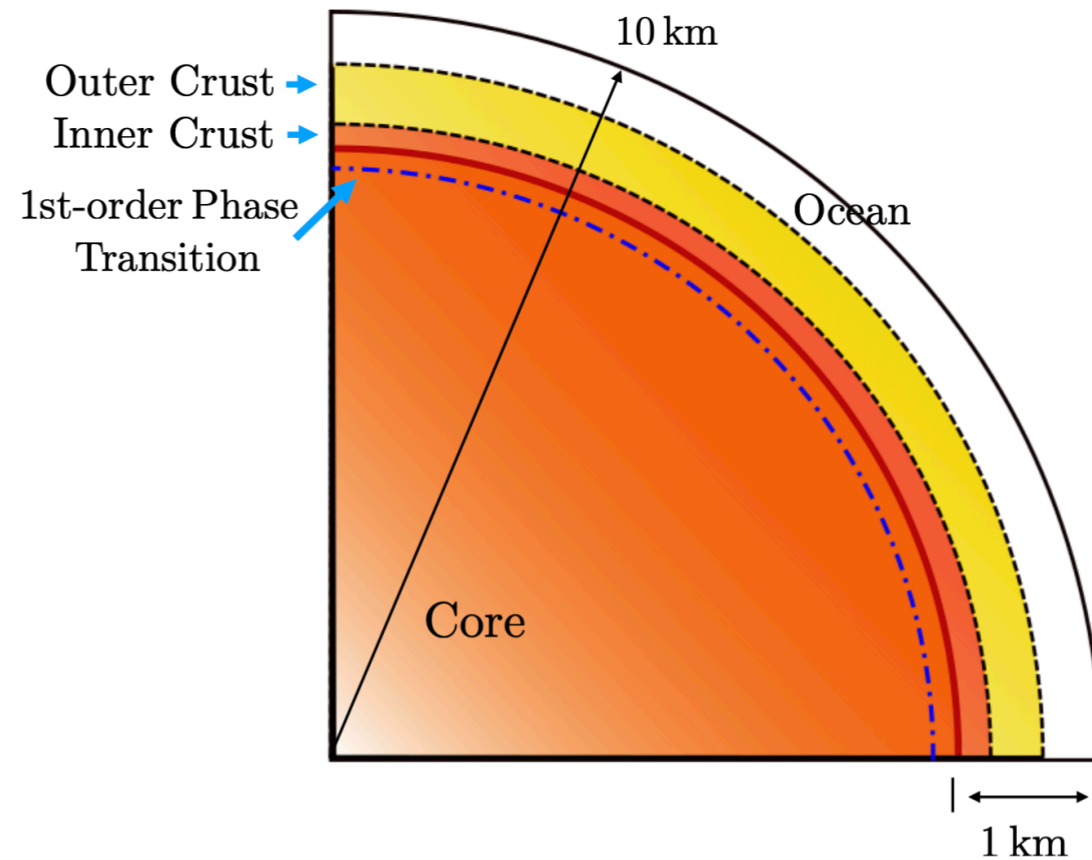
Yangzhou, QCS-2023 2023-Sep-24

Outline

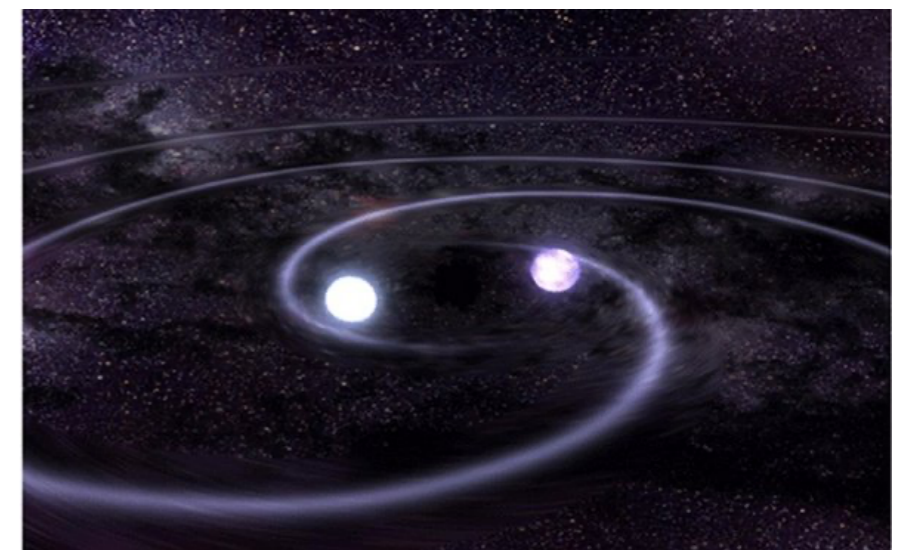
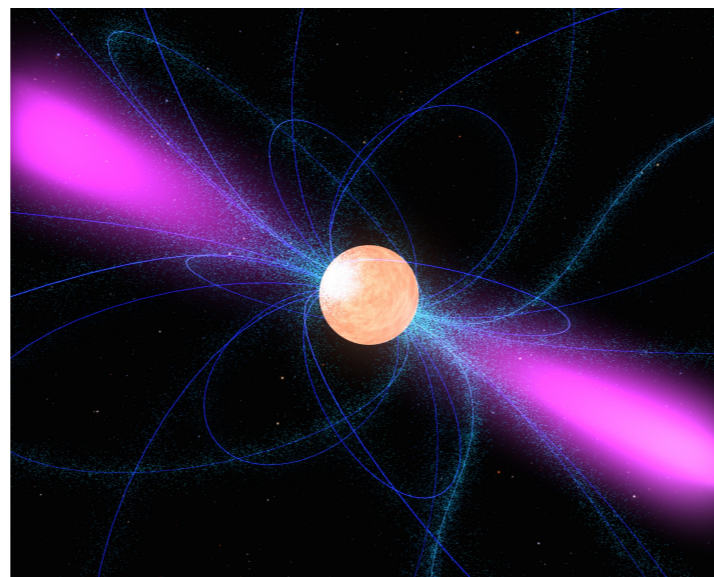
- 1: Neutron star structure and exotic dense matter phase**
- 2: First order phase transition in NSs**
- 3: Neutron star seismology and Interfacial mode**
- 4: Detectability using gravitational waves**
- 5: Discussions and Outlook**

Neutron star structure

- **Densest Star**
- **Strong interacting matters**

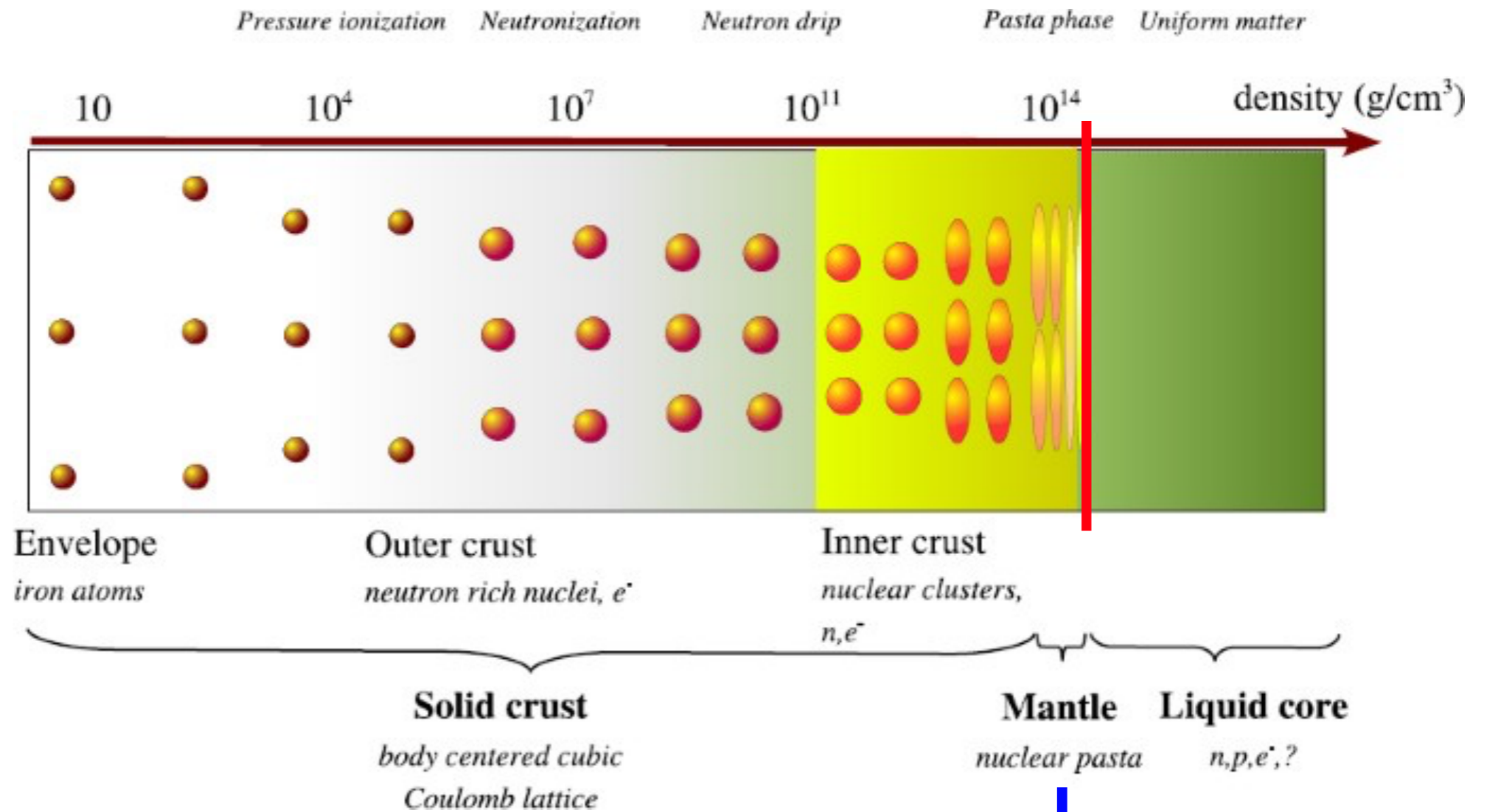


- **Radio Pulsars**
- **Can form binary GW source**



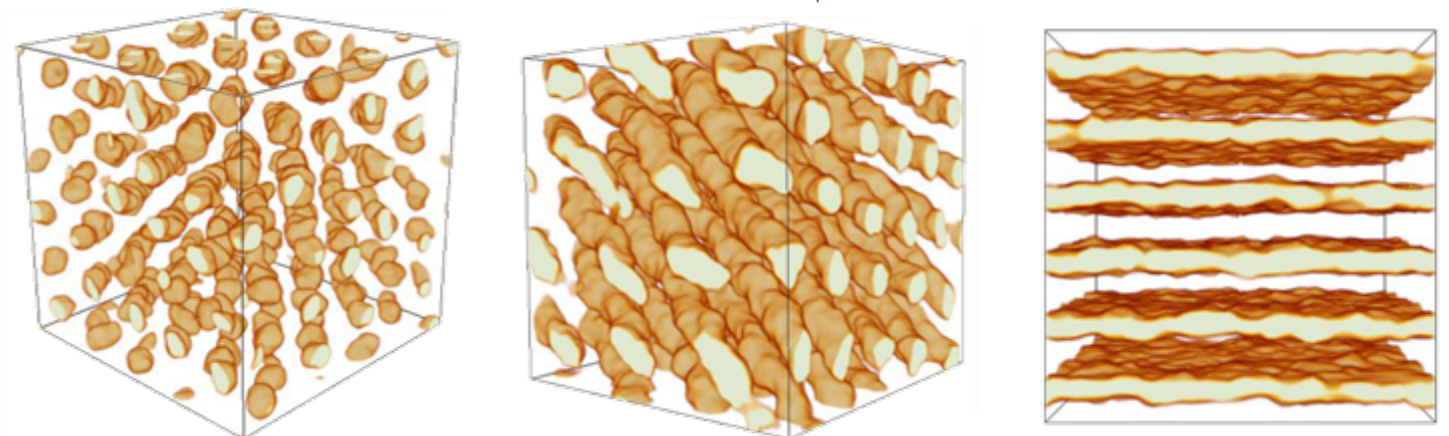
Neutron star matter: Crust+Mantle

Matter phase
in an NS



Nuclear Pasta phase
in an NS: crust-core transition

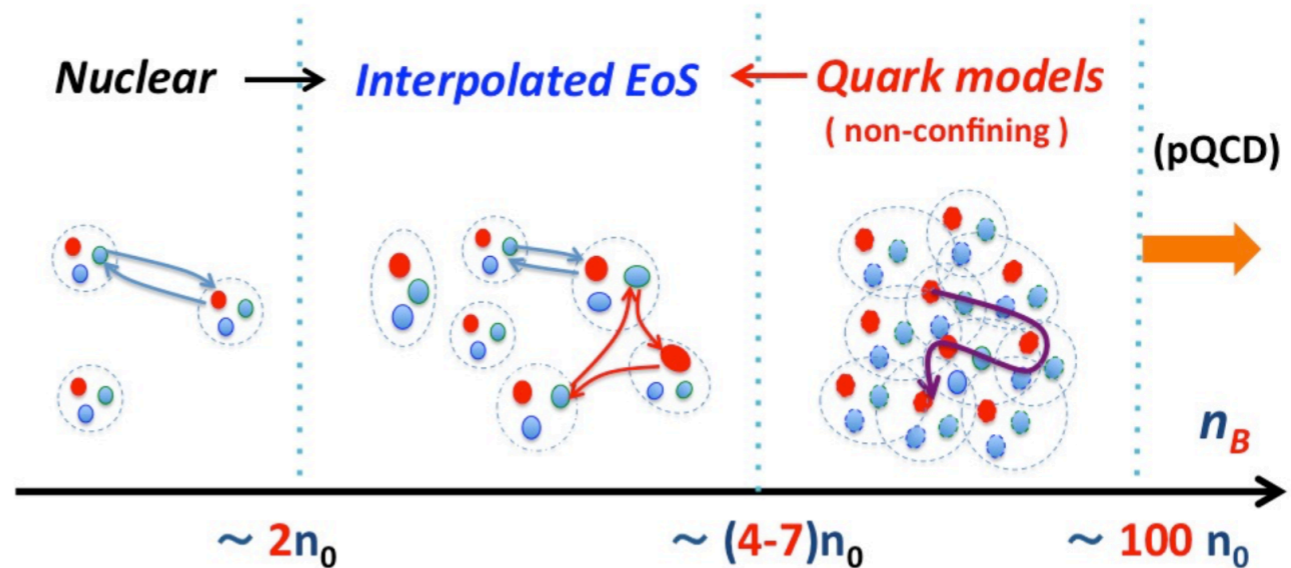
Shear modulus could jump



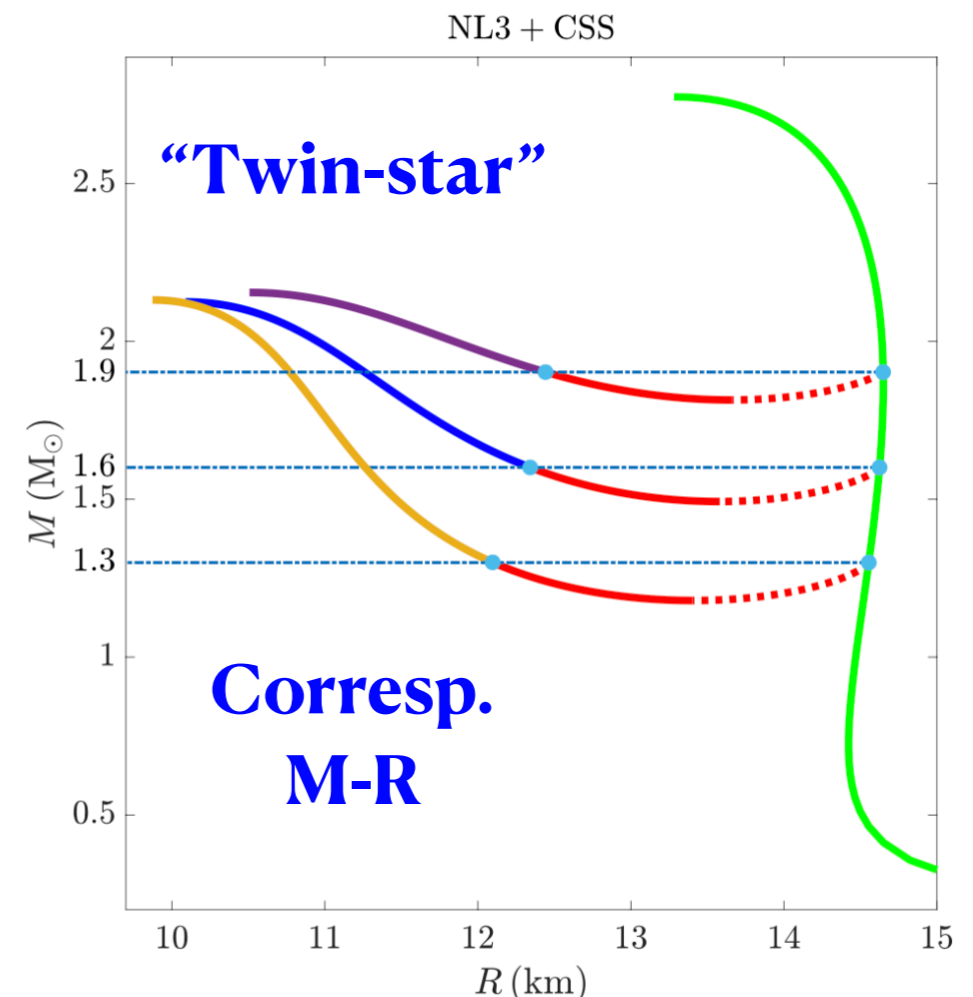
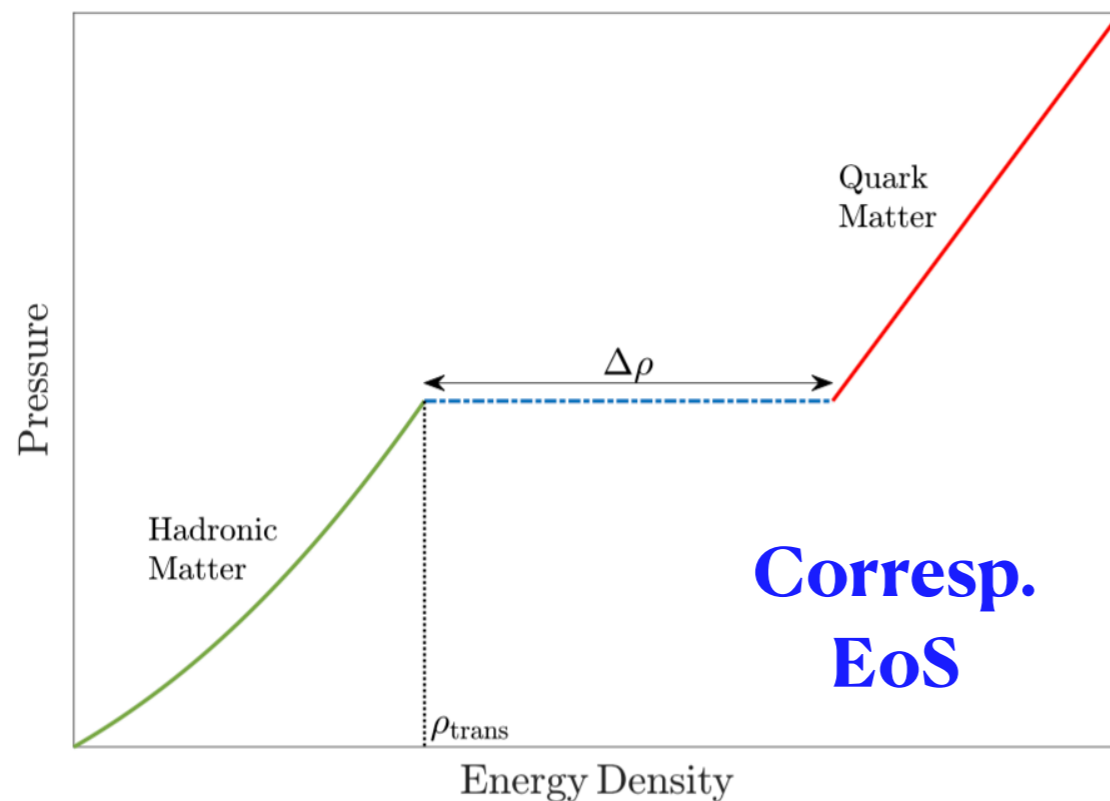
Neutron star matter: Inside the core

Possible
Hadron-Quark
Phase transition

1st order transition

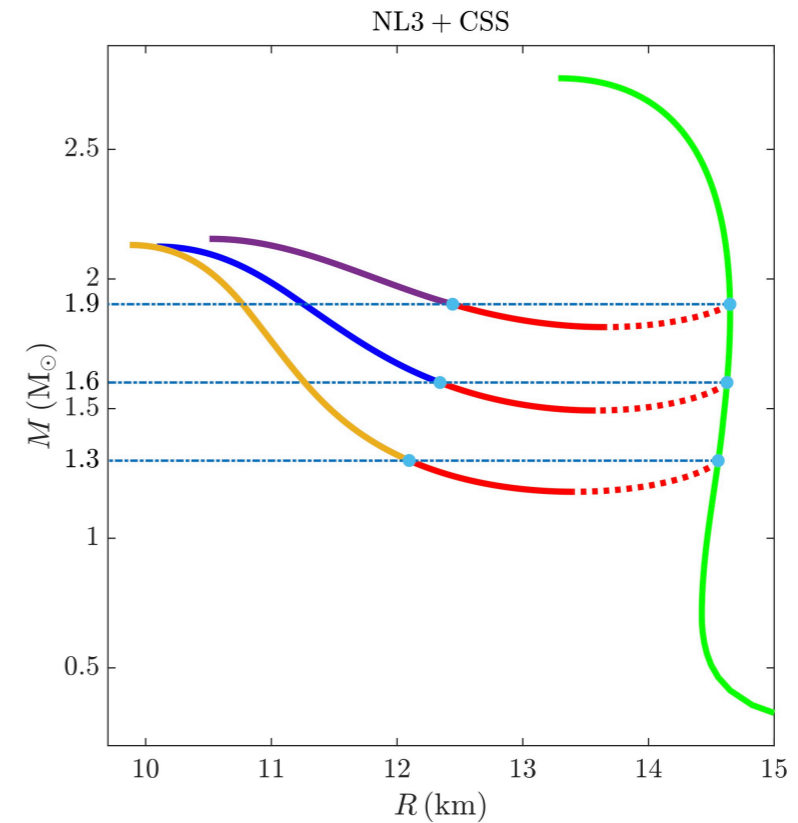
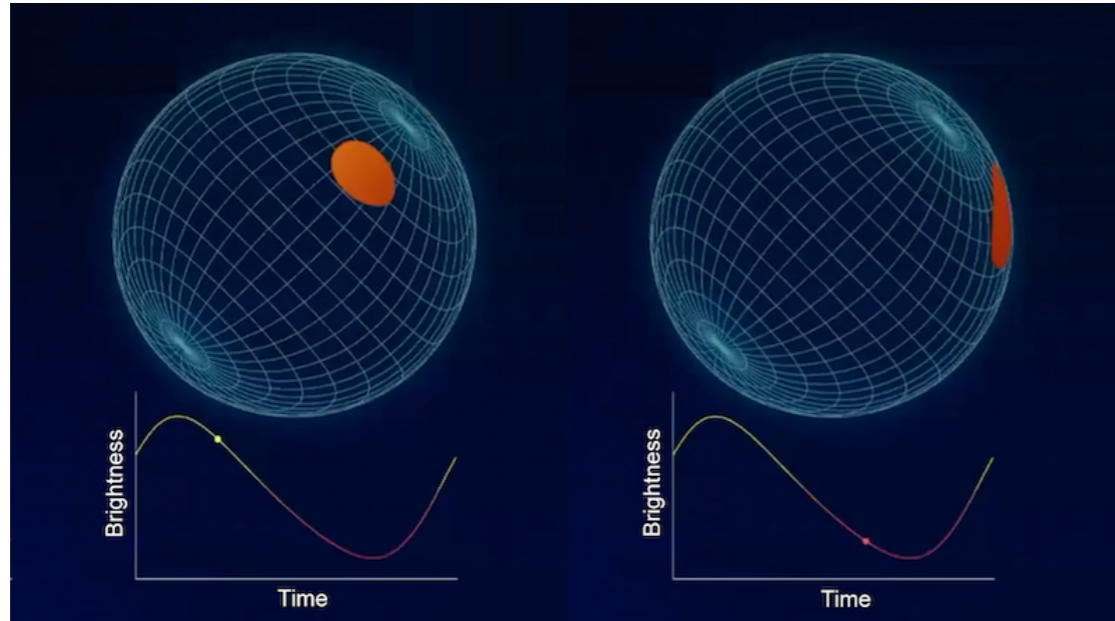


Alford, Han, and Prakash, Phys. Rev. D 88, 083013 (2013)

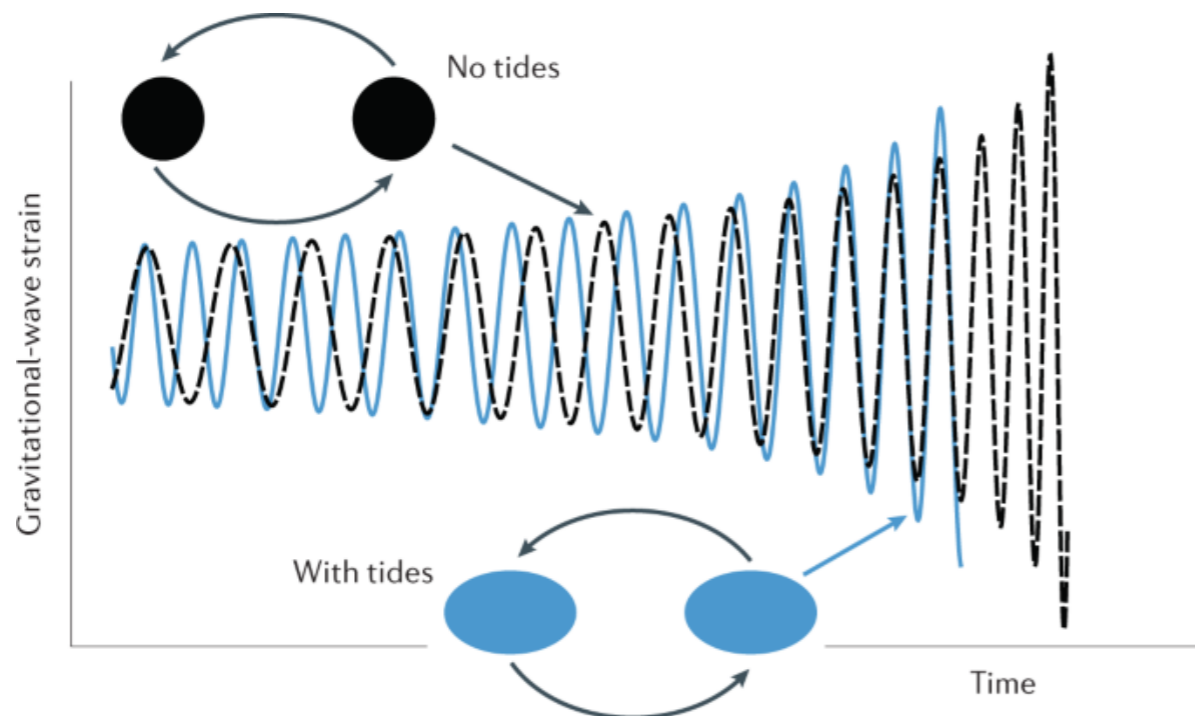


Constraint the Matter Phase

M-R relation example: NS/HS



(adiabatic) Tidal deformability



A question:

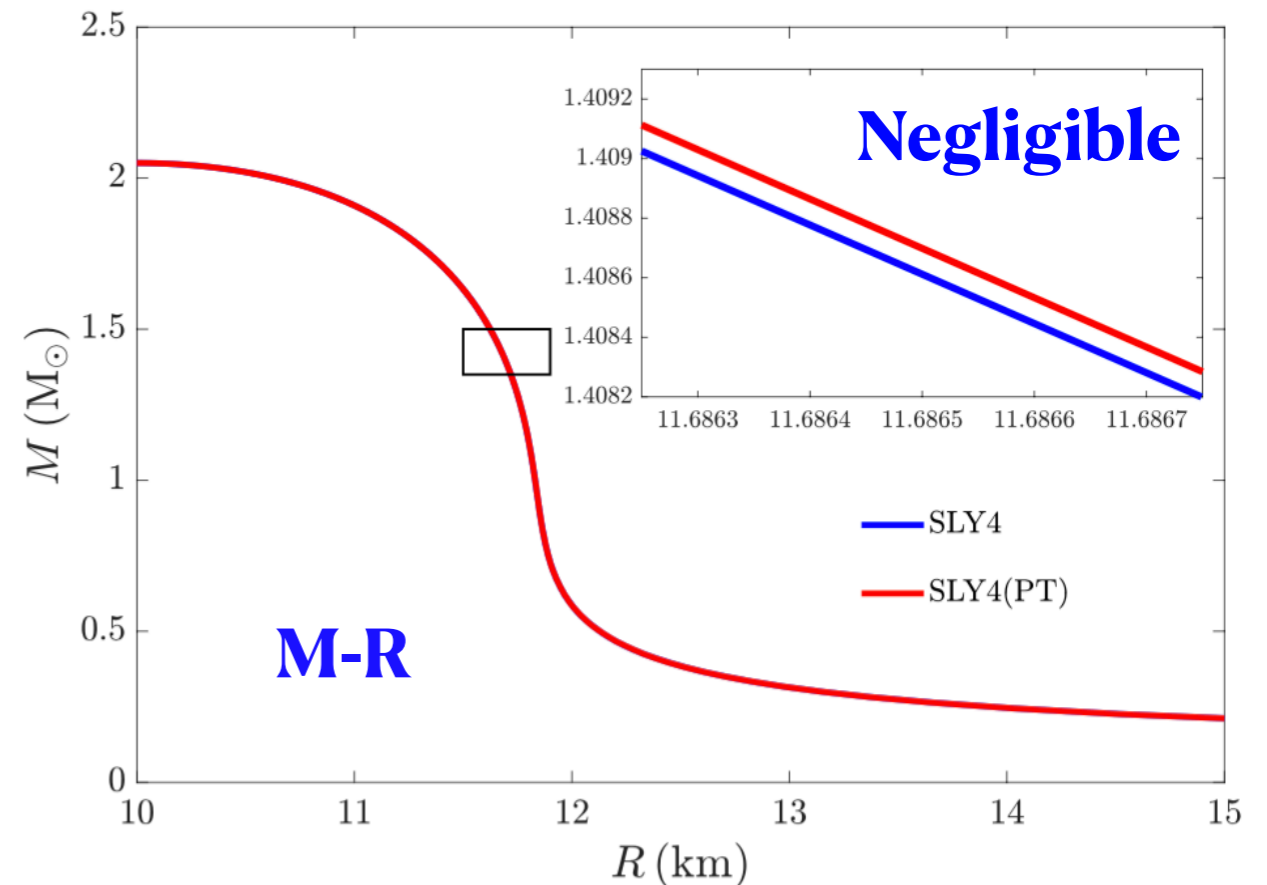
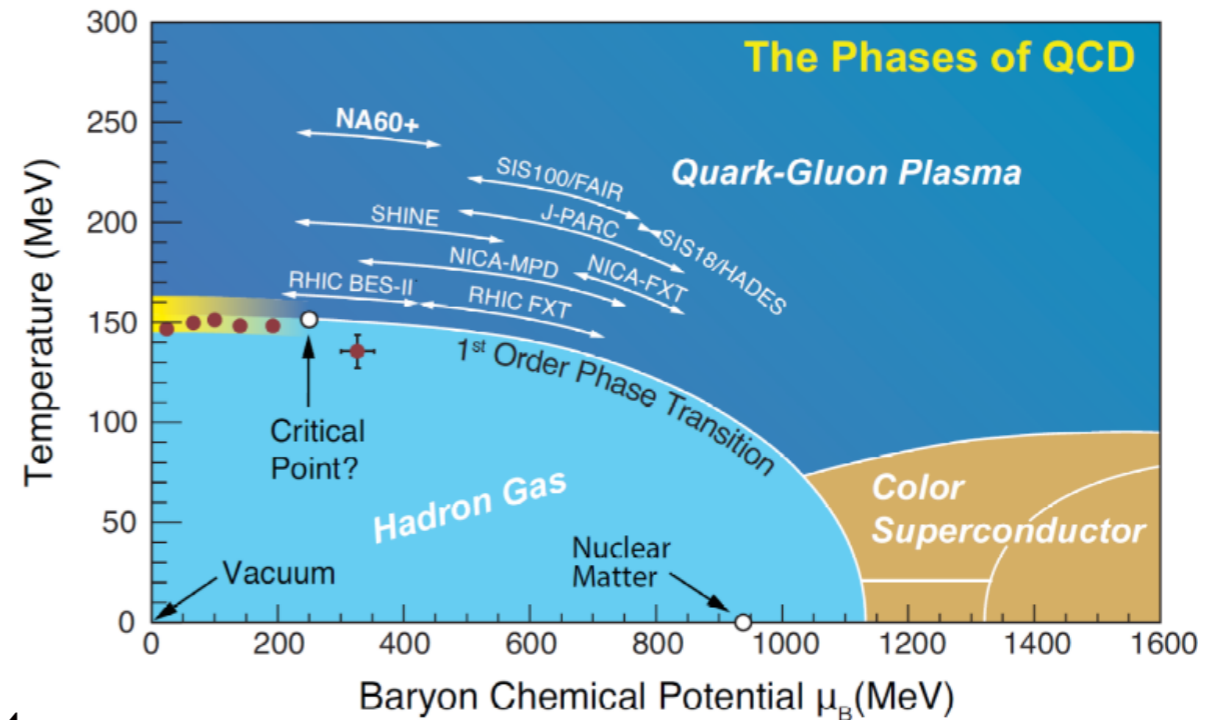
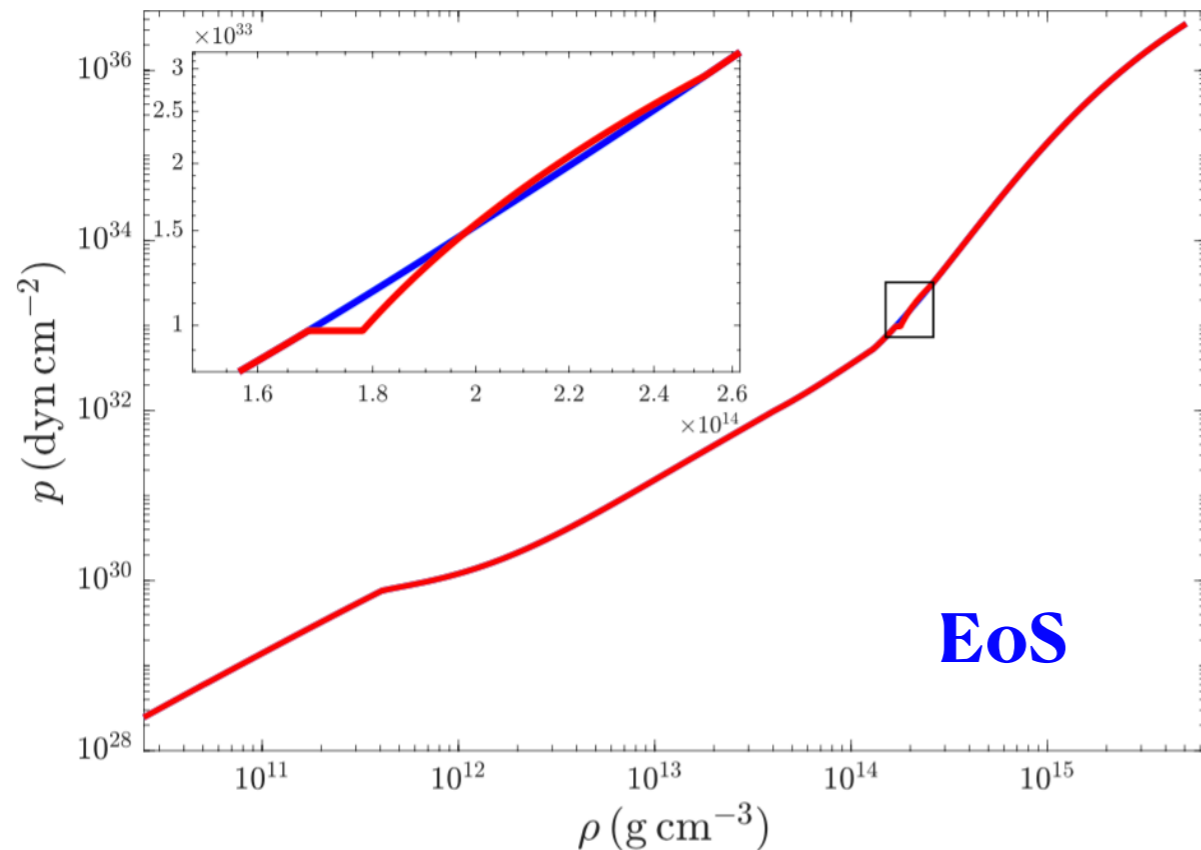
**Resolve detailed
Structure of EoS?**

Detailed structure of EoS

Possible “weak
1st order transition”

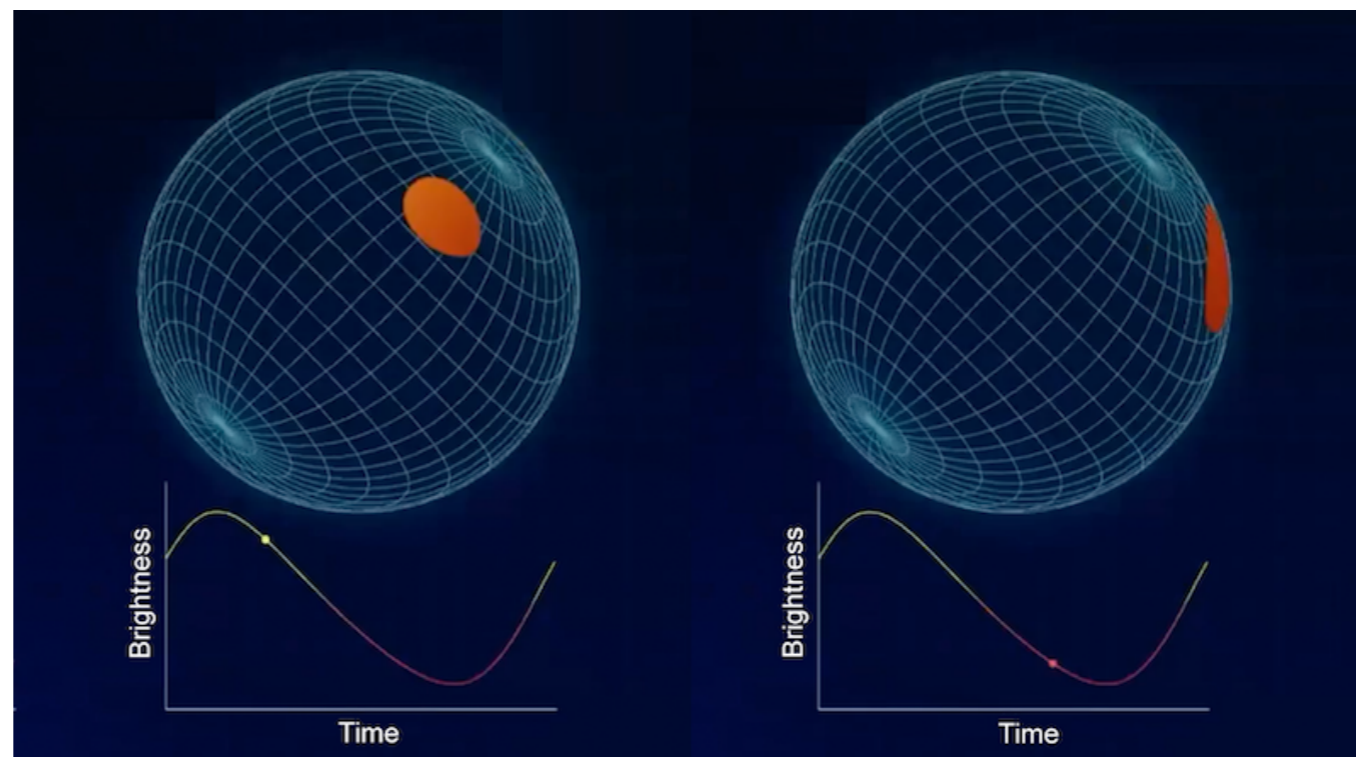
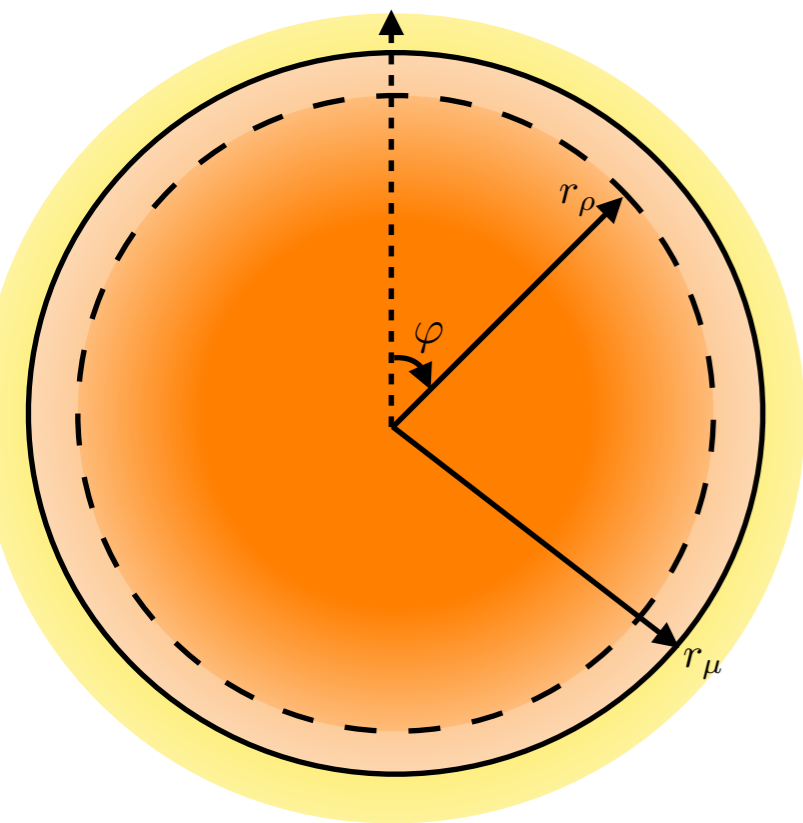
Emergence of new
baryonic state?

Construct a weak 1st PT on the SLy4



Probing weak phase transitions?

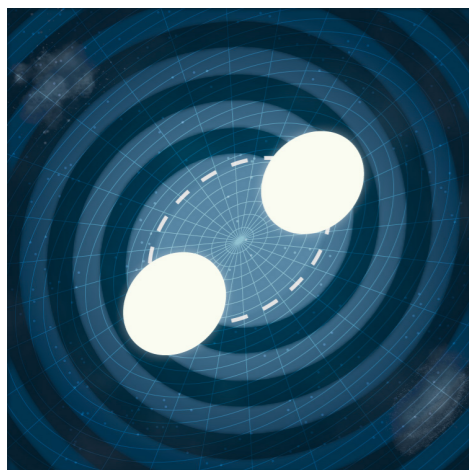
Density discontinuity effect on the M-R



Minor!

Density discontinuity effect on the tidal deformability

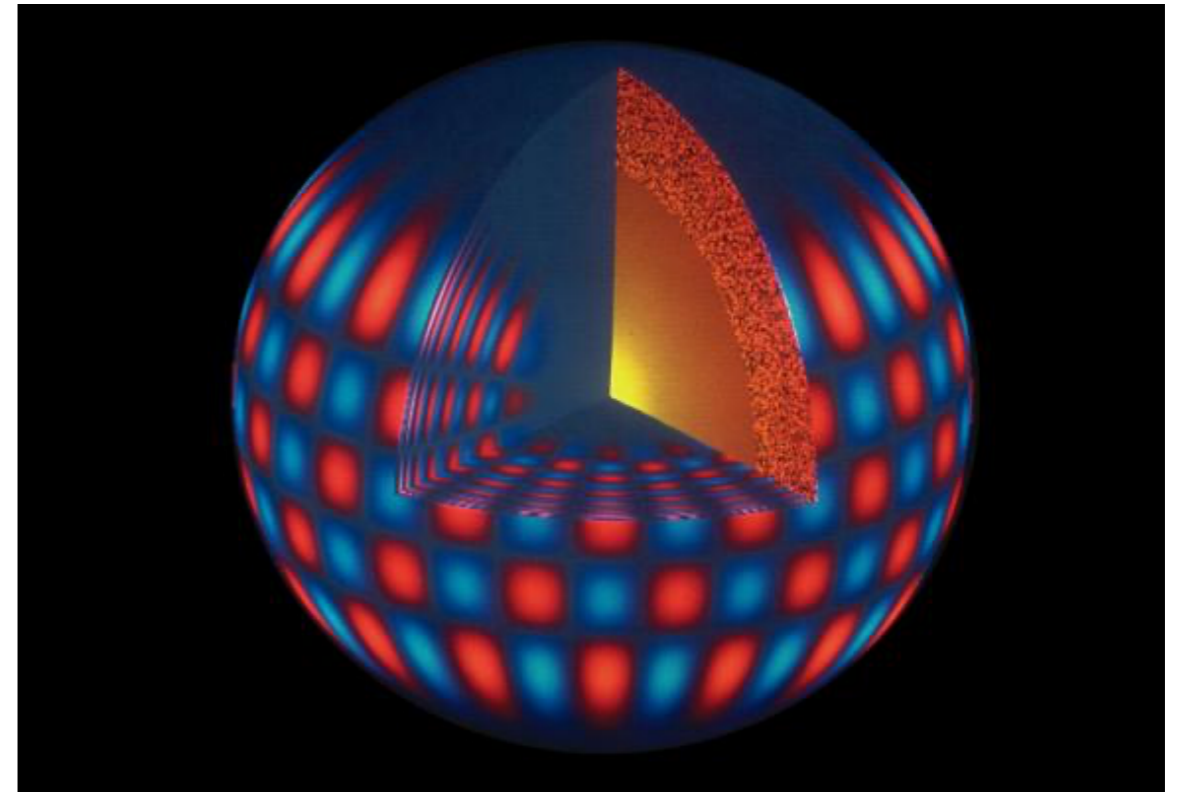
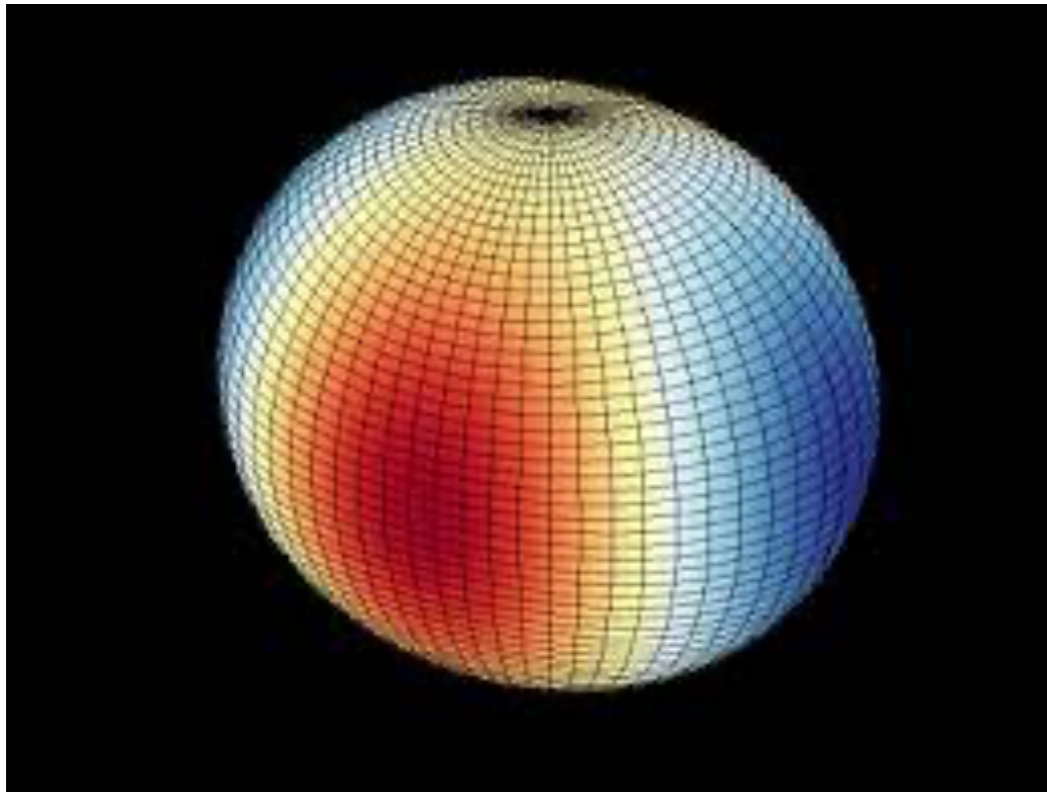
Minor!



EoS	SKI6	RS	SLY4	APR4	DD2	DDME2	TW	DD-LZ1
Λ	488	597	299	248	682	712	406	722
Λ_{PT}	496	651	303	260	714	738	424	755

Only dynamical tide helps!

Neutron star seismology

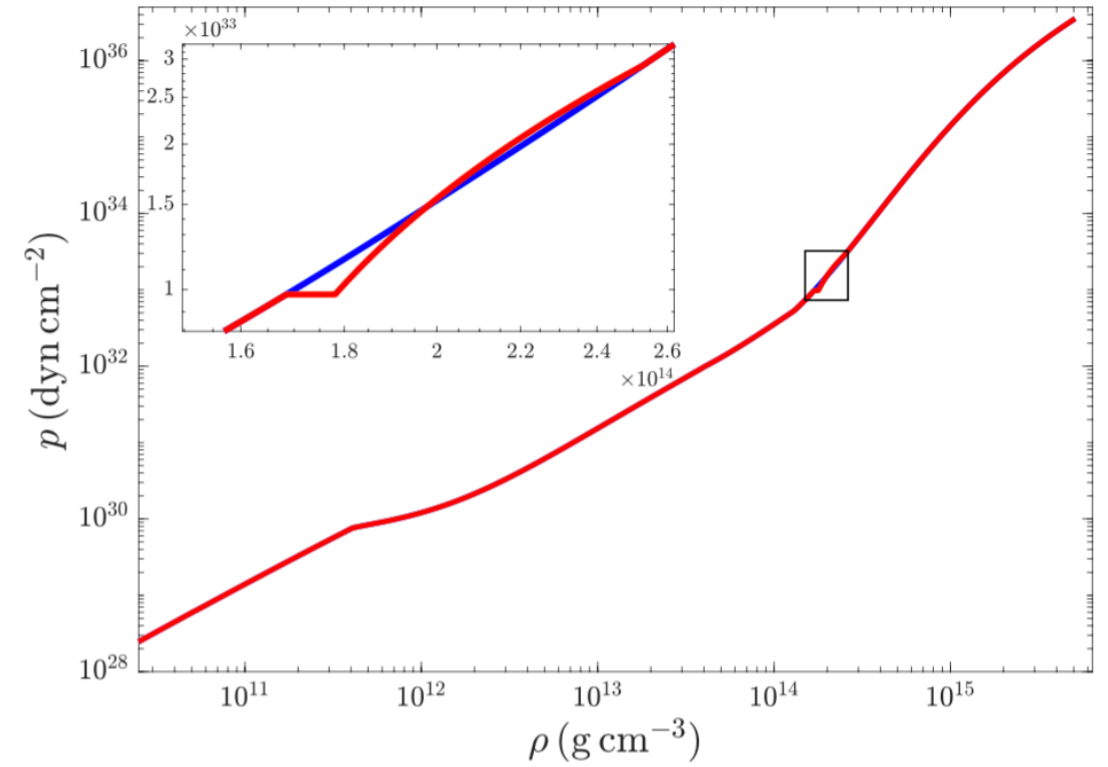
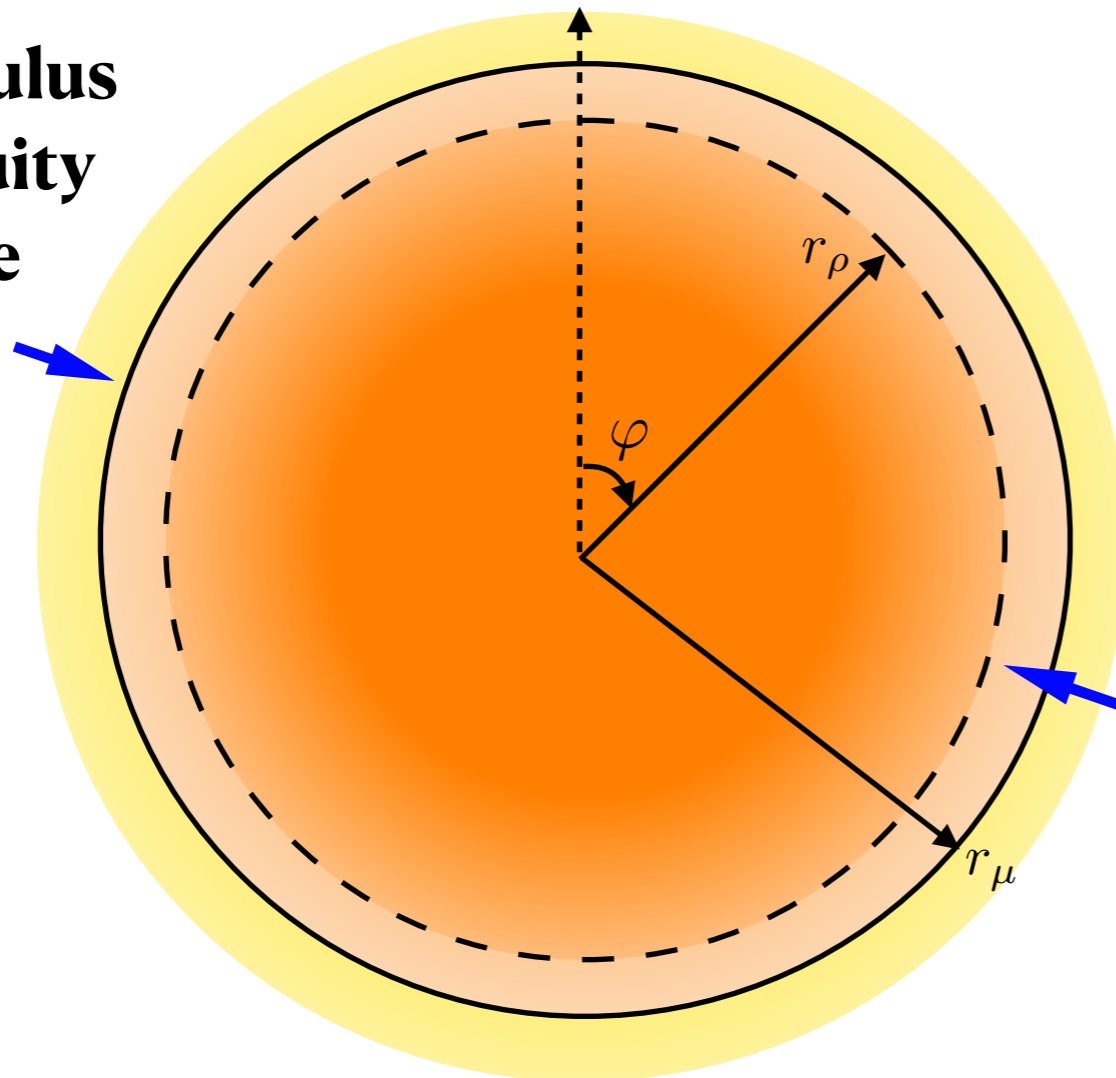


- **These oscillation modes are affected by EoS, e.g.** $\Gamma = \frac{d \ln P}{d \ln \rho}$
- **Can be excited by tidal motion, and NS coalescence**
- **Can couple to the orbital motion, and affect GW radiation**

Neutron star Interfacial mode

The Model

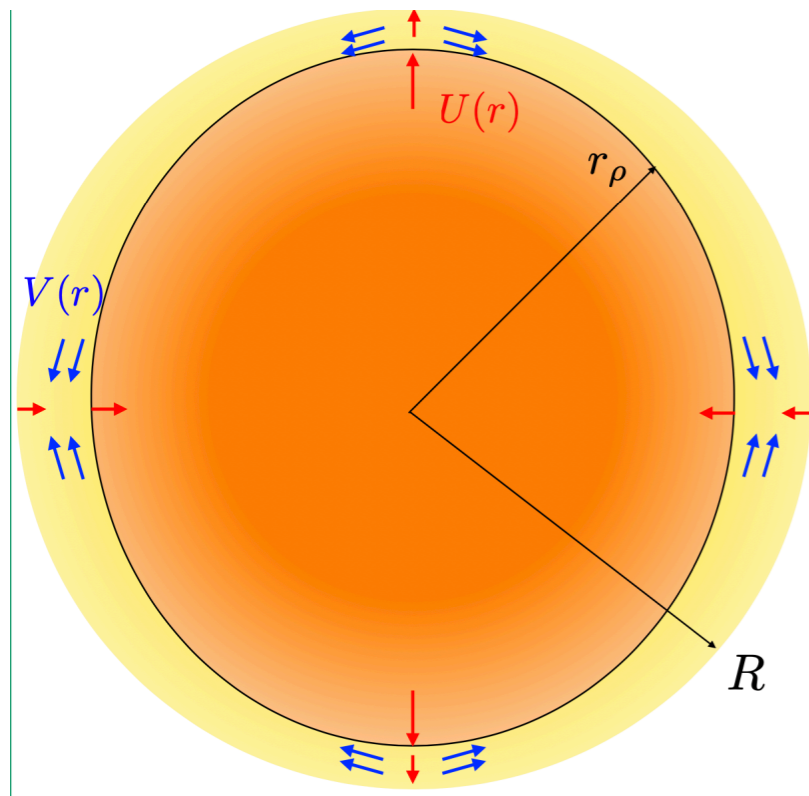
Shear Modulus
Discontinuity
Interface



Target

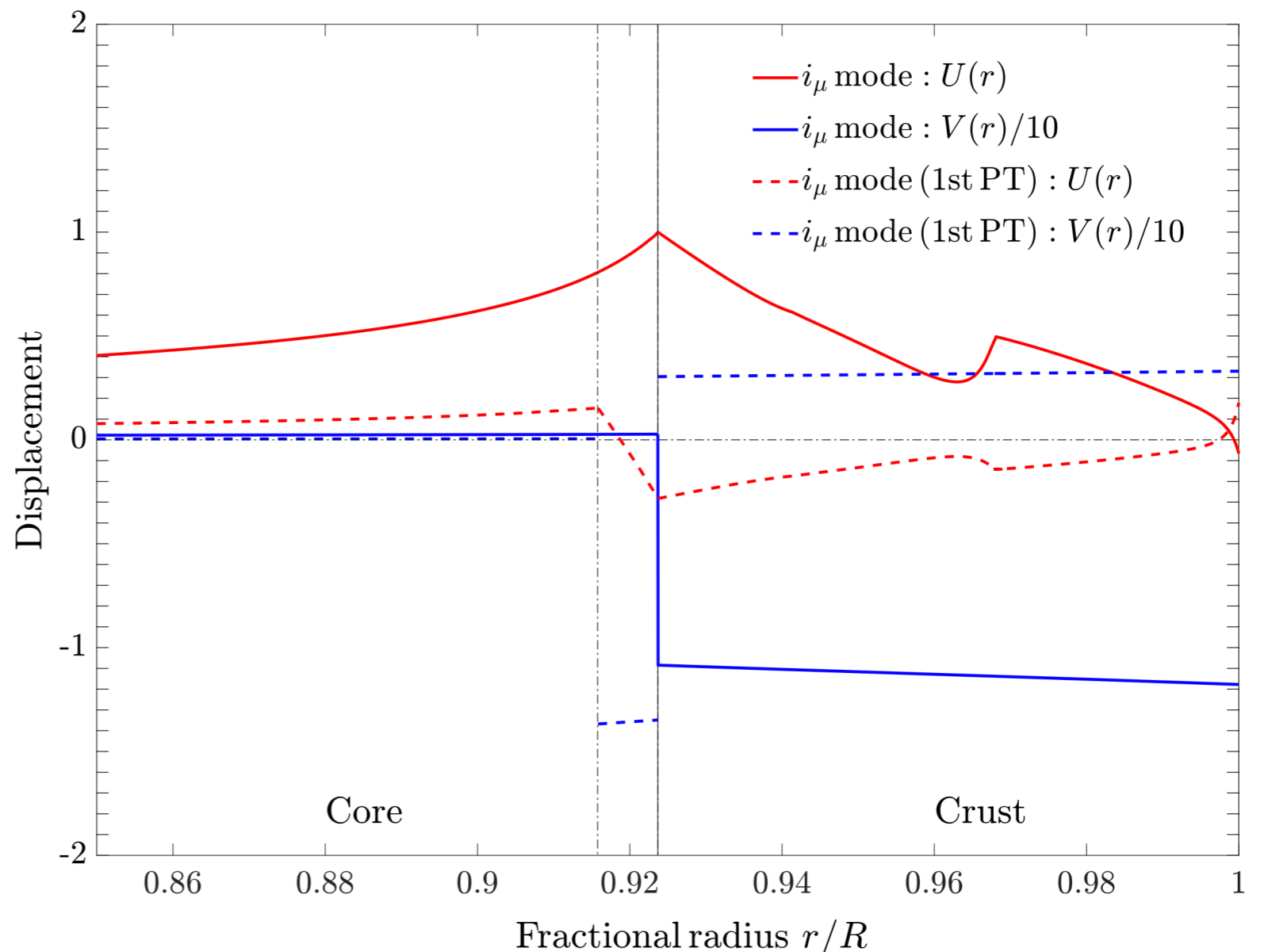
Density
Discontinuity
Interface

Neutron star Interfacial mode- i_μ



Wave function of the shear interfacial mode

Solid line: Pure shear interfacial mode

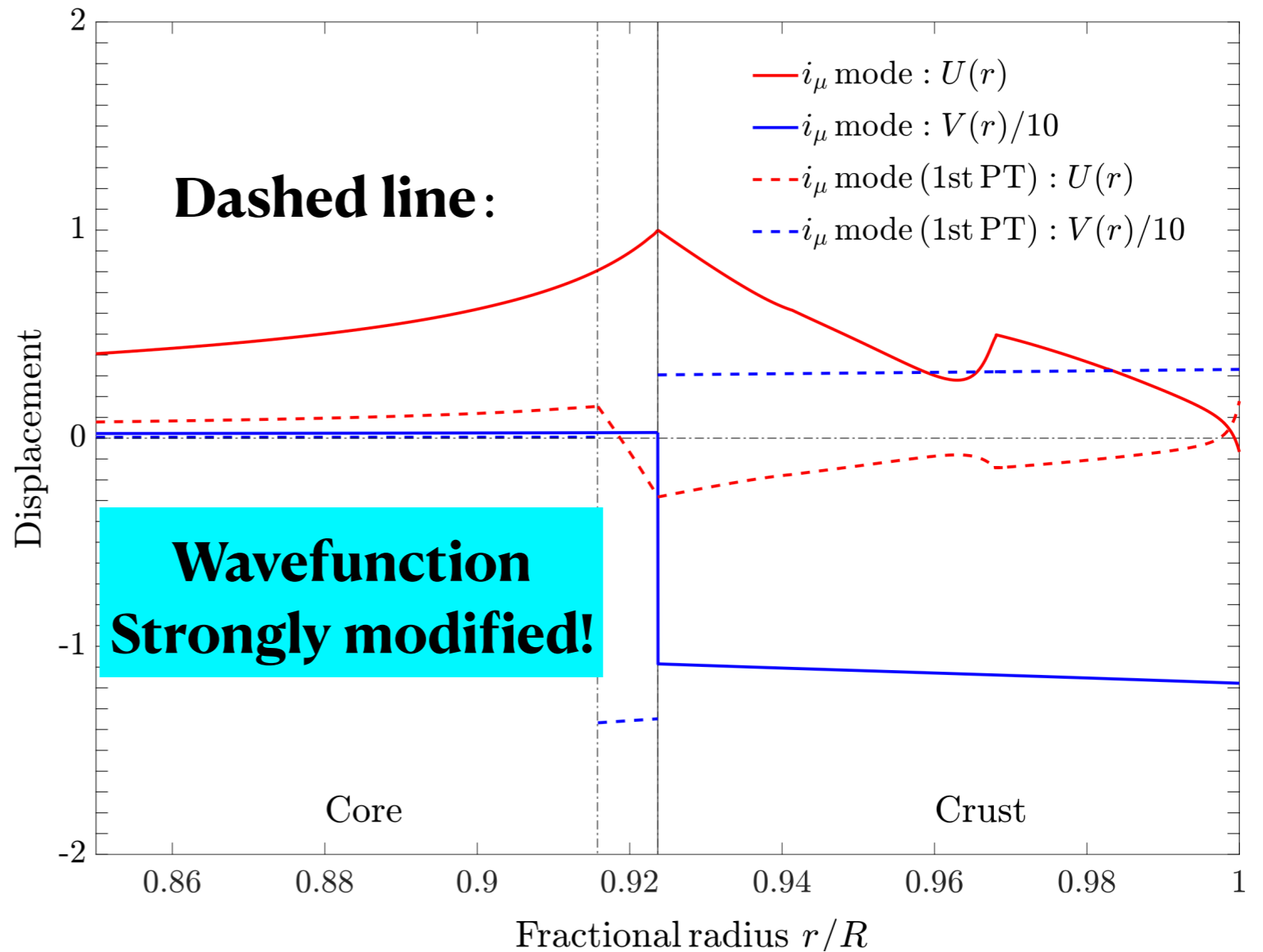
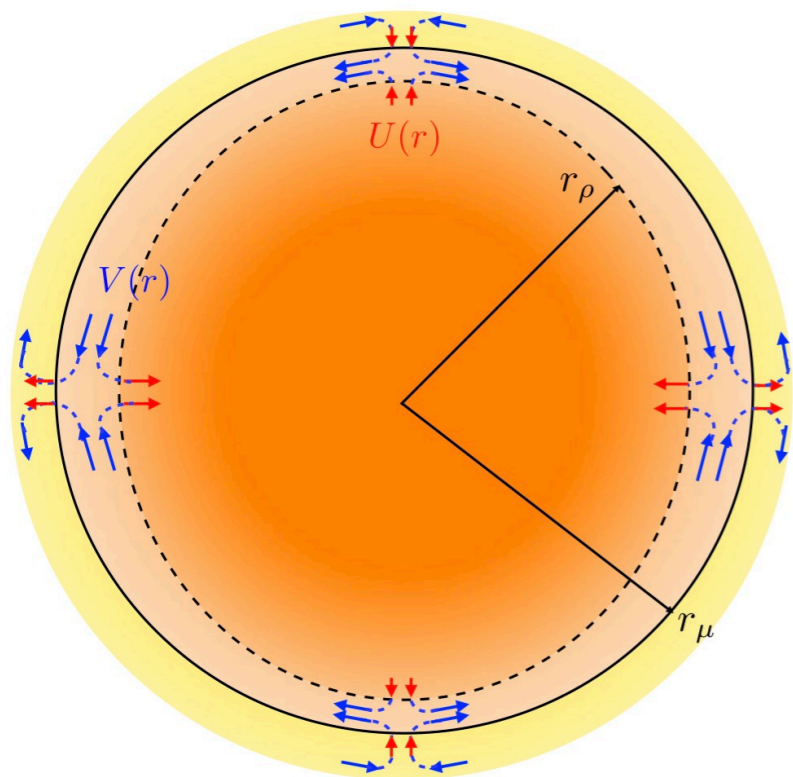
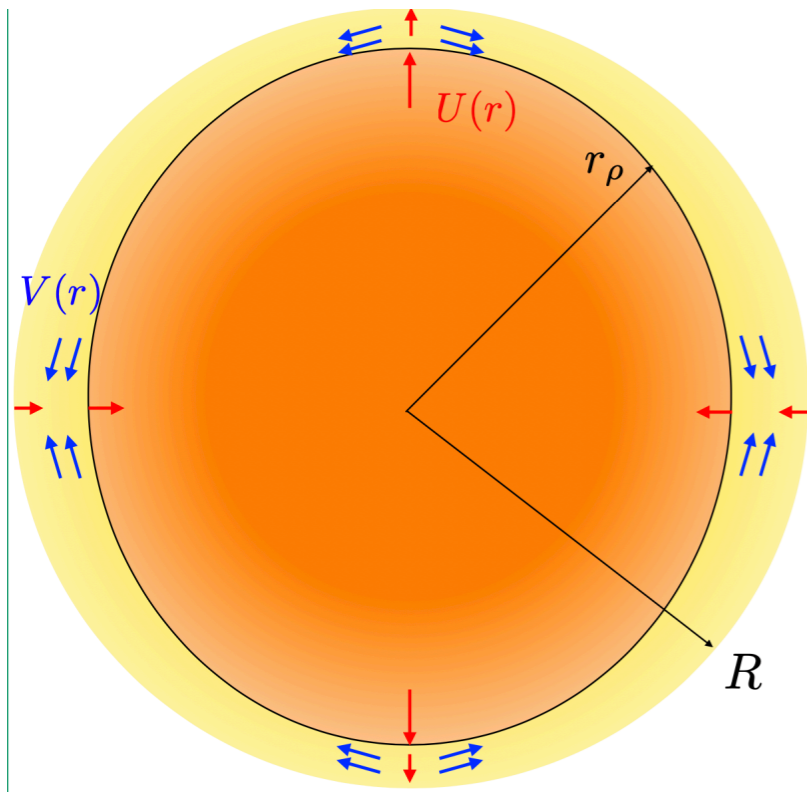


- **Low frequency**
- **Strong interfacial Excitations**
- **Large orbital coupling**

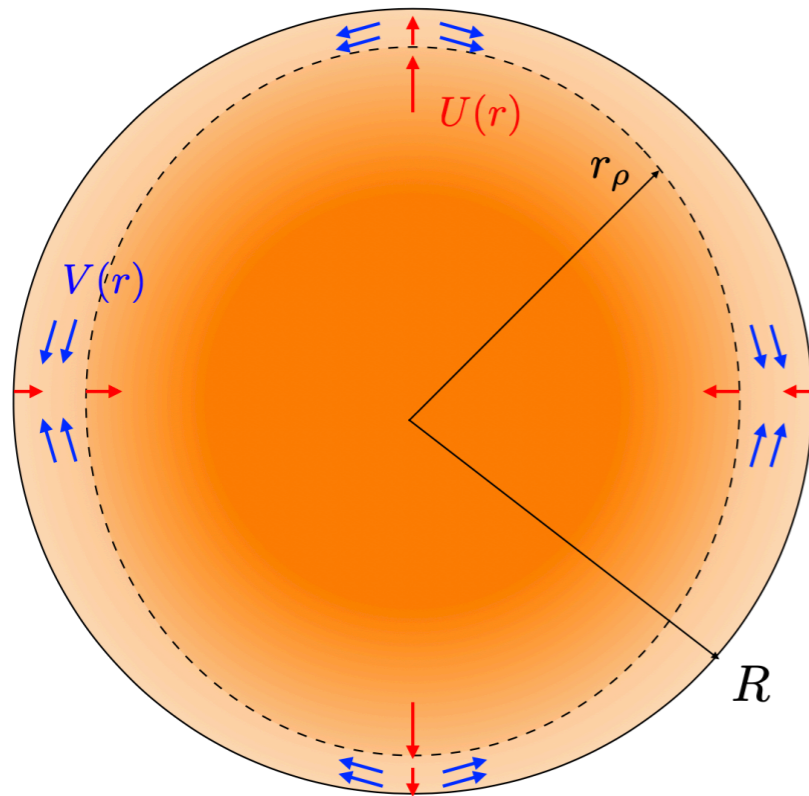
Neutron star Interfacial mode- i_μ

Wave function of the shear interfacial mode—Introduce PT at r_ρ

Domin: Free-slipping fluid $r_\rho < r < r_\mu$



Neutron star Interfacial mode- i_ρ

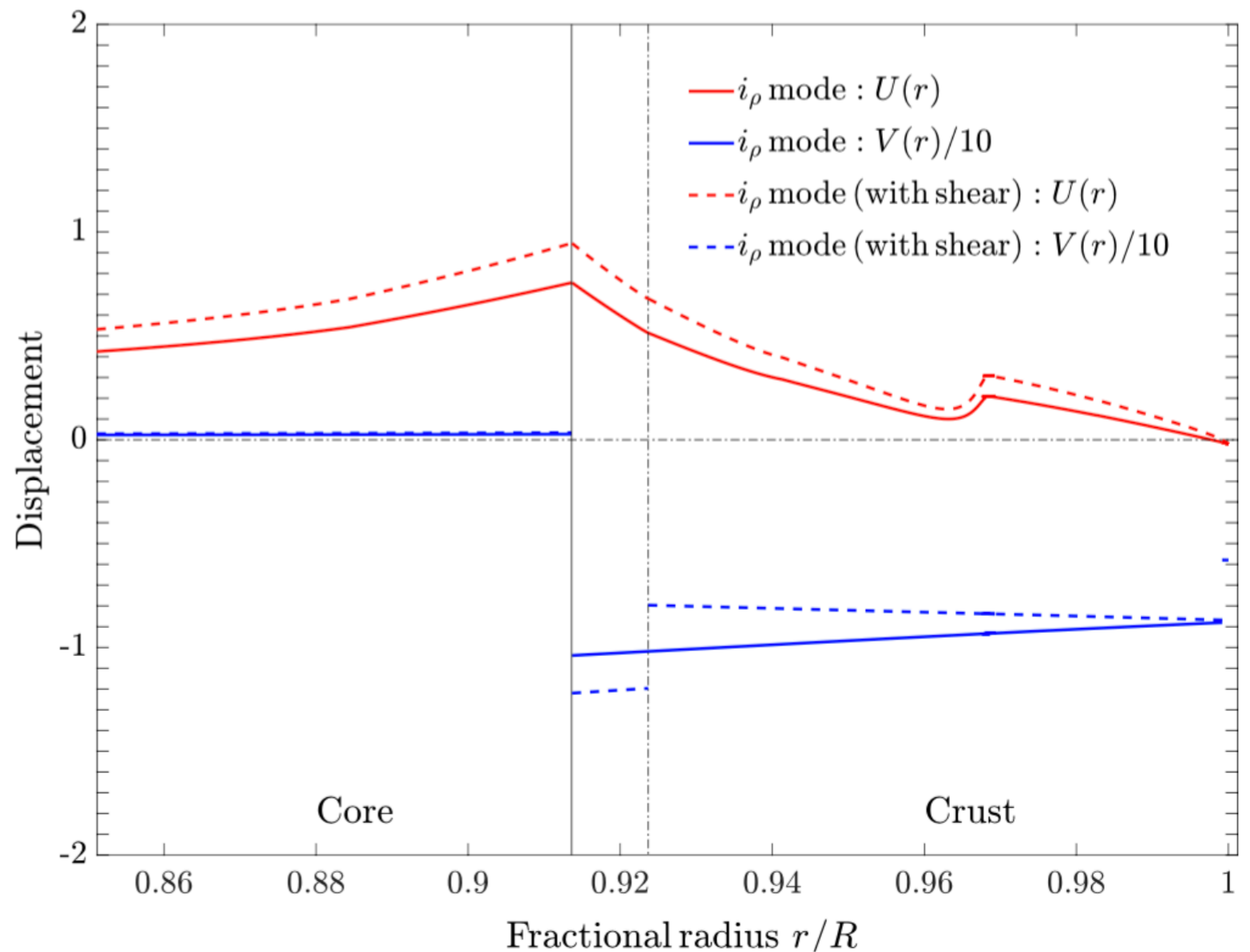


Wave function of the density interfacial mode

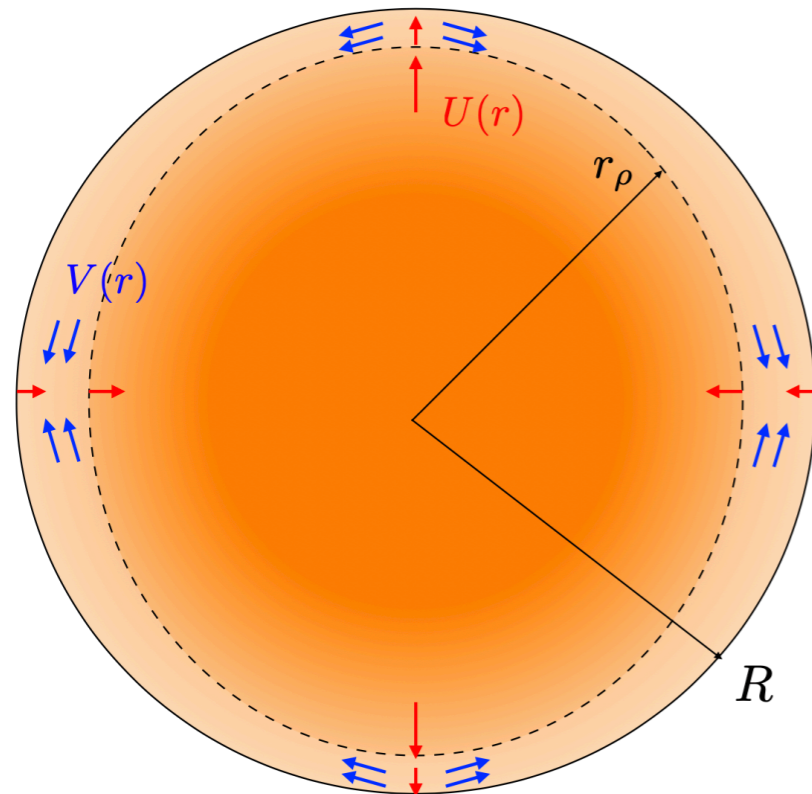
Domin: Core fluid $r > r_\rho$

Similar to Kelvin-Helmholtz mode

- Higher frequency
- Strong interfacial Excitations
- Large orbital coupling

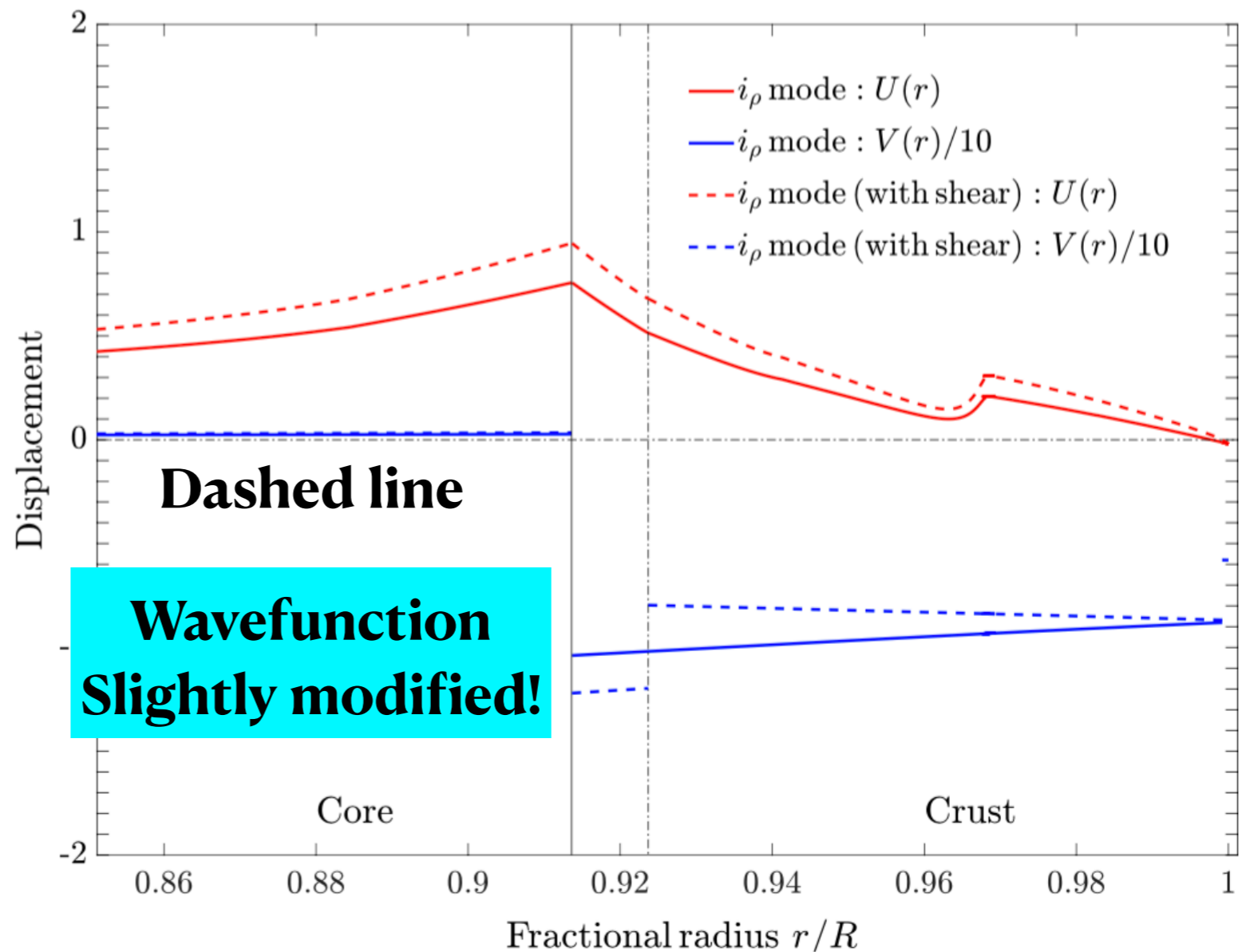
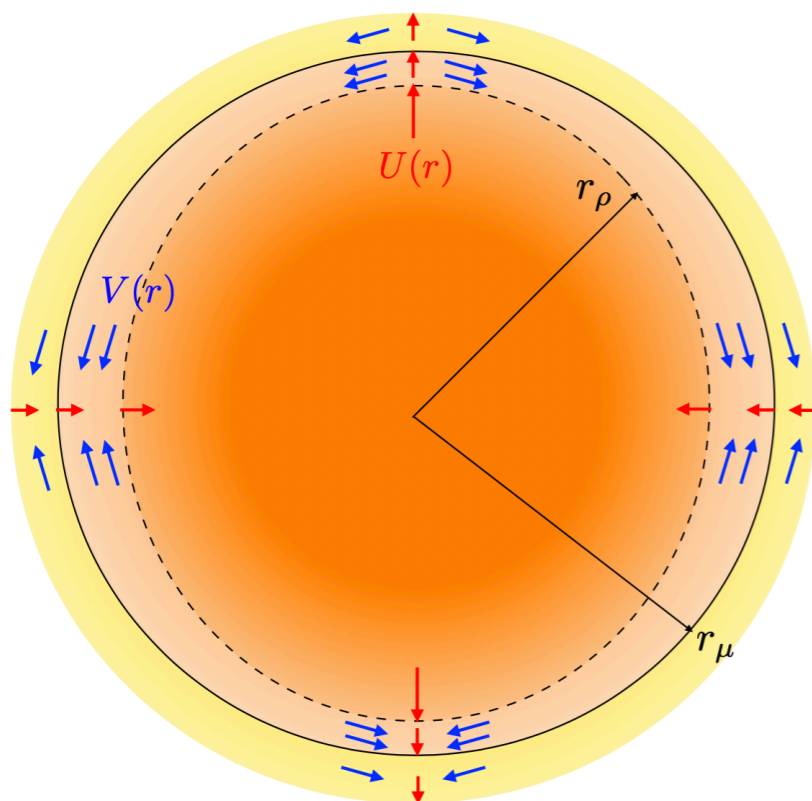


Neutron star Interfacial mode- i_ρ



Wave function of the density interfacial mode

Domin: Core fluid $r > r_\rho$



Mode mixing of $i_\mu - i_\rho$

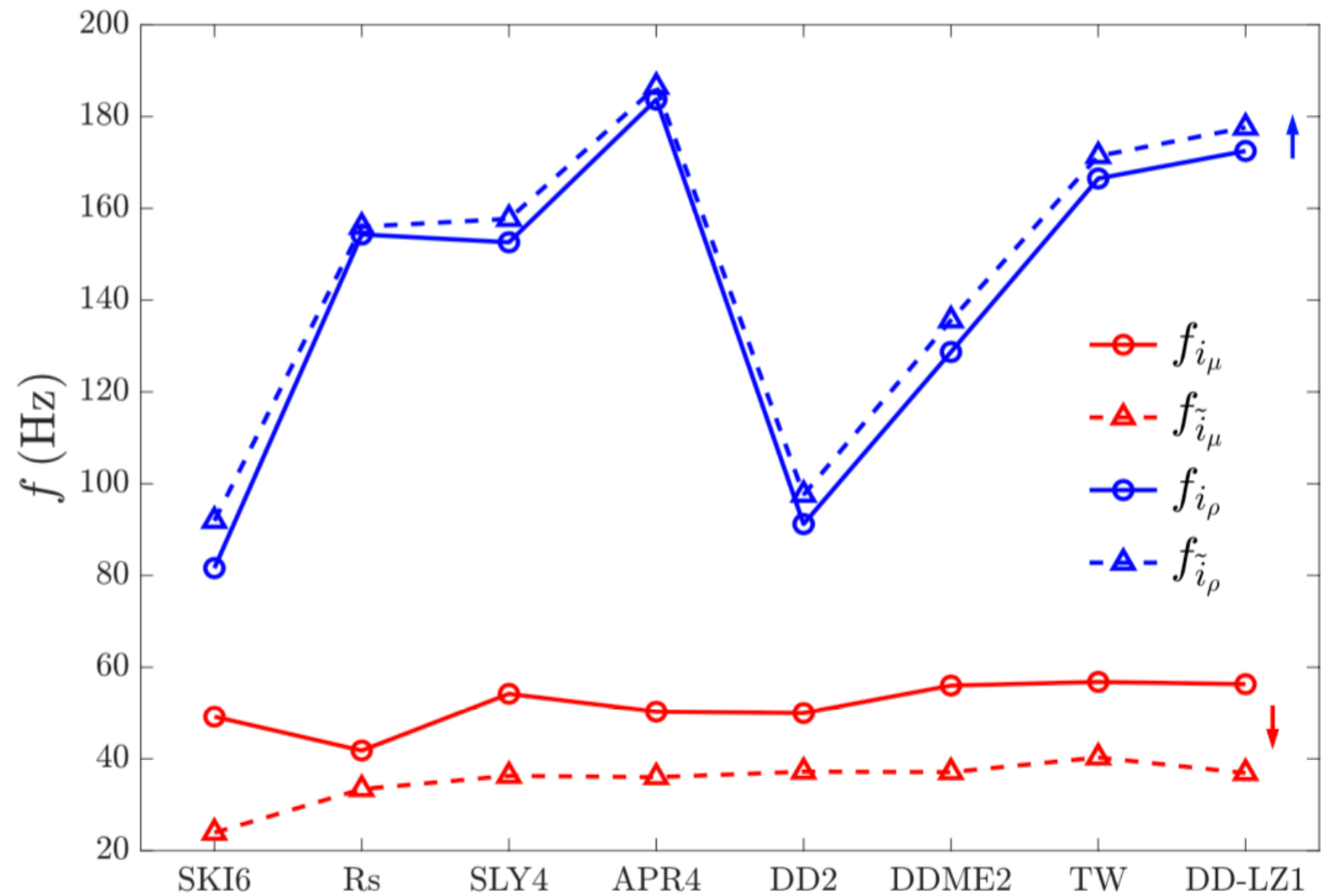
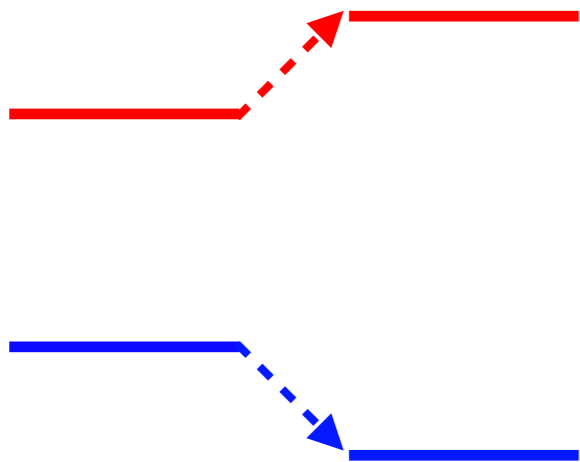
Hamiltonian

$$\mathcal{H} = \begin{pmatrix} \xi_\mu & \xi_\rho \end{pmatrix} \begin{pmatrix} \omega_\mu & \epsilon \\ \epsilon & \omega_\rho \end{pmatrix} \begin{pmatrix} \xi_\mu \\ \xi_\rho \end{pmatrix}$$

**Significant Overlap
Between**

$$i_\mu - i_\rho$$

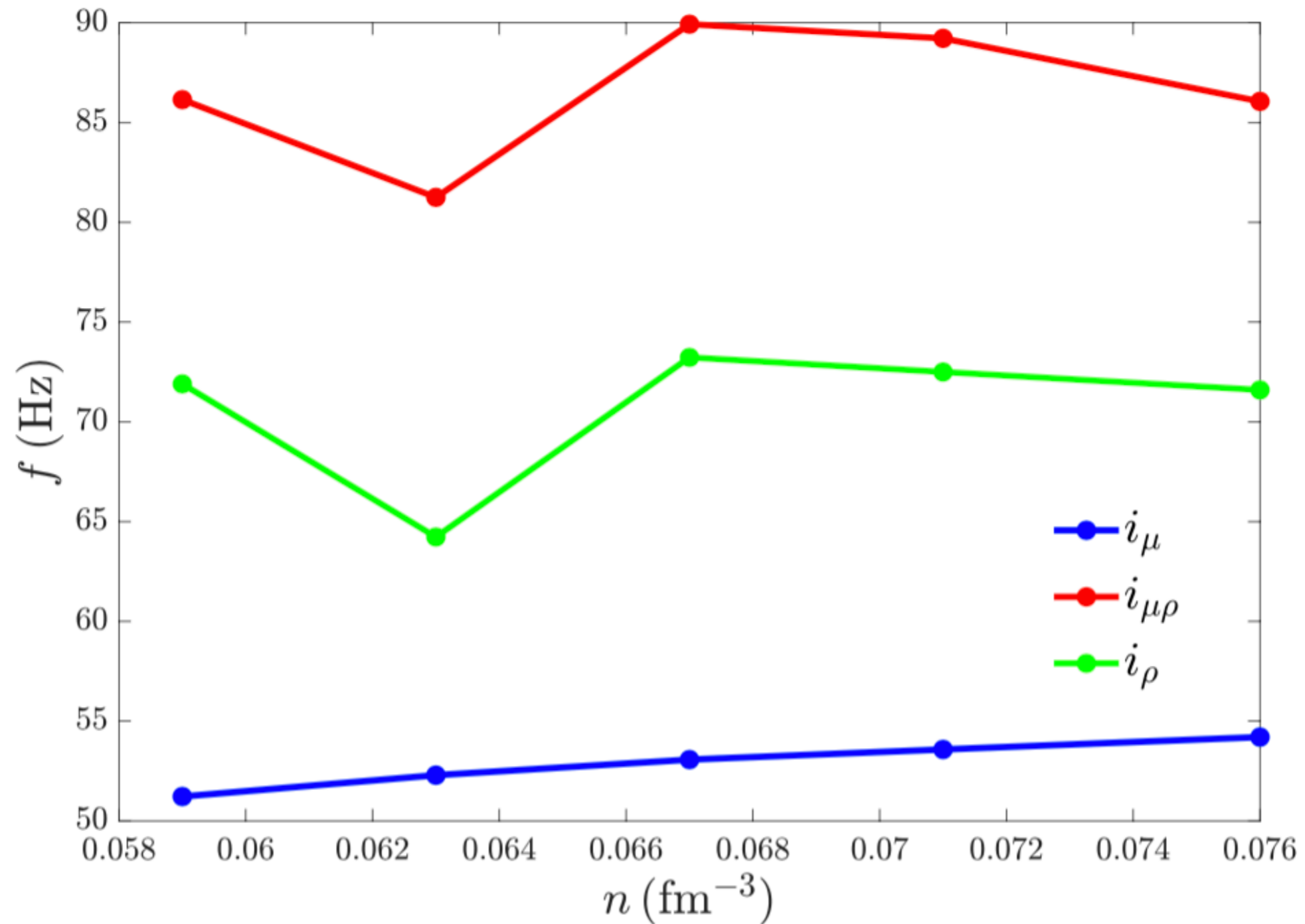
Avoid crossing



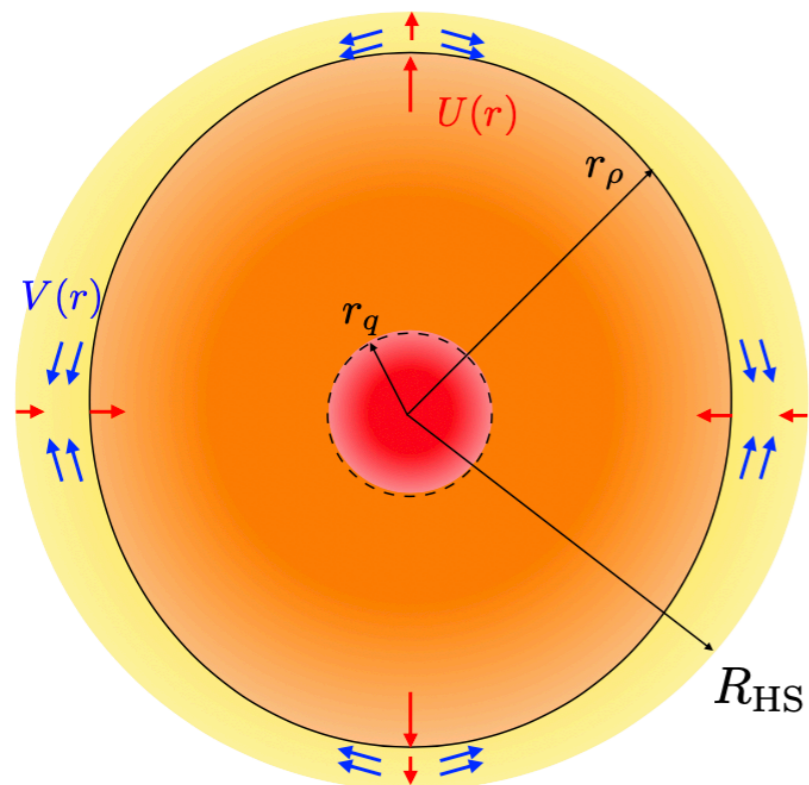
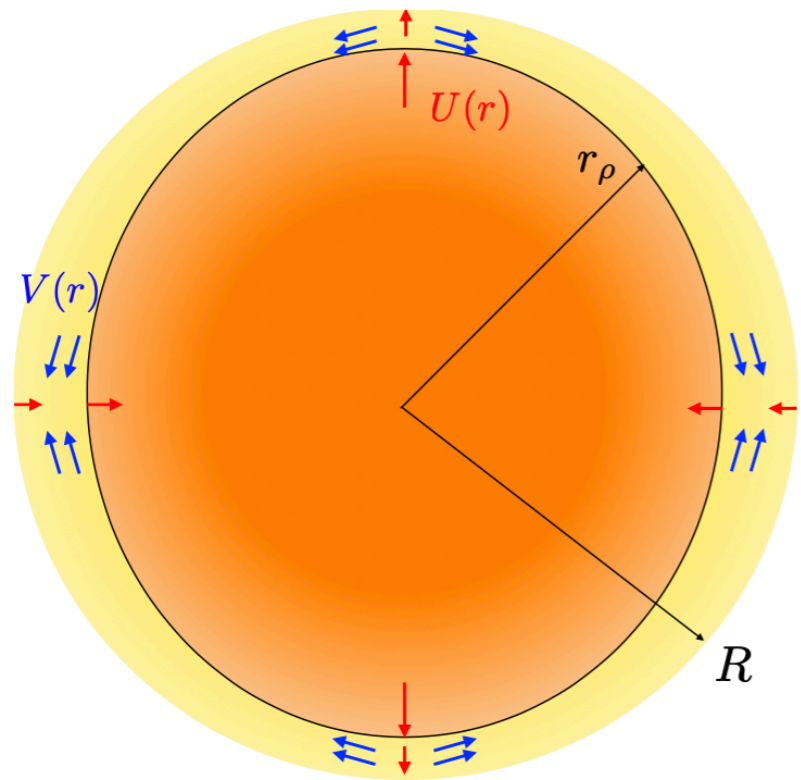
$$\tilde{\omega}_\rho = \frac{1}{2} [\omega_\mu + \omega_\rho + \sqrt{(\omega_\mu - \omega_\rho)^2 + 4\epsilon^2}] > \omega_\rho,$$

$$\tilde{\omega}_\mu = \frac{1}{2} [\omega_\mu + \omega_\rho - \sqrt{(\omega_\mu - \omega_\rho)^2 + 4\epsilon^2}] < \omega_\mu,$$

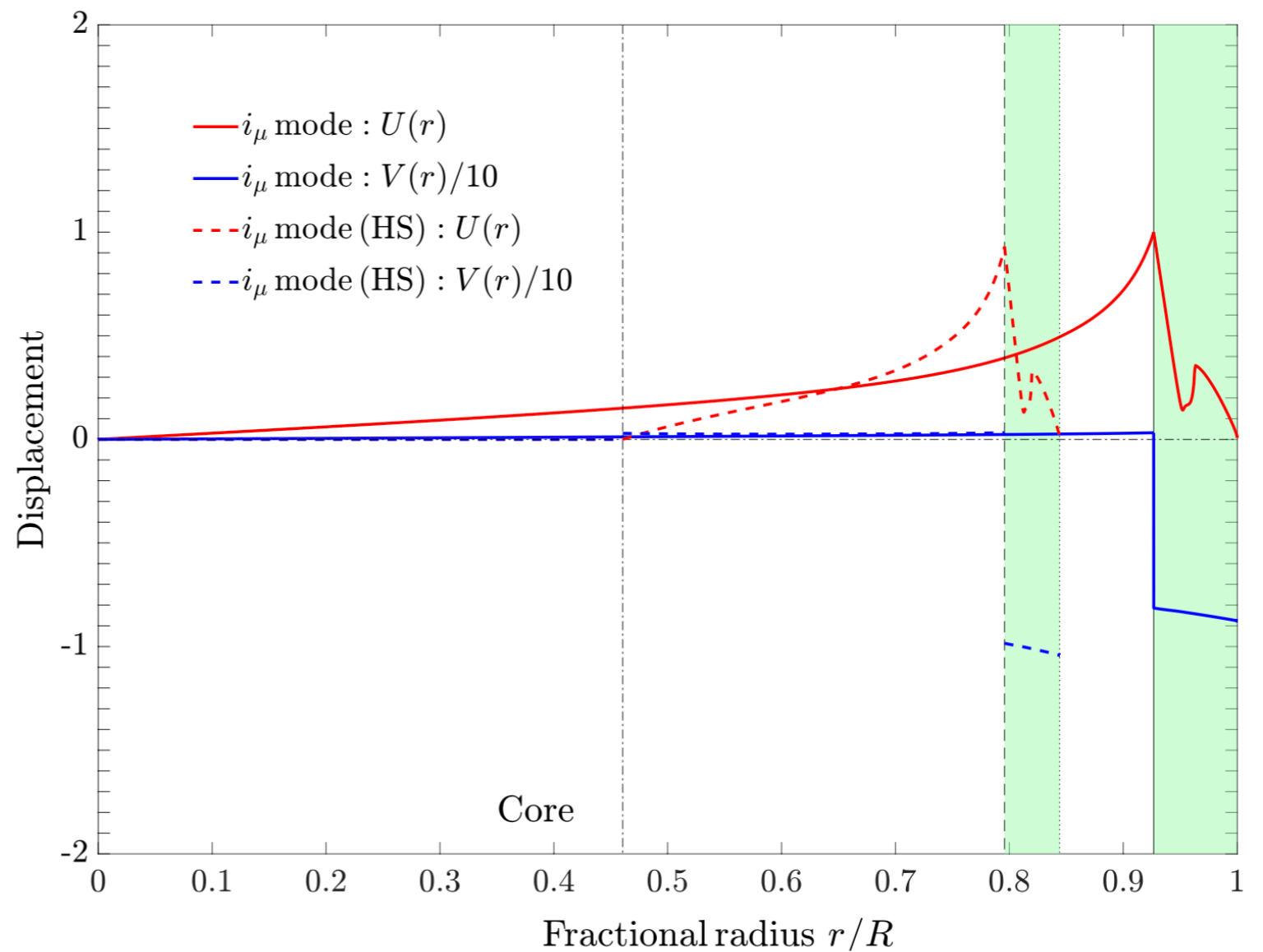
Extremal case: coincide interfaces



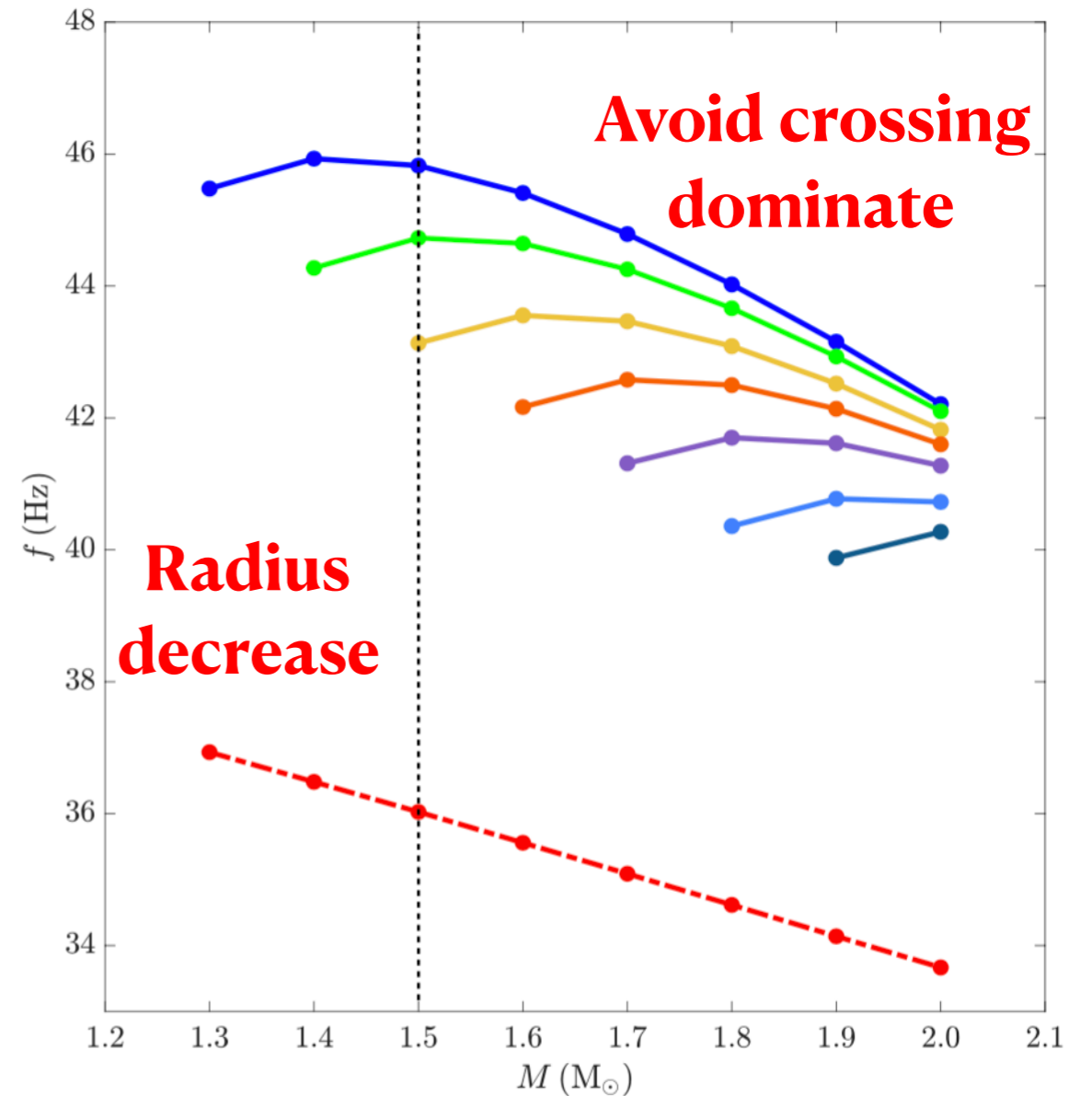
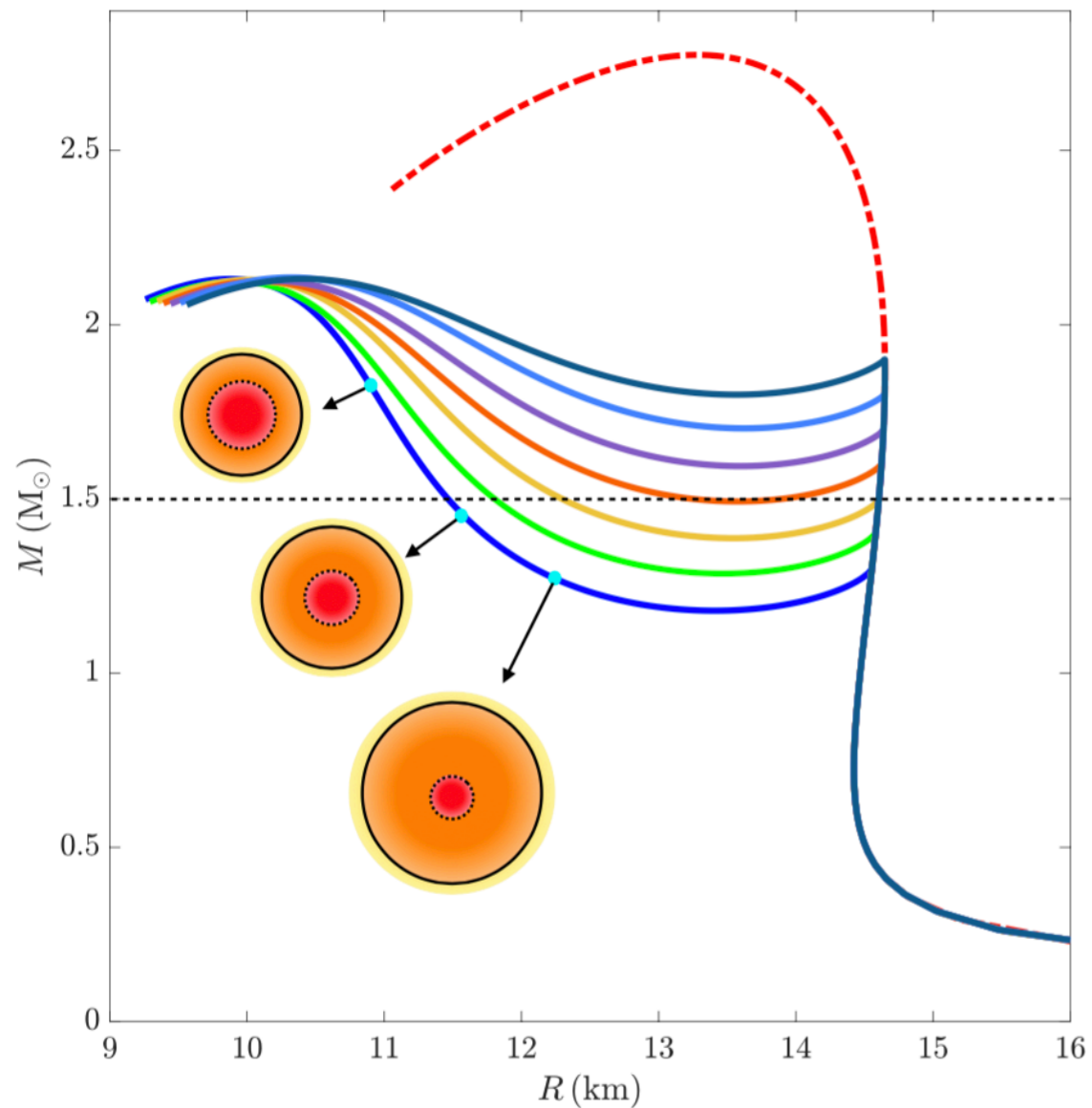
Quark-core affected Neutron star Interfacial mode- i_μ



Wave function of the shear interfacial mode



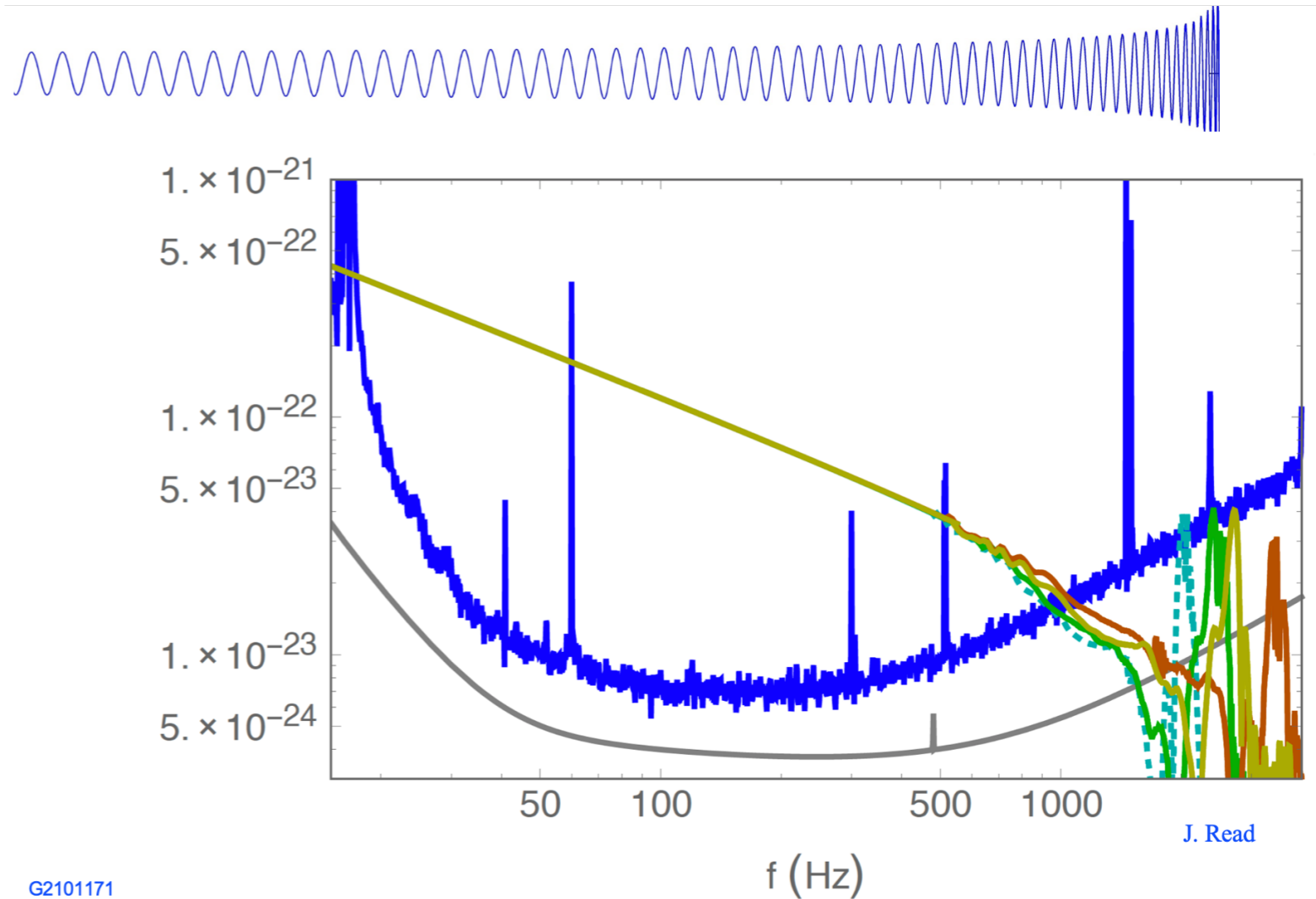
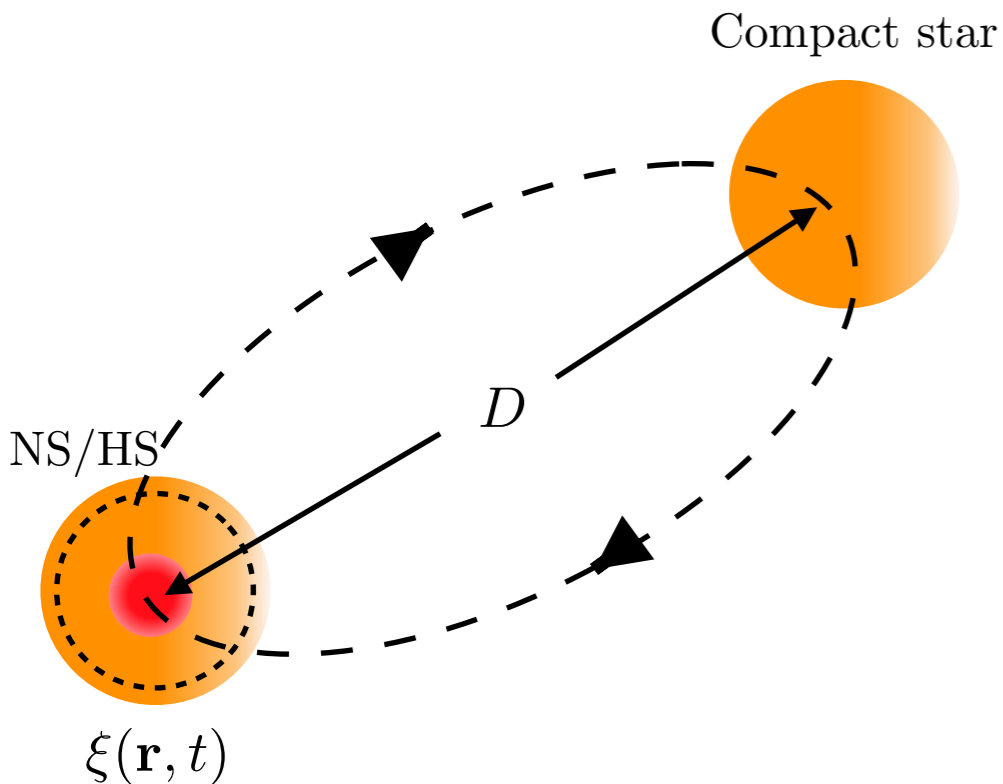
Quark-core affected Neutron star Interfacial mode- i_{μ}



Trend of the interfacial mode frequency affected by Quark core

See Miao's talk for the i-mode related to the hadron-quark interface

Binary NS system and Gravitational waves



- Carry information of EoS
Masses, Tidal deformability

G2101171

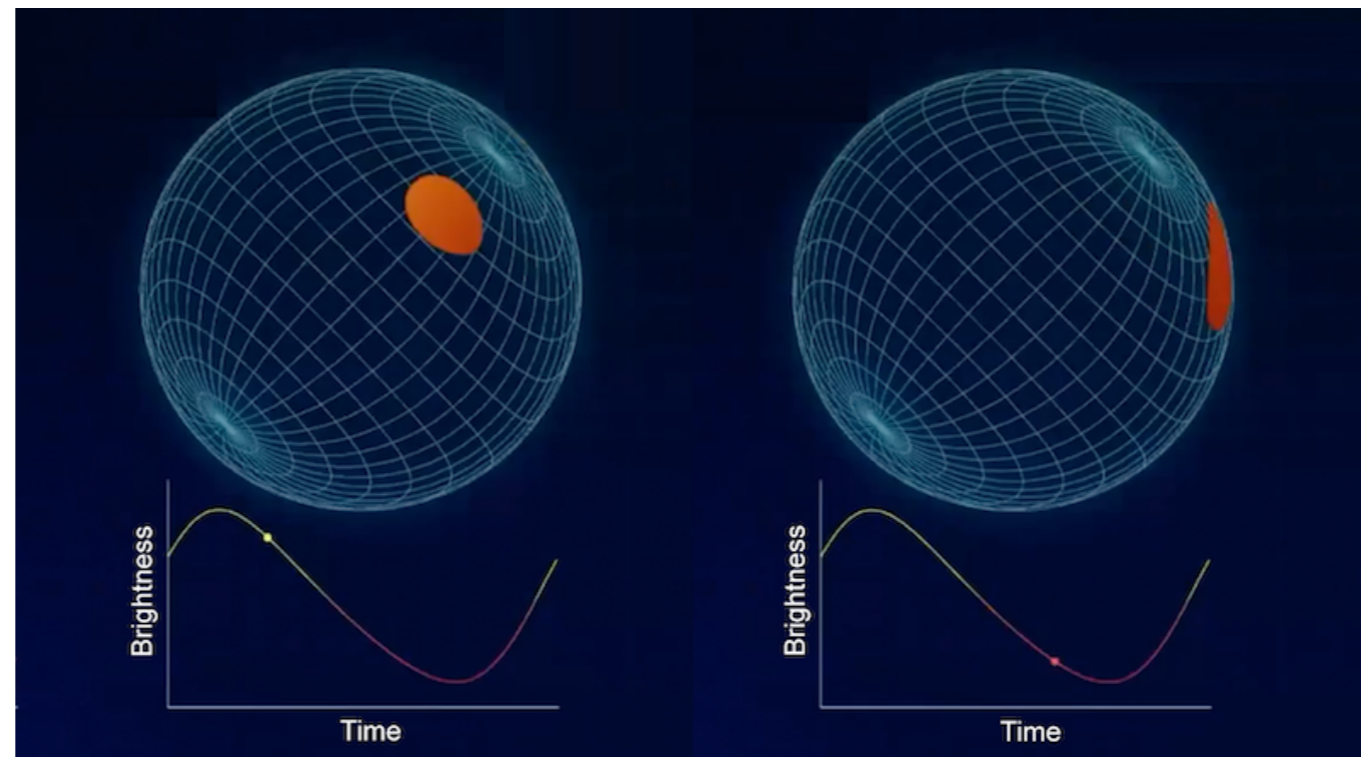
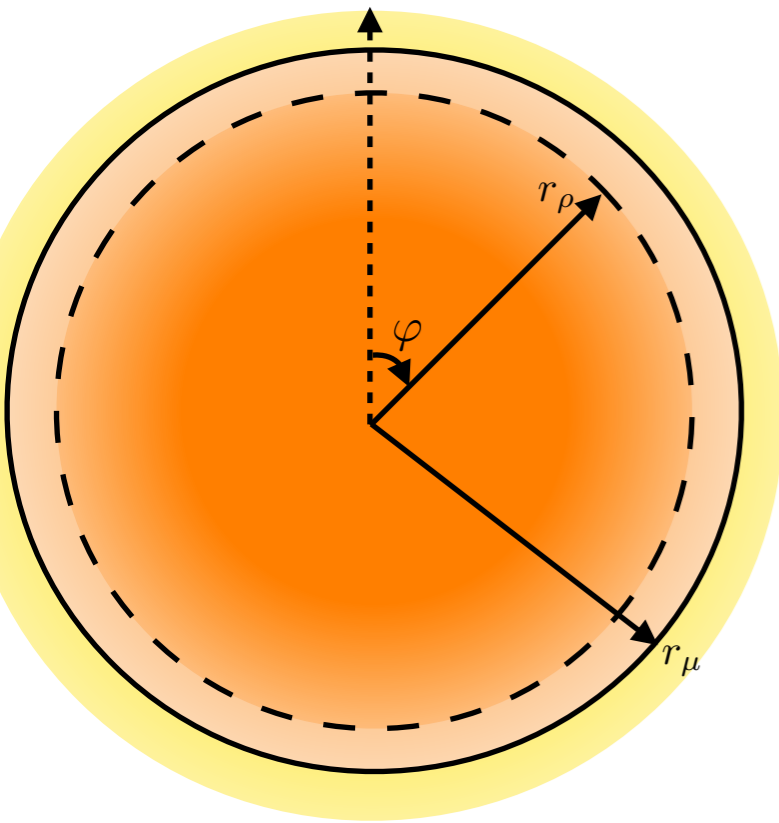
- Orbital-internal mode coupling

Overlap between orbital and internal mode

$$\ddot{a}_m + \omega_\alpha^2 a_m + \gamma \dot{a}_m = \frac{GMW_{2m} Q_{2m}}{D^3(t)} e^{-im\Phi(t)}.$$

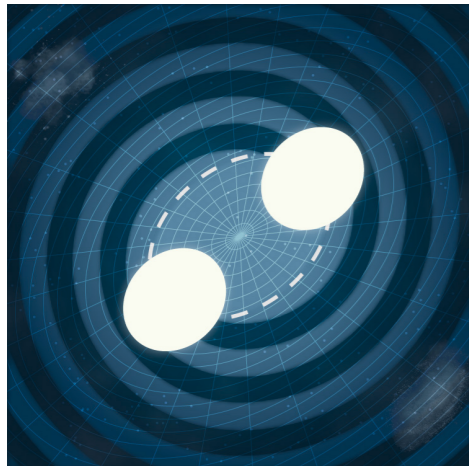
Binary NS system probing transitions?

Density discontinuity effect on the M-R



Minor!

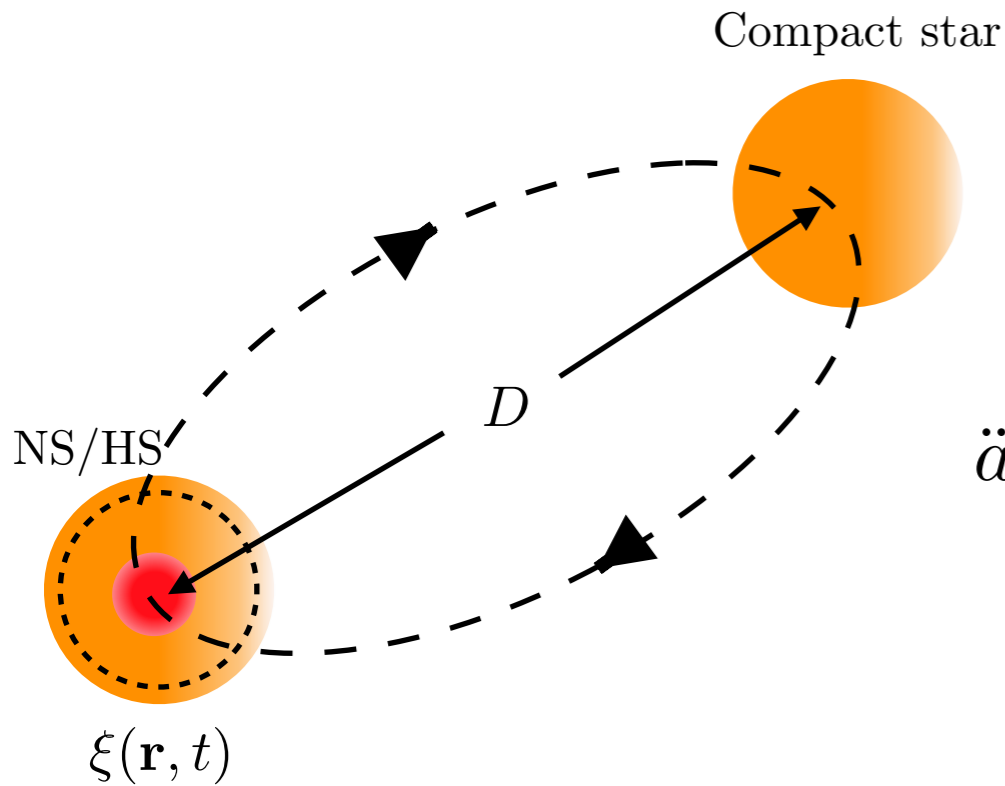
Density discontinuity effect on the tidal deformability



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Minor!

Binary NS system and Gravitational waves

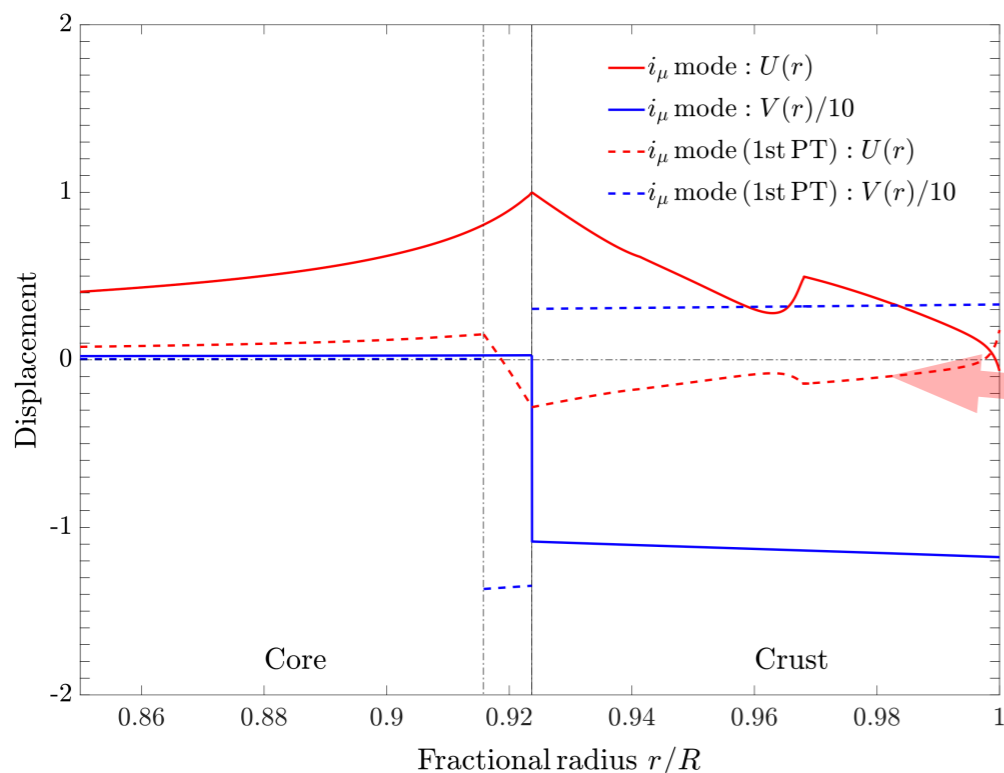


**Density discontinuity effect on
Orbital-internal mode coupling**

$$\ddot{a}_m + \omega_\alpha^2 a_m + \gamma \dot{a}_m = \frac{GMW_{2m}Q_{2m}}{D^3(t)} e^{-im\Phi(t)}.$$

**Overlap between orbital
and internal mode**

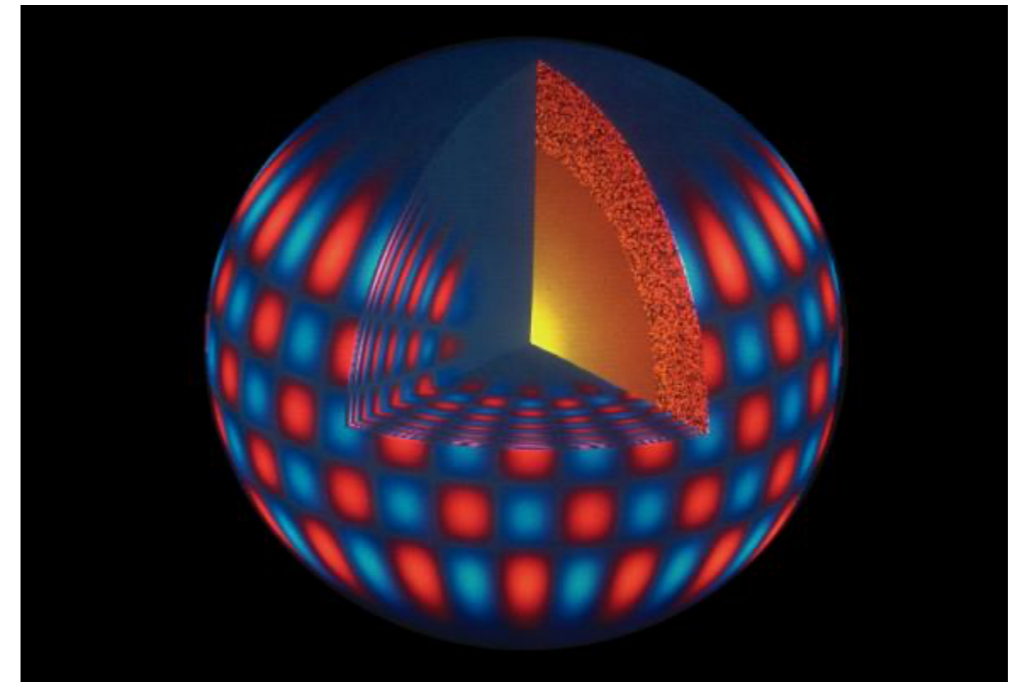
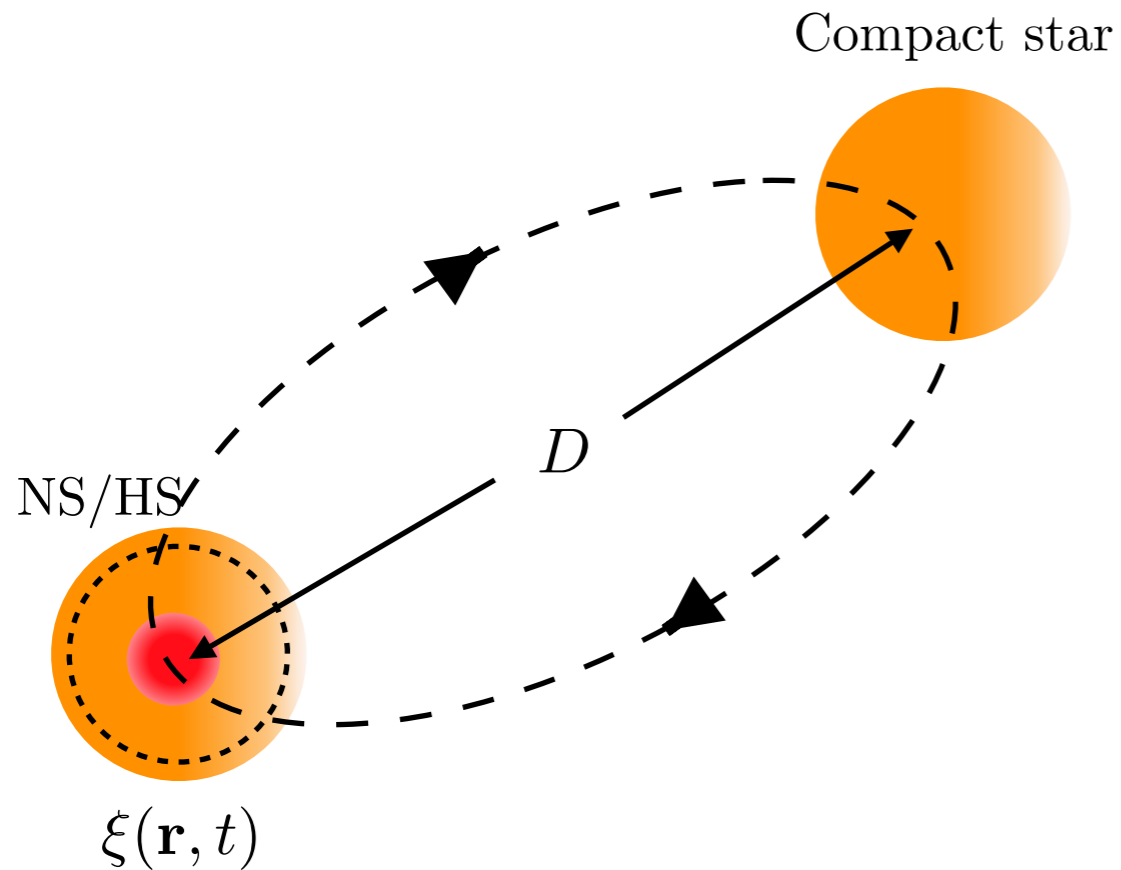
Remind: Wave function



Mode	Q	Q^U	Q^V
i_μ	0.026	0.041	-0.015
i_ρ	-0.019	0.035	-0.054
i_μ (1st PT)	-0.0227	0.00001	-0.00228
i_ρ (with shear)	0.007	0.043	-0.036

Density discontinuity also affects frequency!

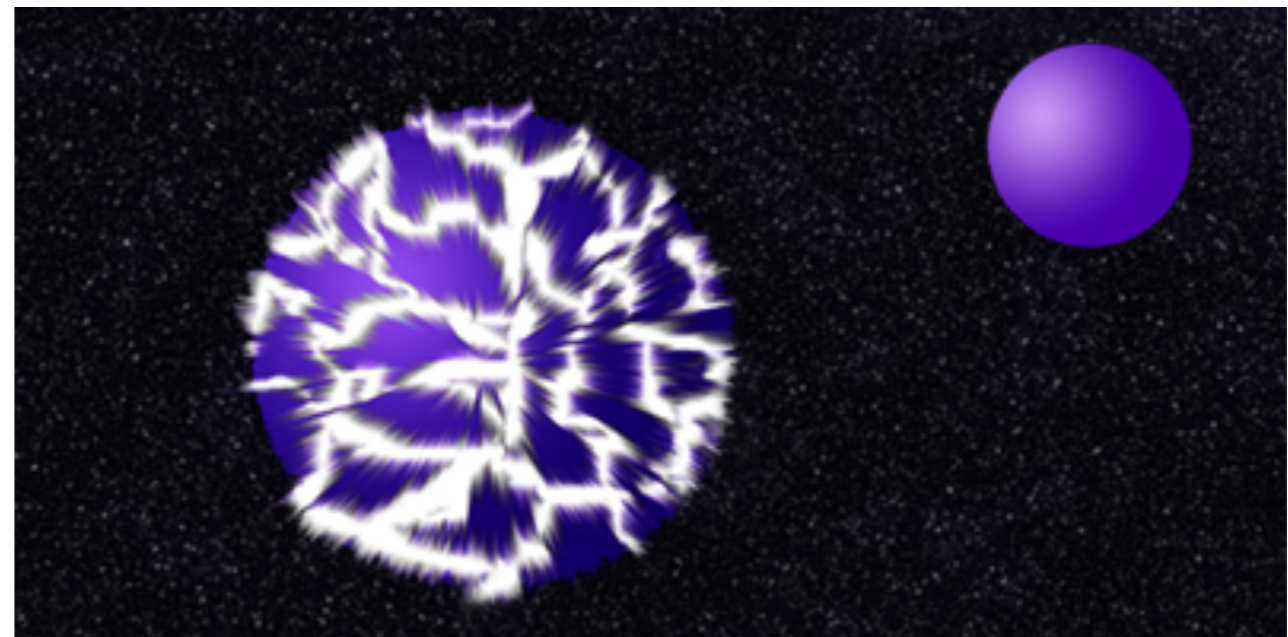
Binary NS system and Gravitational waves



Full-elastic case

Inelastic case:

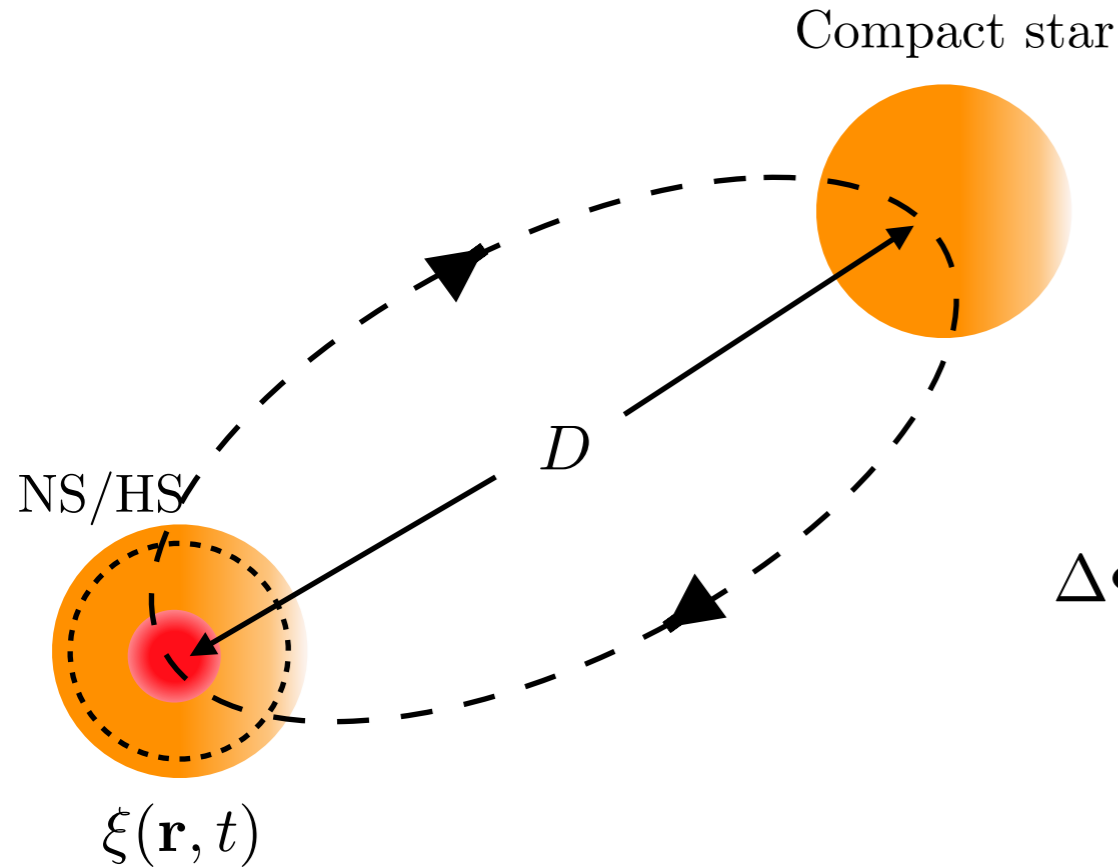
Crust Shattering
Crust Melting



Tsang et al, Phys. Rev. Lett. **108**, 011102

Pan, et al, Phys. Rev. Lett. **125**, 201102

Binary NS system and Gravitational waves



Modification to the gravitational wave Waveform

$$h(f) = A(f)\exp[-i\Phi(f)]$$

$$\Delta\Phi(f) = -\sum_j \sum_{A=1,2} \delta\phi_{j\text{GW}}^{(A)} \left(1 - \frac{f}{f_j^{(A)}}\right) \Theta(f - f_j^{(A)})$$

$$\begin{aligned} \Delta\phi_{j\text{GW}} &= -\frac{5\pi^2}{1024} \left(\frac{Rc^2}{GM}\right)^5 \frac{2q}{1+q} |Q_{2,2}^j|^2 (2\pi\tilde{f}_j)^{-2} \\ &\approx 54 \left(\frac{100\text{ Hz}}{f_j}\right)^2 \left(\frac{Q_{2,2}^j}{0.03}\right)^2 \left(\frac{1.4 M_\odot}{M}\right)^4 \left(\frac{R}{10\text{ km}}\right)^2 \frac{2q}{1+q}, \end{aligned}$$

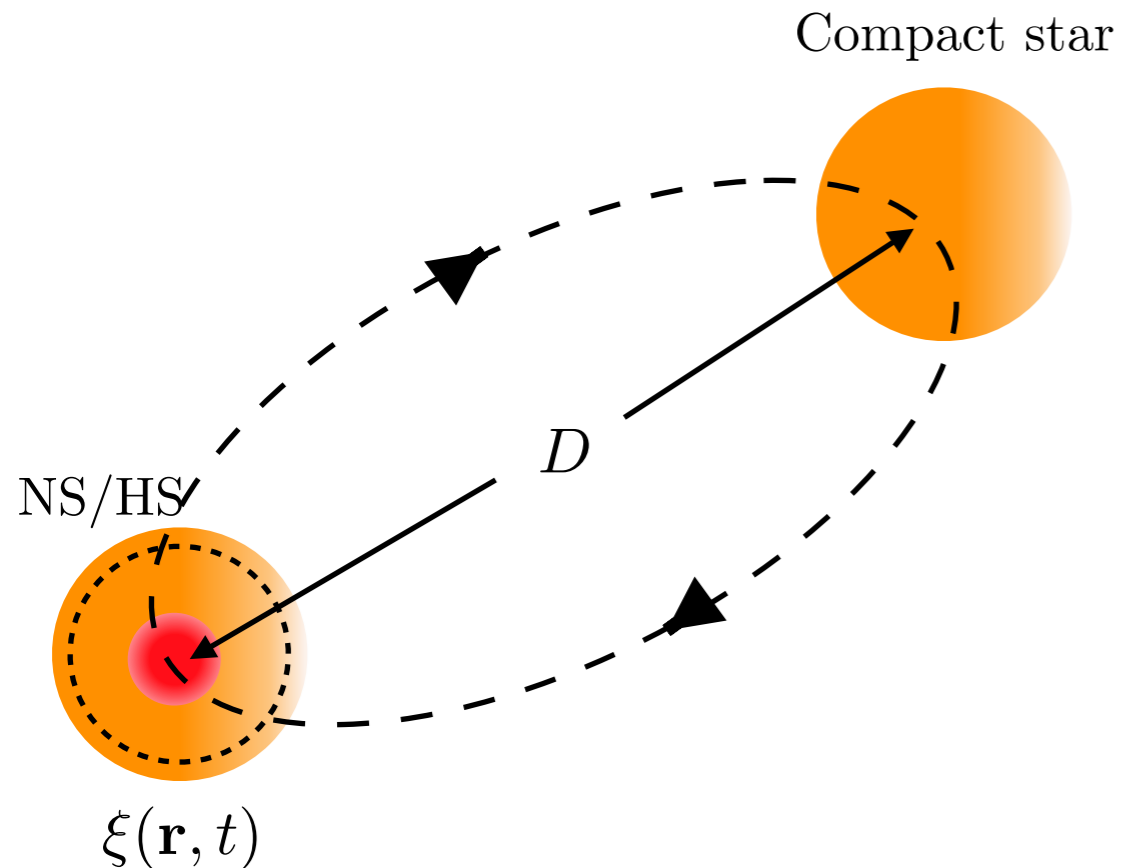
Energy stored in NS oscillation:

- **A earlier merger time**
- **Resonance induced phase shift**

New parameters:

NS oscillation frequency & phase shift

Detectability of phase transition from GW signals



Fisher information analysis (assuming no prior)

$$\Gamma_{mn} = \left(\frac{\partial h}{\partial \theta_m} \middle| \frac{\partial h}{\partial \theta_n} \right),$$

$$(a|b) = 2 \int_0^\infty \frac{a^*(f)b(f) + a(f)b^*(f)}{\underline{S_{hh}(f)}}$$

Detector strain sensitivity

$$\Delta\theta_m = \sqrt{(\mathbf{\Gamma}^{-1})_{mm}}$$

Energy stored in NS oscillation:

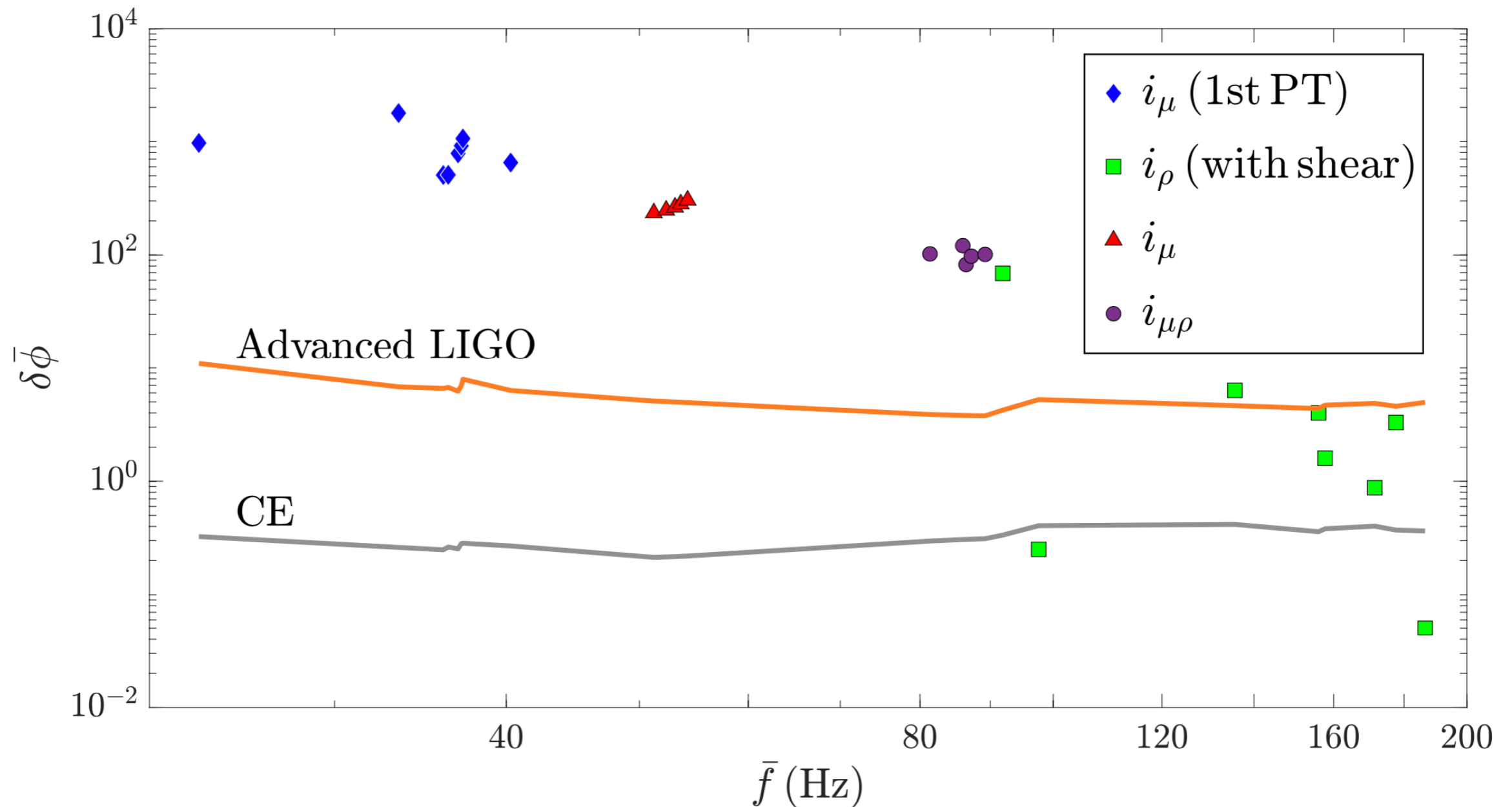
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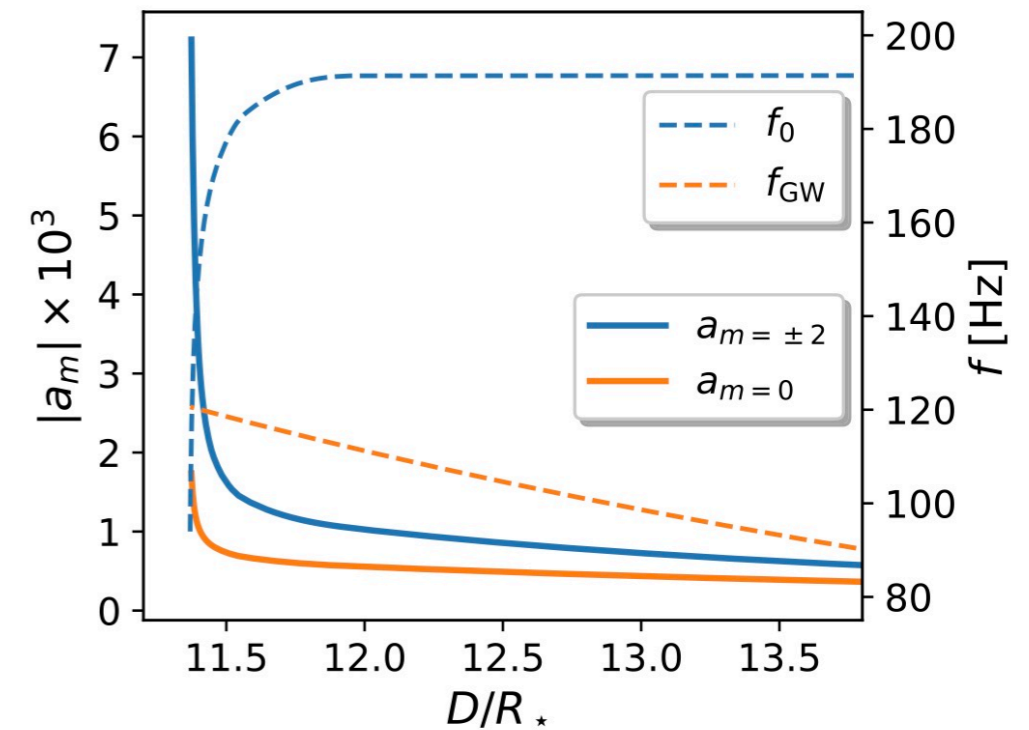
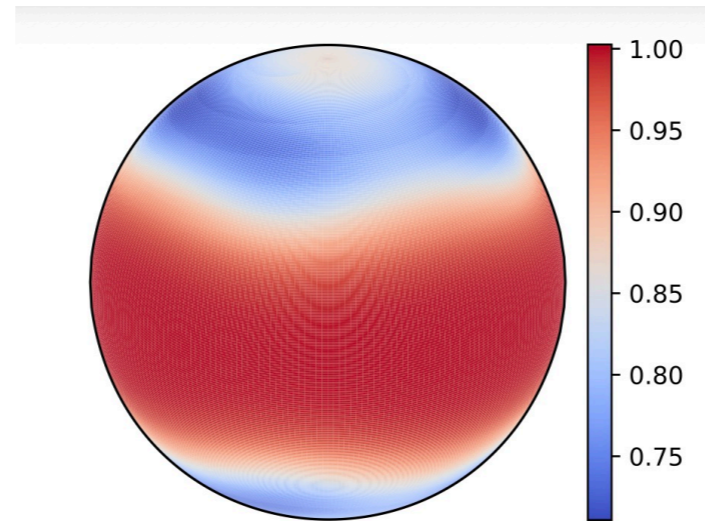
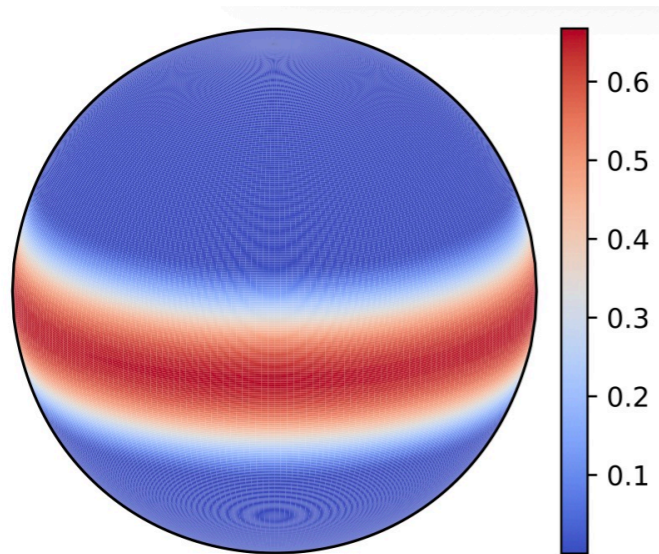
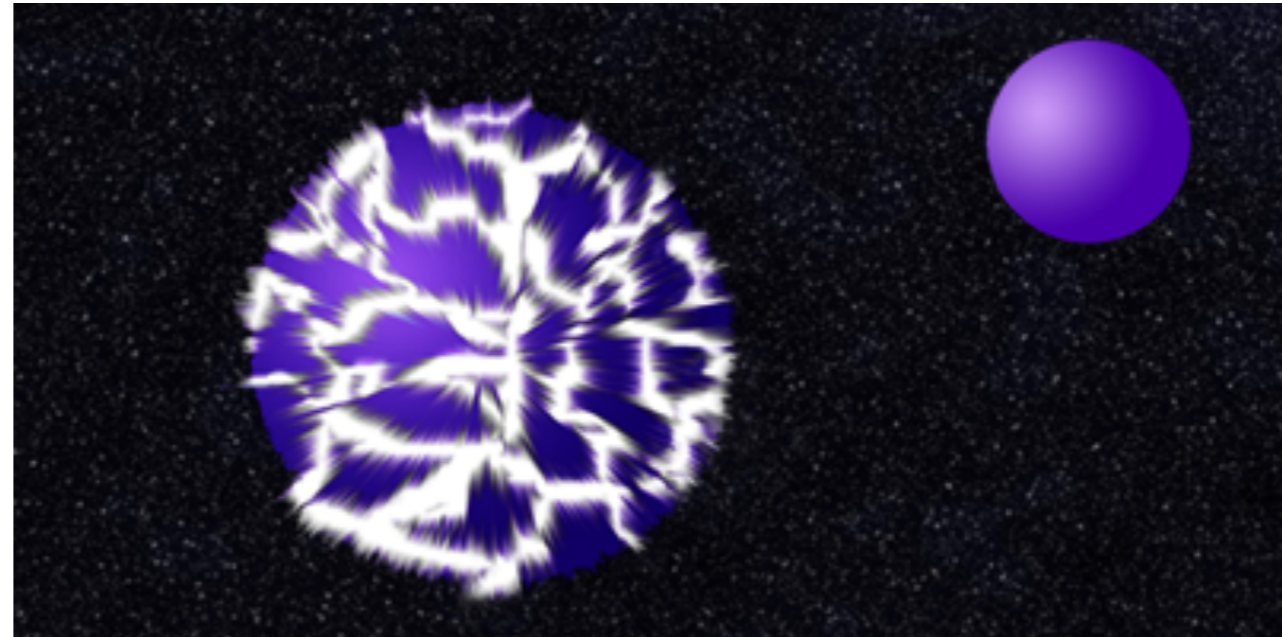
Detectability of phase transition from GW signals

Detectability in the full elastic case



Detectability of phase transition from GW signals

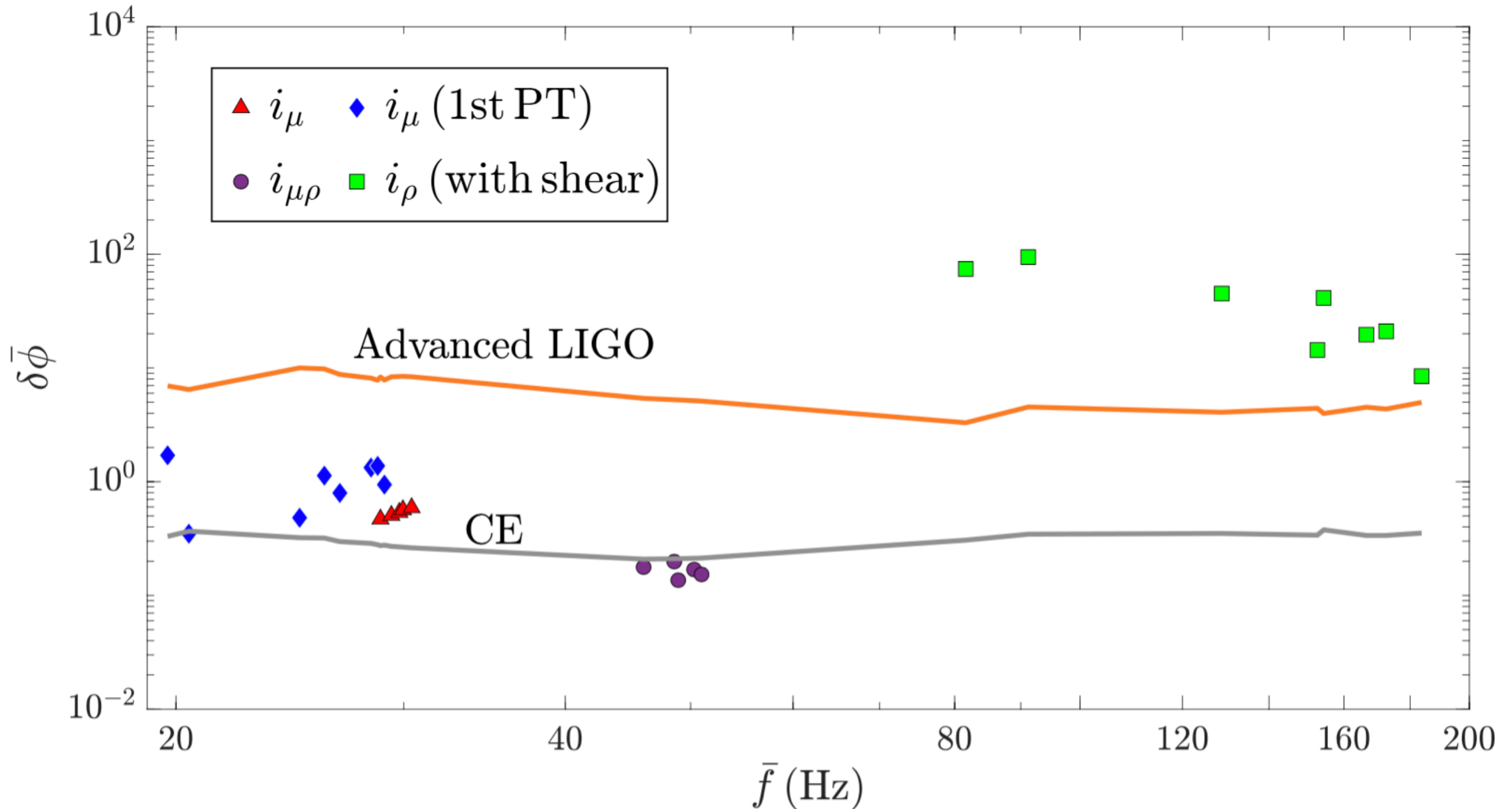
Inelastic case:
Crust Shattering



Crust Melting, from Pan et. al. PRL, 125,201102,2020

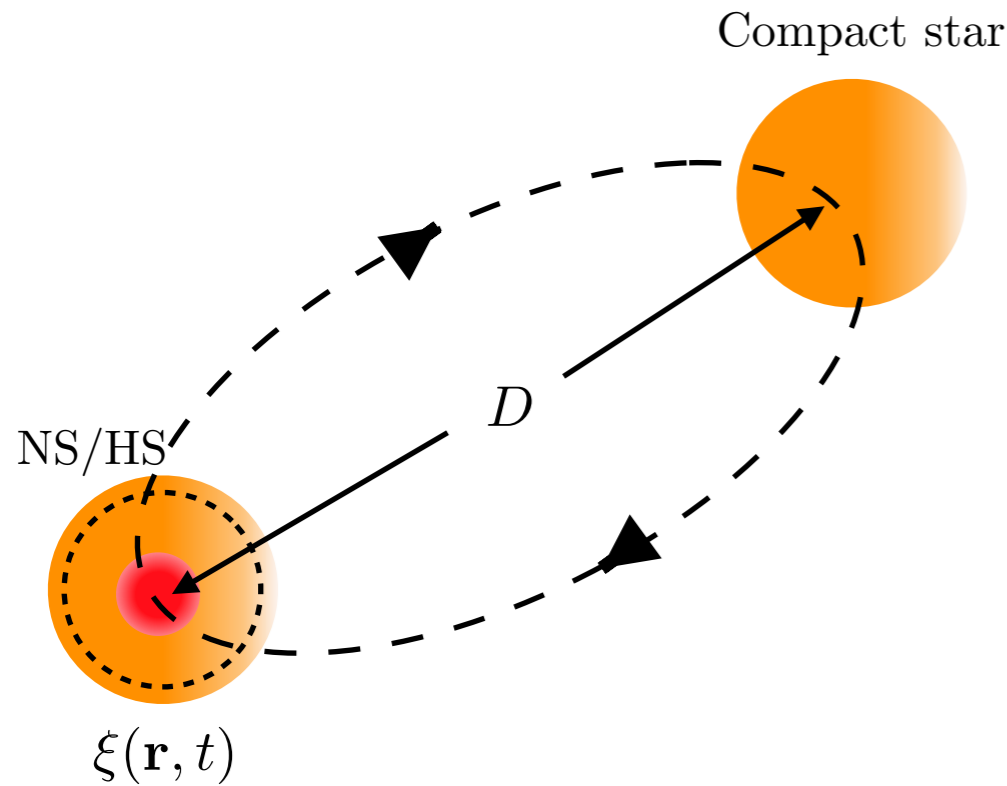
Detectability of phase transition from GW signals

Detectability in the inelastic case



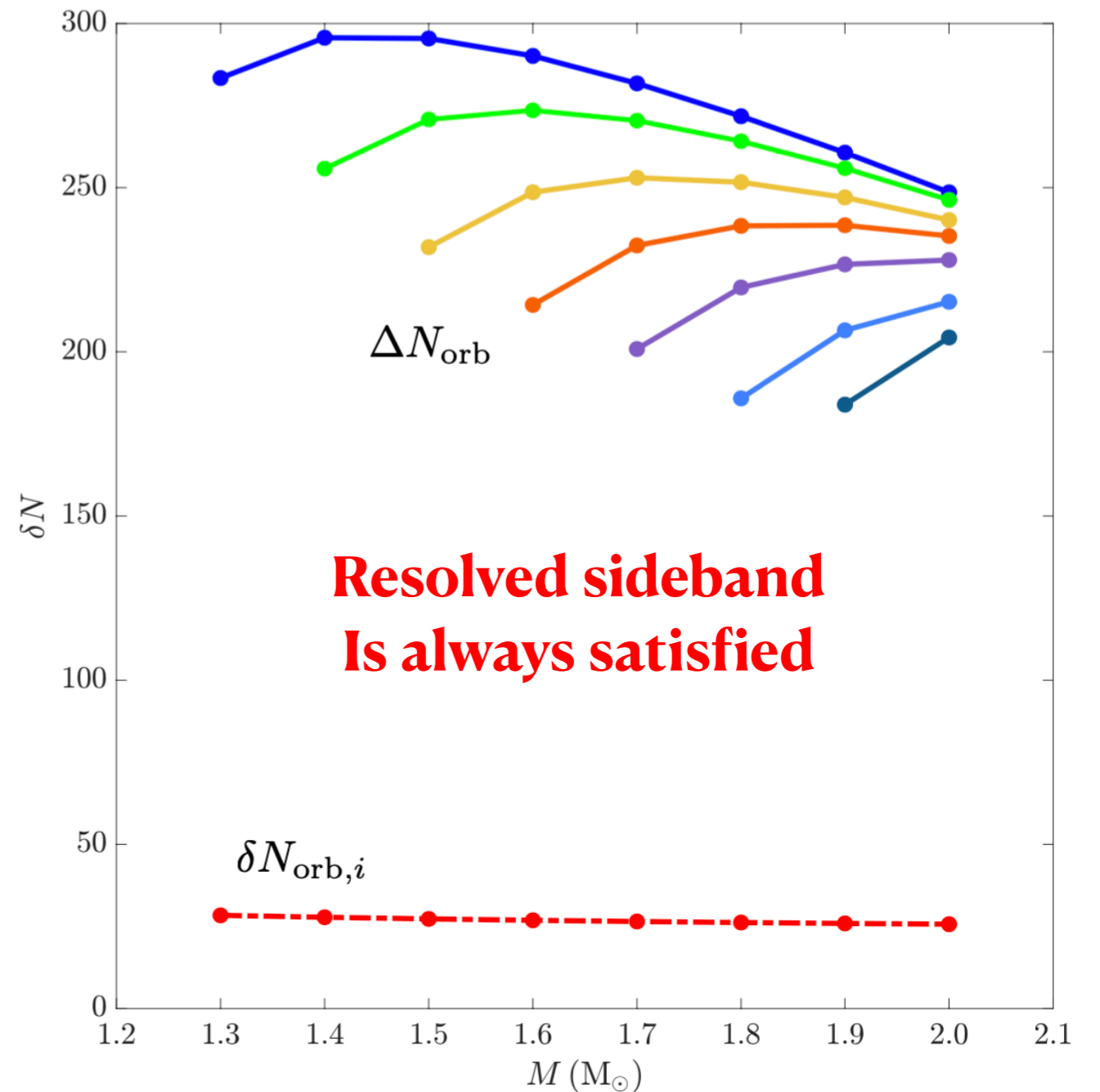
Detectability of phase transition from GW signals

Distinguishing the twin-star



**The on-resonance bandwidth
Must be smaller than the NS-HS
I-mode Frequency difference!**

Resolved sideband limit!



Outlook and Summary

1st order Phase transition could have a minor effect on M-R and deformability

1st order Phase transition can significantly affect Interfacial Mode

These effects are promising to be detected using GWs from BNS

A Complete and consistent GR treatment still lack

Inelastic process is still not very clear

Coupling with other modes is yet to be analysed

Acknowledgement



Jiaxiang Zhu



Chuming Wang



Chengjun Xia
(From Yangzhou University)



Enping Zhou

Micala Oertel, Paris Observatory

and ComPOSE team

Thank you!

Questions?