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NATIONAL ASTRONOMICAL OBSERVATORIES, CAS



# The HI absorption line & anomalous dispersion in pulsar emission

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Kunming

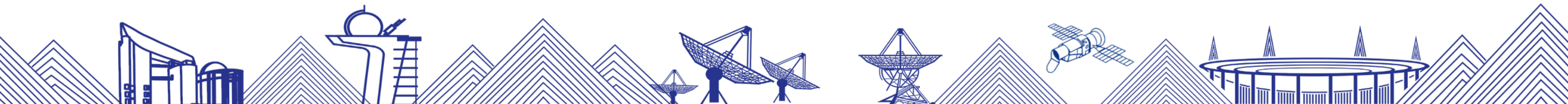
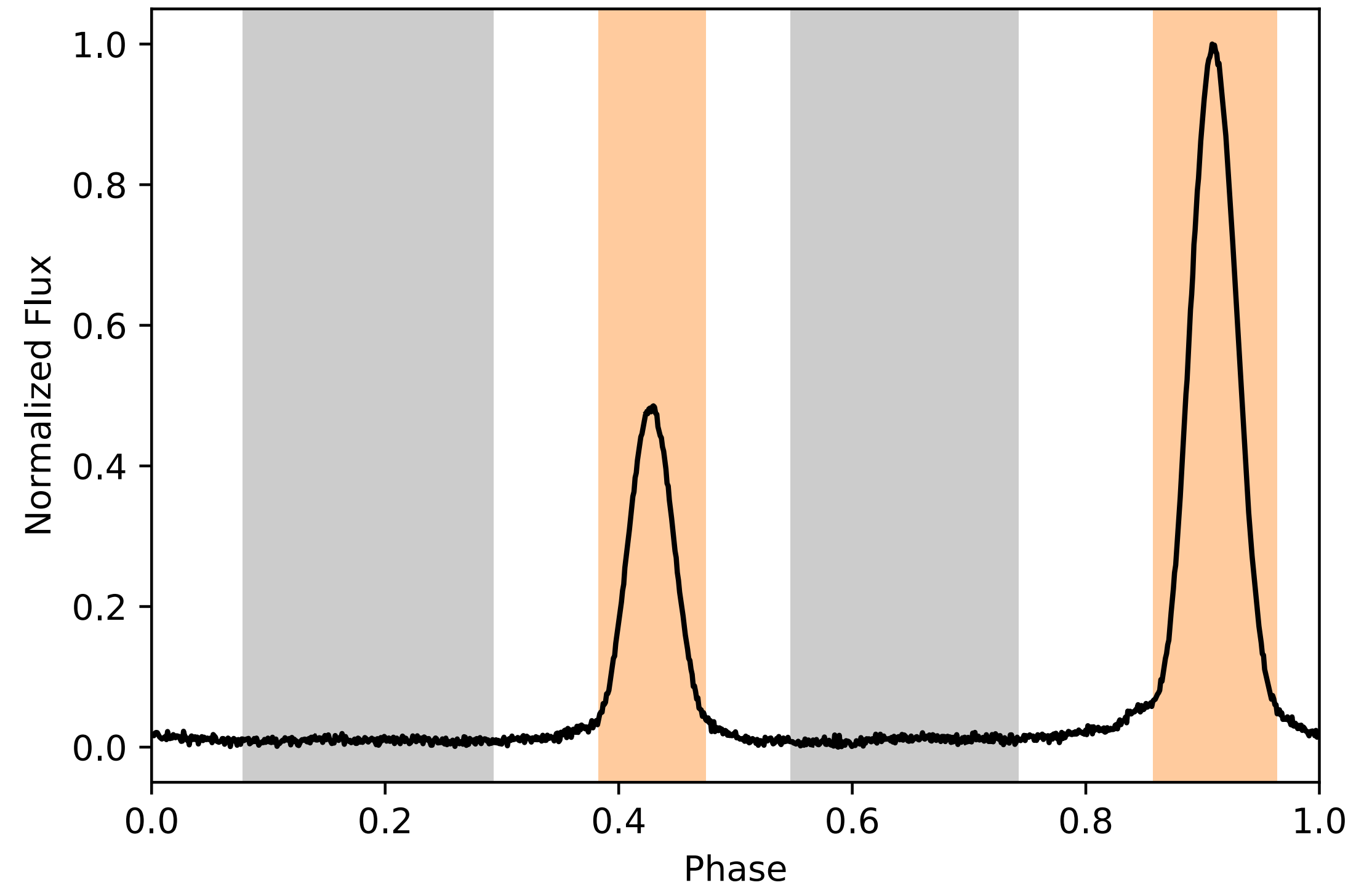
# H I absorption line

- Radiative transfer equation

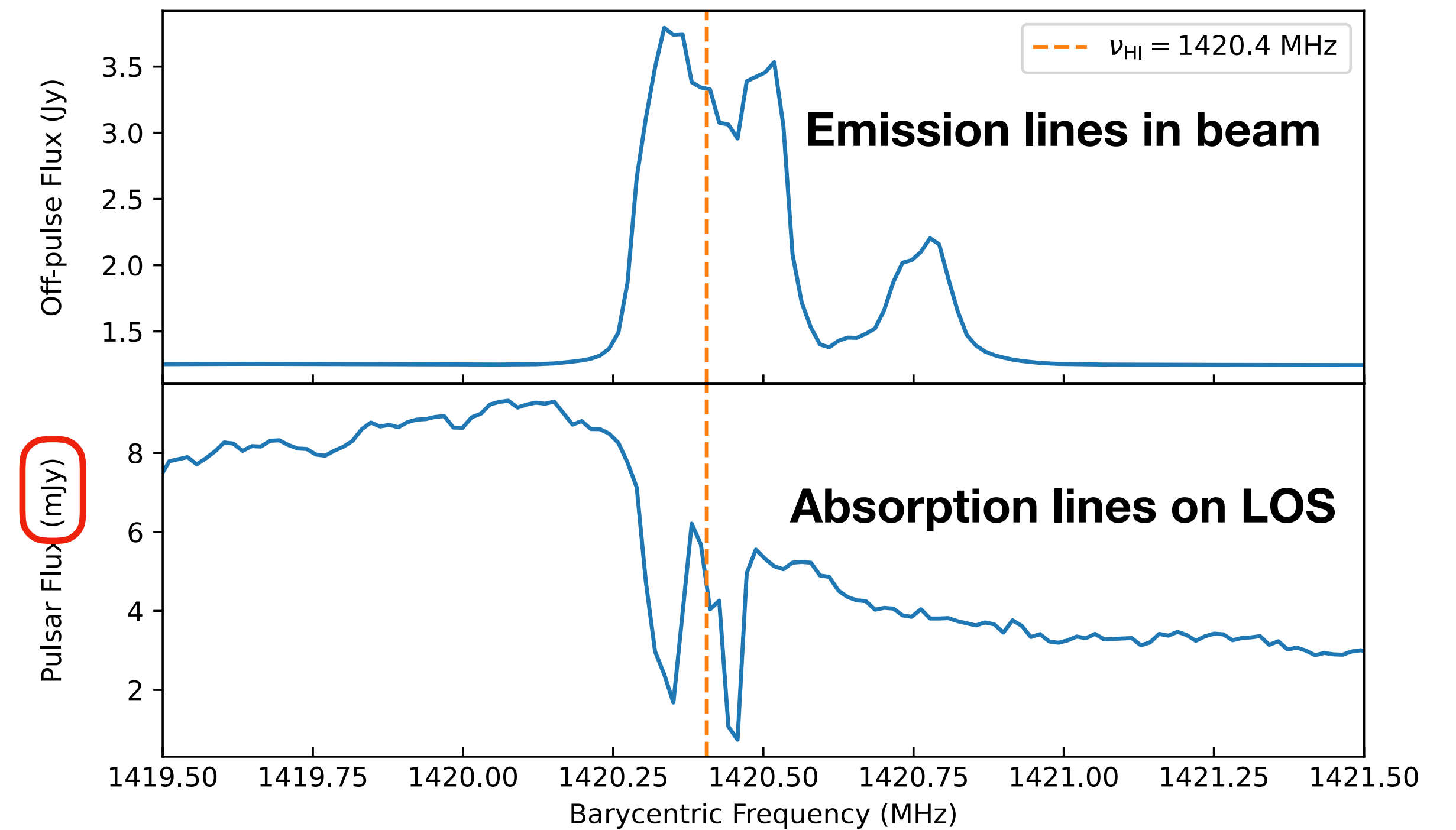
$$\frac{dI_\nu}{ds} = j_\nu - \alpha_\nu I_\nu$$

$$I_\nu = I_{\nu,0} e^{-\tau_\nu} + S_\nu (1 - e^{-\tau_\nu})$$

- On-Off observation  
angular resolution  
time resolution: pulsar

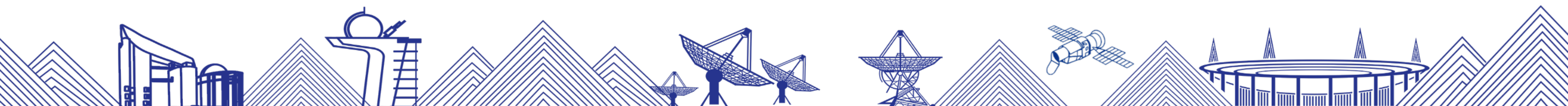
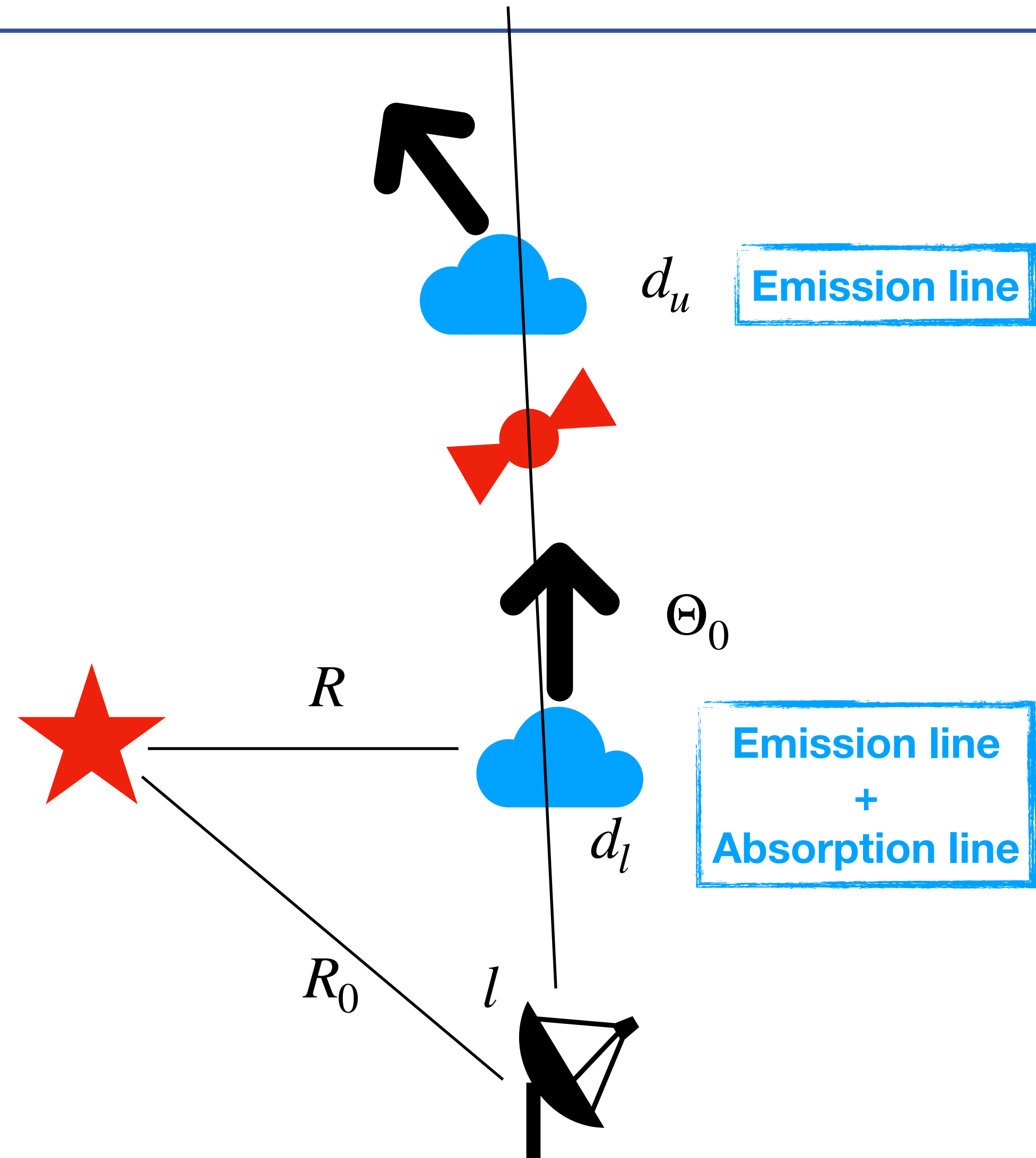


- PSR B1937+21 (J1939+2134)  
P = 1.56 ms  
bright
- DSPSR  
CPU off-line  
500 MHz/32768 chan = 15 kHz/chan
- Scintillation



# Kinematic distance

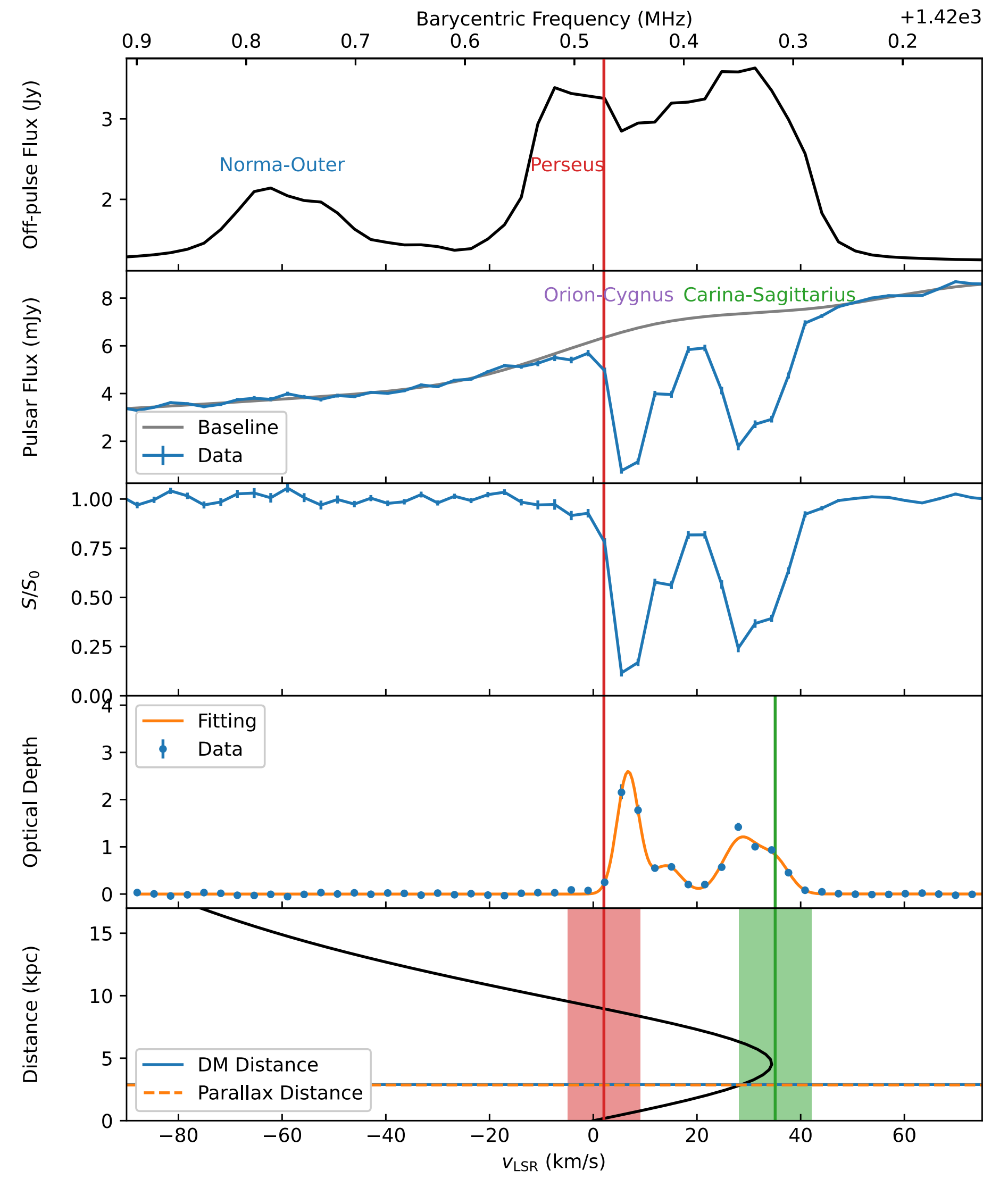
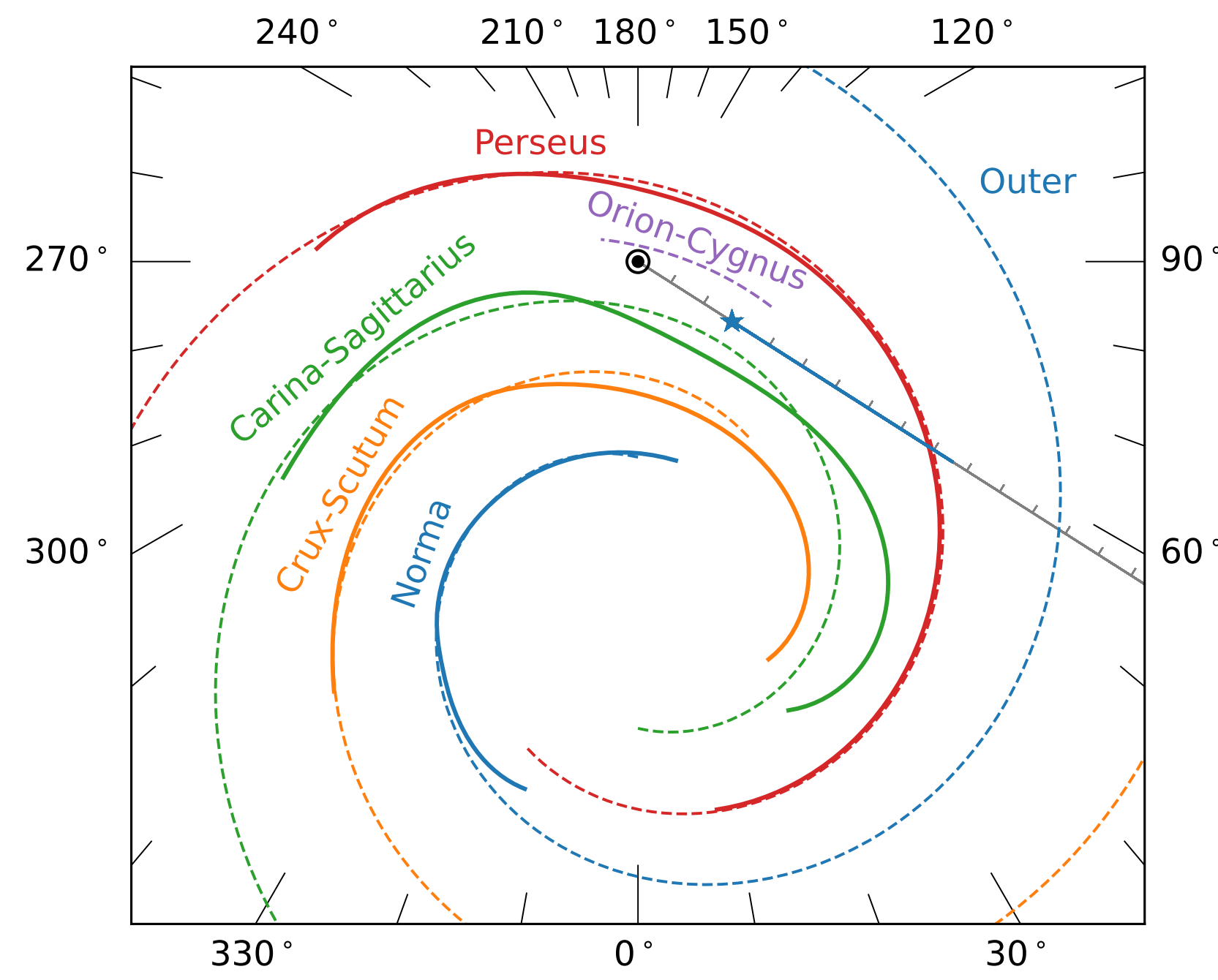
- Galactic rotation curve  
 $R_0 = 8.5 \text{ kpc}$ ,  $\Theta_0 = 220 \text{ km/s}$
- Radial velocity of HI cloud  
 $R^2 = R_0^2 + d^2 - 2R_0d \cos l$   
 $v_r = R_0(\omega - \omega_0) \sin l \cos b$   
 Local Standard of Rest (LSR)  
 streaming & random motion:  $\sim 7 \text{ km/s}$   
 (Fich et al. 1989, Frail et al. 1990)
- Lower bound of pulsar distance  
 furthestmost cloud with absorption
- Upper bound of pulsar distance  
 nearest cloud without absorption



- Lower bound  
2.8 - 6.3 kpc  
Carina-Sagittarius Arm

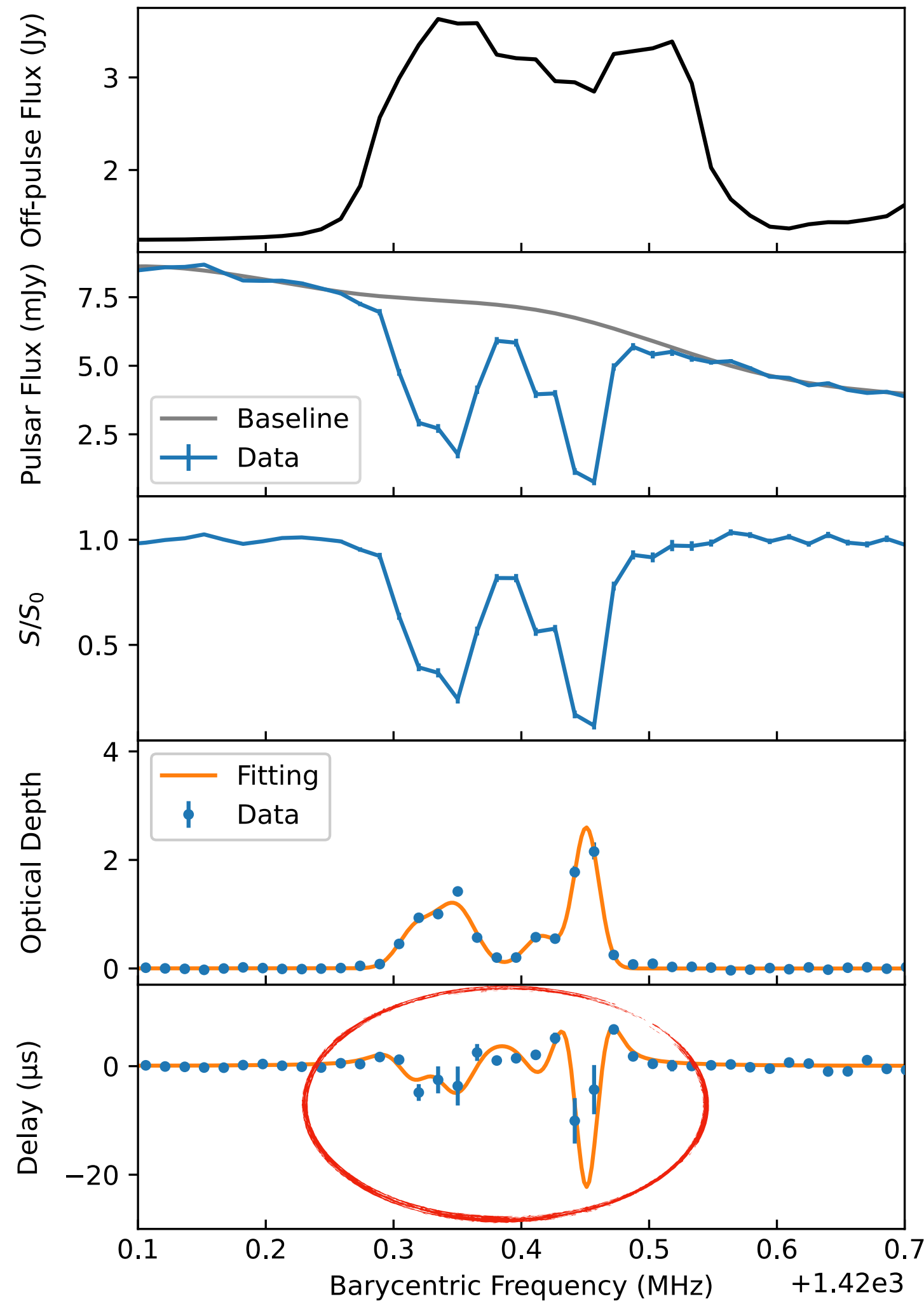
- Upper bound  
8.3 - 9.6 kpc  
Perseus Arm

- Previous results  
DM distance: 2.9 kpc (YMW16)  
VLBI distance: 2.6 kpc (Ding et al. 2023)  
kinematic distance:  $d_l = 4.6$  kpc,  $d_u = 14.8$  kpc (Weisberg et al. 2008)

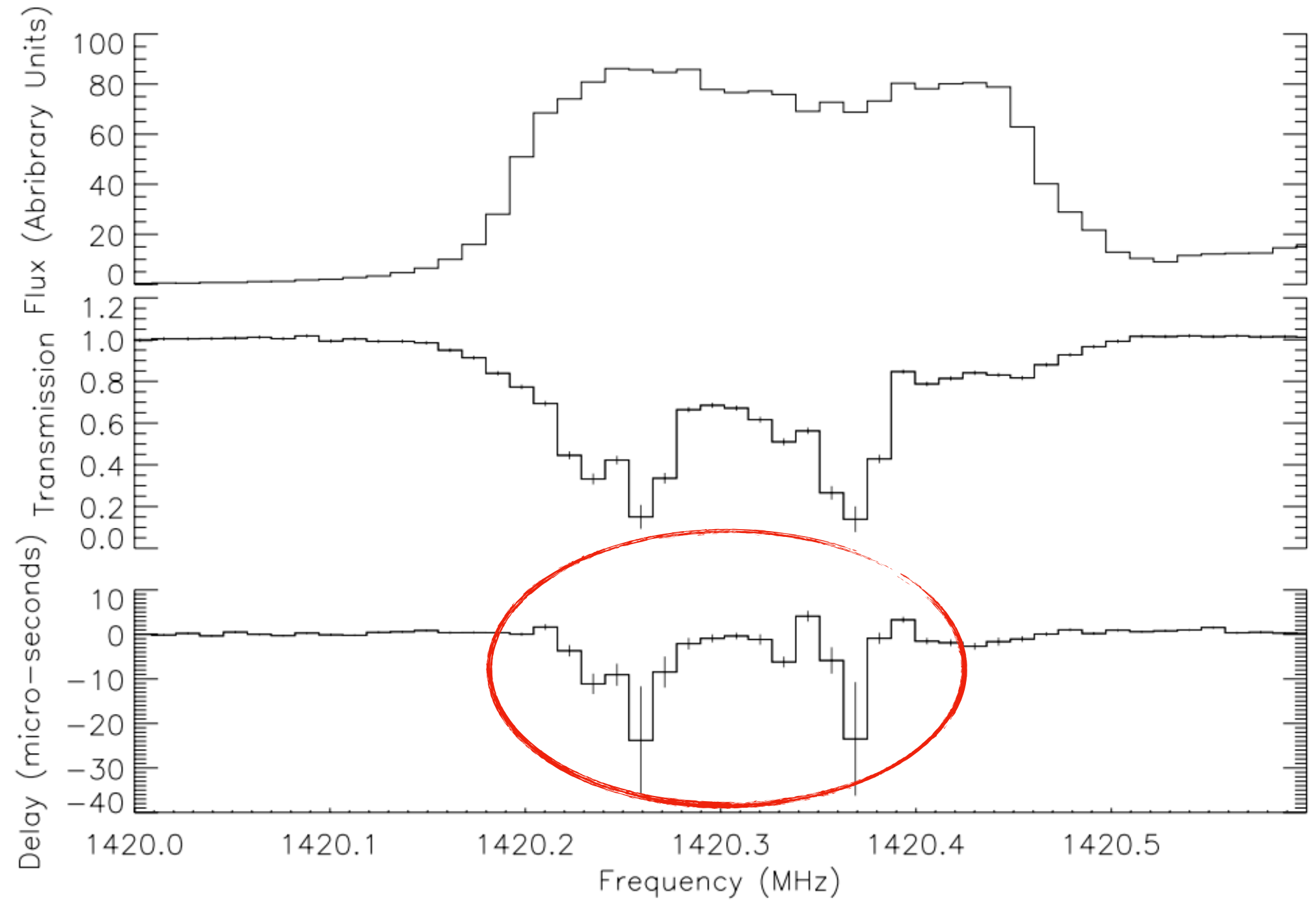




# Timing at H I absorption line



FAST result



Arecibo result  
Jenet et al. 2010

**What about causality?**



# Kramers-Kronig relation

- Causality in Green's function of  $\epsilon(\omega)$

$$G(\tau < 0) = 0$$

$$\epsilon(\omega)/\epsilon_0 = 1 + \int_0^{\infty} G(\tau) e^{i\omega\tau} d\tau$$

$\epsilon(\omega)$  is analytic in the upper half- $\omega$ -plane.

- Kramers-Kronig relation

$$\boxed{\text{Re}[\epsilon(\omega)/\epsilon_0]} = 1 + \frac{1}{\pi} \mathcal{P} \int_{-\infty}^{+\infty} \frac{\text{Im}[\epsilon(\omega')/\epsilon_0]}{\omega' - \omega} d\omega'$$

$$\text{Im}[\epsilon(\omega)/\epsilon_0] = -\frac{1}{\pi} \mathcal{P} \int_{-\infty}^{+\infty} \frac{\text{Re}[\epsilon(\omega')/\epsilon_0]}{\omega' - \omega} d\omega'$$

absorption  $\iff$  dispersion

- Lorentz dispersion model  
Damped harmonic oscillator

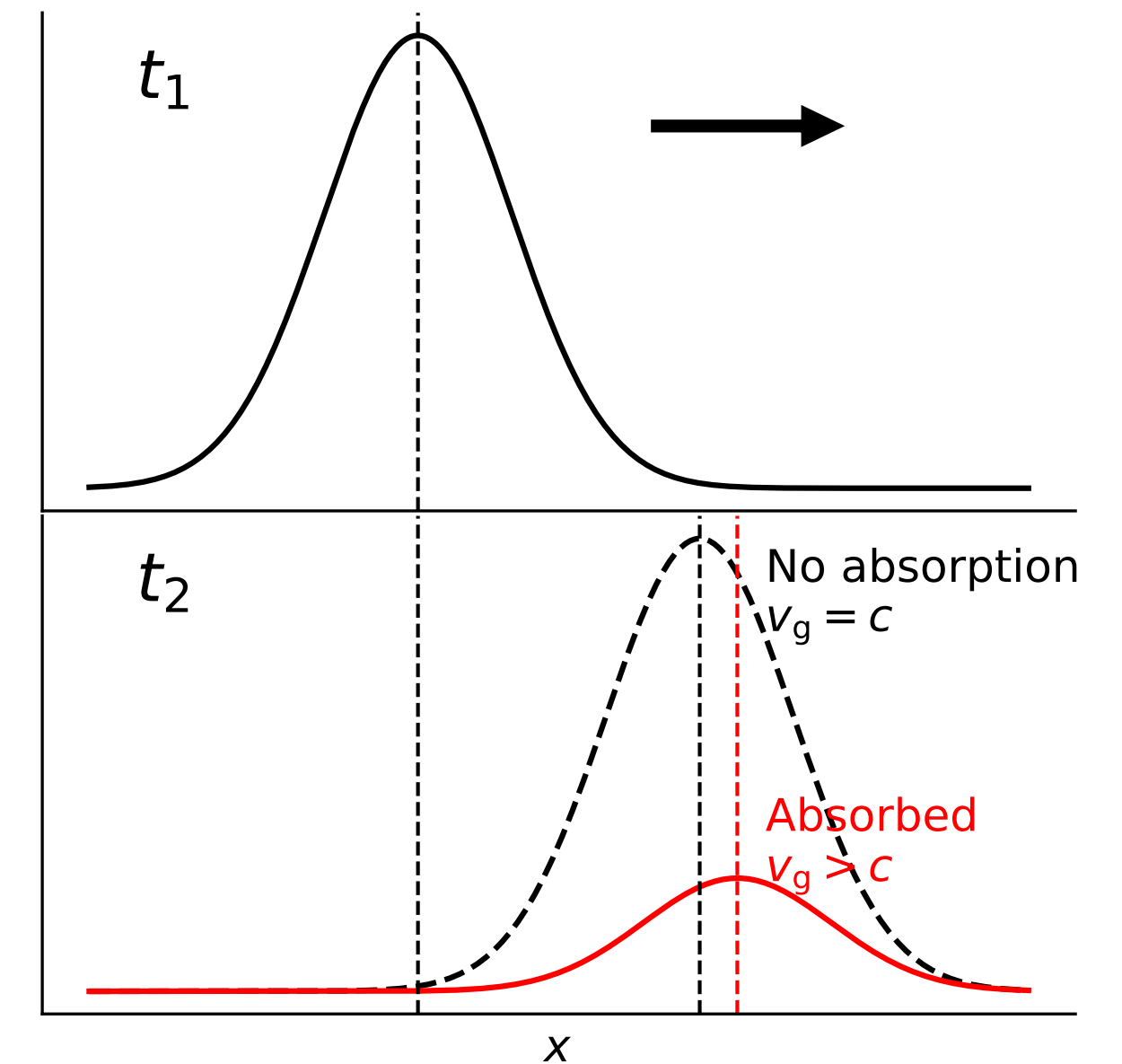
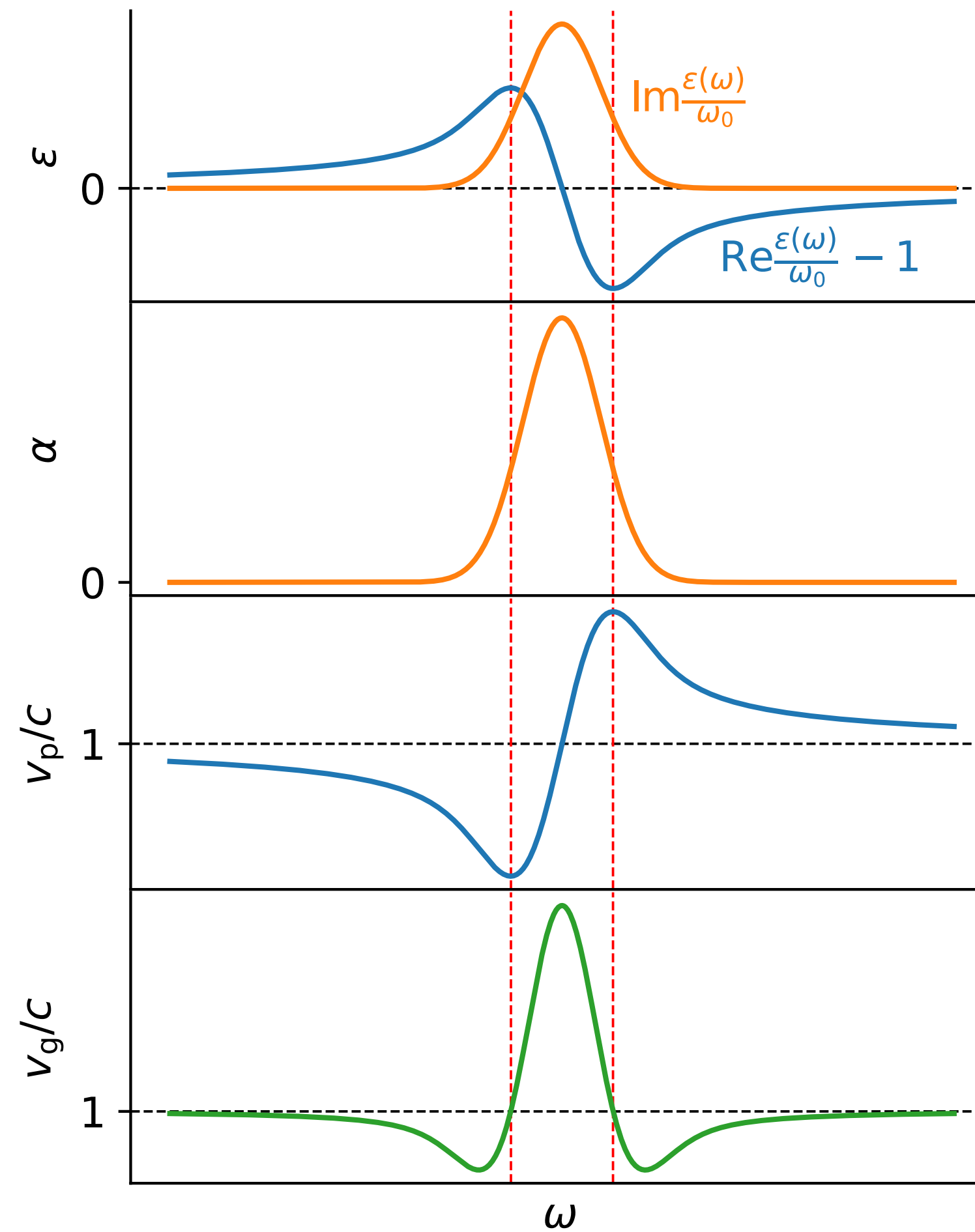
$$m_e \ddot{\mathbf{x}} + m_e \gamma \dot{\mathbf{x}} + m_e \omega_0^2 \mathbf{x} = -e \mathbf{E}_0$$

$$\frac{\epsilon(\omega)}{\epsilon_0} = 1 + \frac{Ne^2}{\epsilon_0 m_e} \sum_i \frac{f_i}{\omega_i^2 - \omega^2 - i\omega\gamma_i}$$

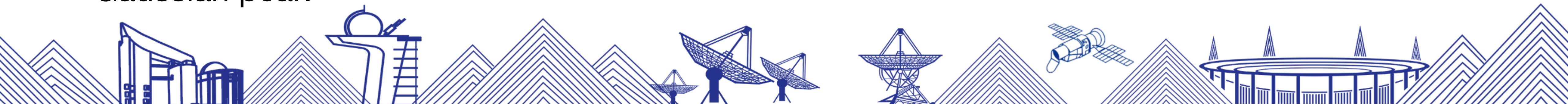


# Anomalous dispersion

- Normal dispersion  
 $n$  increases with  $\omega$
- Anomalous dispersion  
 $n$  decreases with  $\omega$
- Phase velocity  $v_p = \omega/k = c/n$   
Group velocity  $v_g = d\omega/dk$   
$$v_g = \frac{c}{n(\omega) + \omega \frac{dn}{d\omega}}$$
  
 $v_g > c$  around absorption lines
- Group velocity is defined at Gaussian peak



**Causality is preserved**





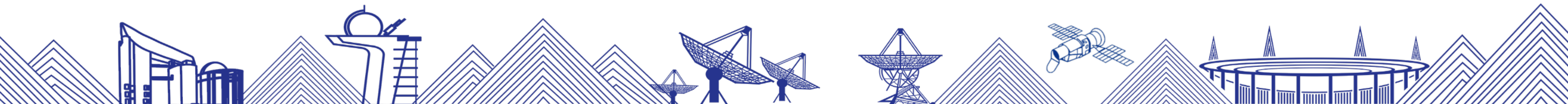
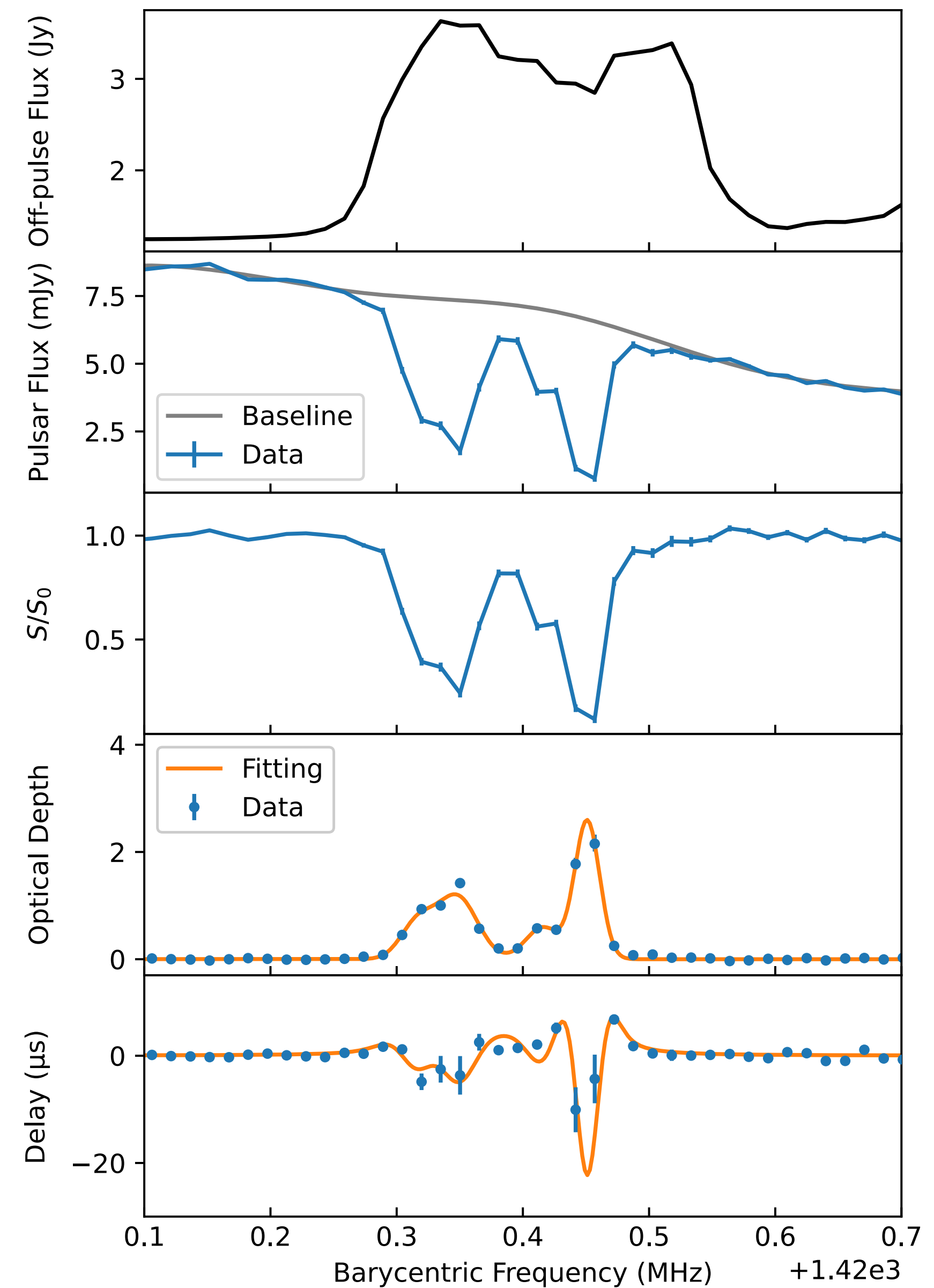
- Absorption lines  
4 Gaussian components in optical depth

$$\tau(f) = \tau_0 e^{-\frac{(f-f_c)^2}{2f_d^2}}$$

- Prediction of Lorentz model

$$\Delta t(f) = \tau_0 \left( \frac{f-f_c}{4\pi f_d^2} \right) \text{Im} \left[ w \left( \frac{f-f_c}{\sqrt{2}f_d} \right) \right] - \frac{\tau_0}{2\sqrt{2}\pi^{3/2}f_d}$$

Faddeeva function  $w(z) = e^{-z^2} \text{erfc}(-iz)$   
(Janet et al. 2010)



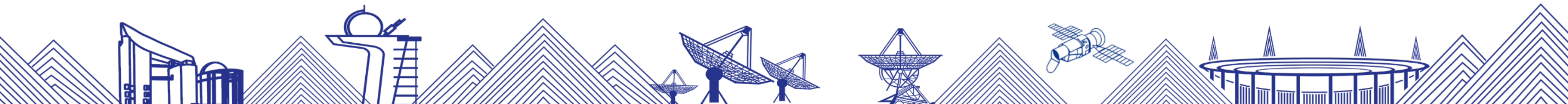


# Summary

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- Kinematic distance of PSR B1937+21 between 2 Galactic arms
- Anomalous dispersion  
~  $10 \mu\text{s}$  faster-than-light
- Requires high S/N  
large telescopes (Arecibo, FAST and ???)  
bright pulsars (B1937+21 and ???)  
good luck (HI cloud, scintillation)  
new FAST proposal for more pulsars

***Thanks!***



# Reference

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